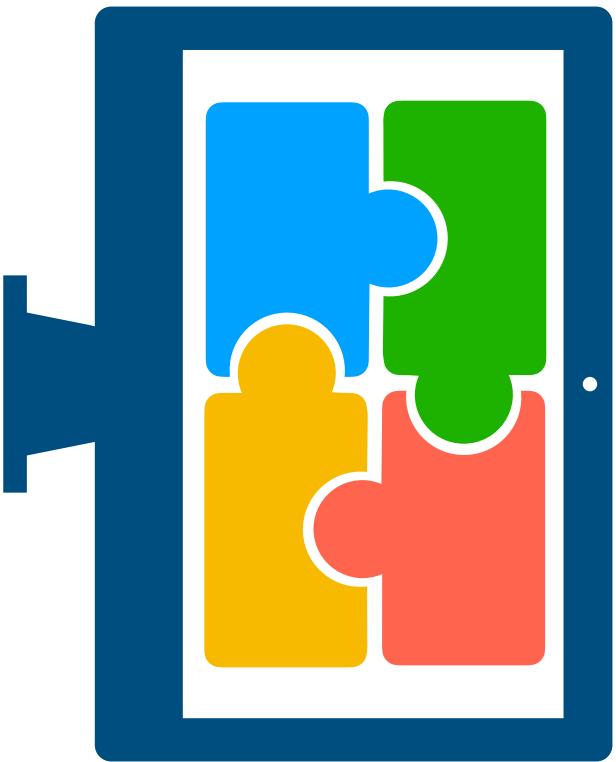


# Prontuario

## Linguaggi di Programmazione



# Algoritmo di unificazione

delete

$\mathcal{G} \cup \{t \stackrel{?}{=} t\}$   
becomes  
 $\mathcal{G}$

swap

$\mathcal{G} \cup \{x \stackrel{?}{=} t\}$   
becomes if  $x \in vars(\mathcal{G}) \setminus vars(t)$   
 $\mathcal{G}[x = t] \cup \{x \stackrel{?}{=} t\}$

eliminate

$\mathcal{G} \cup \{f(t_1, \dots, t_m) \stackrel{?}{=} x\}$   
becomes

$\mathcal{G} \cup \{x \stackrel{?}{=} f(t_1, \dots, t_m)\}$

decompose

$\mathcal{G} \cup \{f(t_1, \dots, t_m) \stackrel{?}{=} f(u_1, \dots, u_m)\}$   
becomes

$\mathcal{G} \cup \{t_1 \stackrel{?}{=} u_1, \dots, t_m \stackrel{?}{=} u_m\}$

occur-check

$\mathcal{G} \cup \{x \stackrel{?}{=} f(t_1, \dots, t_m)\}$

fails if  $x \in vars(f(t_1, \dots, t_m))$

conflict

$\mathcal{G} \cup \{f(t_1, \dots, t_m) \stackrel{?}{=} g(u_1, \dots, u_h)\}$

fails if  $f \neq g$  or  $m \neq h$

# Sintassi | IMP

**Definition 3.1 (IMP: syntax).** The following productions define the syntax of IMP:

$$\begin{array}{lll} a \in Aexp & ::= & n \mid x \mid a_0 + a_1 \mid a_0 - a_1 \mid a_0 \times a_1 \\ b \in Bexp & ::= & \nu \mid a_0 = a_1 \mid a_0 \leq a_1 \mid \neg b \mid b_0 \vee b_1 \mid b_0 \wedge b_1 \\ c \in Com & ::= & \text{skip} \mid x := a \mid c_0; c_1 \mid \text{if } b \text{ then } c_0 \text{ else } c_1 \mid \text{while } b \text{ do } c \end{array}$$

# SOS rules

$$\overline{\langle x, \sigma \rangle \rightarrow \sigma(x)} \text{ (ide)}$$

$$\frac{\overline{\langle a_0, \sigma \rangle \rightarrow n_0} \quad \overline{\langle a_1, \sigma \rangle \rightarrow n_1}}{\langle a_0 + a_1, \sigma \rangle \rightarrow n_0 + n_1} \text{ (sum)}$$

$$\frac{\overline{\langle a_0, \sigma \rangle \rightarrow n_0} \quad \overline{\langle a_1, \sigma \rangle \rightarrow n_1}}{\langle a_0 \times a_1, \sigma \rangle \rightarrow n_0 \times n_1} \text{ (prod)}$$

# SOS Rules

$$\frac{\langle b, \sigma \rangle \rightarrow v}{\langle \neg b, \sigma \rangle \rightarrow \neg v} \text{ (not)}$$

$$\frac{\langle a_0, \sigma \rangle \rightarrow n_0 \quad \langle a_1, \sigma \rangle \rightarrow n_1}{\langle a_0 = a_1, \sigma \rangle \rightarrow (n_0 = n_1)} \text{ (equ)}$$

$$\frac{\langle b_0, \sigma \rangle \rightarrow v_0 \quad \langle b_1, \sigma \rangle \rightarrow v_1}{\langle b_0 \vee b_1, \sigma \rangle \rightarrow (v_0 \vee v_1)} \text{ (or)}$$

$$\frac{\langle a_0, \sigma \rangle \rightarrow n_0 \quad \langle a_1, \sigma \rangle \rightarrow n_1}{\langle a_0 \leq a_1, \sigma \rangle \rightarrow (n_0 \leq n_1)} \text{ (leq)}$$

$$\frac{\langle b_0, \sigma \rangle \rightarrow v_0 \quad \langle b_1, \sigma \rangle \rightarrow v_1}{\langle b_0 \wedge b_1, \sigma \rangle \rightarrow (v_0 \wedge v_1)} \text{ (and)}$$

# SOS Rules

$$\overline{\langle \text{skip}, \sigma \rangle \rightarrow \sigma} \quad (\text{skip})$$

$$\frac{\langle a, \sigma \rangle \rightarrow m}{\langle x := a, \sigma \rangle \rightarrow \sigma[m/x]} \quad (\text{assign})$$

$$\frac{\langle b, \sigma \rangle \rightarrow \text{false} \quad \langle c_1, \sigma \rangle \rightarrow \sigma'}{\langle \text{if } b \text{ then } c_0 \text{ else } c_1, \sigma \rangle \rightarrow \sigma'} \quad (\text{iff})$$

$$\frac{\langle b, \sigma \rangle \rightarrow \text{true} \quad \langle c_0, \sigma \rangle \rightarrow \sigma'}{\langle \text{if } b \text{ then } c_0 \text{ else } c_1, \sigma \rangle \rightarrow \sigma'} \quad (\text{iftt})$$

$$\frac{\langle c_0, \sigma \rangle \rightarrow \sigma'' \quad \langle c_1, \sigma'' \rangle \rightarrow \sigma'}{\langle c_0; c_1, \sigma \rangle \rightarrow \sigma'} \quad (\text{seq})$$

$$\frac{\langle b, \sigma \rangle \rightarrow \text{true} \quad \langle c, \sigma \rangle \rightarrow \sigma'' \quad \langle \text{while } b \text{ do } c, \sigma'' \rangle \rightarrow \sigma'}{\langle \text{while } b \text{ do } c, \sigma \rangle \rightarrow \sigma'} \quad (\text{whtt})$$

$$\frac{\langle b, \sigma \rangle \rightarrow \text{false}}{\langle \text{while } b \text{ do } c, \sigma \rangle \rightarrow \sigma} \quad (\text{whff})$$

# Semantica denotazione

di  $\mathbf{IMP}$

$$\mathcal{A}[\mathit{n}] \sigma \stackrel{\text{def}}{=} n$$

$$\mathcal{A}[x] \sigma \stackrel{\text{def}}{=} \sigma x$$

$$\mathcal{A}[a_0 + a_1] \sigma \stackrel{\text{def}}{=} (\mathcal{A}[a_0] \sigma) + (\mathcal{A}[a_1] \sigma)$$

$$\mathcal{A}[a_0 - a_1] \sigma \stackrel{\text{def}}{=} (\mathcal{A}[a_0] \sigma) - (\mathcal{A}[a_1] \sigma)$$

$$\mathcal{A}[a_0 \times a_1] \sigma \stackrel{\text{def}}{=} (\mathcal{A}[a_0] \sigma) \times (\mathcal{A}[a_1] \sigma)$$

$$\mathcal{C}[\mathbf{skip}] \sigma \stackrel{\text{def}}{=} \sigma$$

$$\mathcal{C}[x := a] \sigma \stackrel{\text{def}}{=} \sigma[\mathcal{A}[a] \sigma /_x]$$

$$\mathcal{C}[c_0; c_1] \sigma \stackrel{\text{def}}{=} \mathcal{C}[c_1]^*(\mathcal{C}[c_0] \sigma)$$

$$\mathcal{B}[v] \sigma \stackrel{\text{def}}{=} v$$

$$\mathcal{B}[a_0 = a_1] \sigma \stackrel{\text{def}}{=} (\mathcal{A}[a_0] \sigma) = (\mathcal{A}[a_1] \sigma)$$

$$\mathcal{B}[a_0 \leq a_1] \sigma \stackrel{\text{def}}{=} (\mathcal{A}[a_0] \sigma) \leq (\mathcal{A}[a_1] \sigma)$$

$$\mathcal{B}[\neg b] \sigma \stackrel{\text{def}}{=} \neg(\mathcal{B}[b] \sigma)$$

$$\mathcal{B}[b_0 \vee b_1] \sigma \stackrel{\text{def}}{=} (\mathcal{B}[b_0] \sigma) \vee (\mathcal{B}[b_1] \sigma)$$

$$\mathcal{B}[b_0 \wedge b_1] \sigma \stackrel{\text{def}}{=} (\mathcal{B}[b_0] \sigma) \wedge (\mathcal{B}[b_1] \sigma)$$

$$\mathcal{C}[\mathbf{while } b \mathbf{ do } c] = \Gamma_{b,c} \mathcal{C}[\mathbf{while } b \mathbf{ do } c]$$

$$\mathcal{C}[\mathbf{while } b \mathbf{ do } c] \stackrel{\text{def}}{=} \text{fix } \Gamma_{b,c} = \bigsqcup_{n \in \mathbb{N}} \Gamma_{b,c}^n(\perp_{\Sigma} \rightarrow \perp_{\Sigma})$$

$$\Gamma_{b,c} \stackrel{\text{def}}{=} \lambda \varphi. \lambda \sigma. \mathcal{B}[b] \sigma \rightarrow \varphi^*(\mathcal{C}[c] \sigma), \sigma$$

# Sintassi HOFL

$$\begin{array}{c} t ::= x \mid n \mid t_0 \text{ op } t_1 \mid \text{if } t \text{ then } t_0 \text{ else } t_1 \\ \hline (t_0, t_1) \mid \text{fst}(t) \mid \text{snd}(t) \\ \hline \lambda x. t \mid t_0 \ t_1 \\ \hline \text{rec } x. t \end{array}$$

# Sistema di tipi

$$\frac{\frac{x : \widehat{\tau}}{n : int} \quad \frac{t_0 : int \quad t_1 : int}{t_0 \text{ op } t_1 : int}}{t_0 : \tau \quad t_1 : \tau} \quad \text{if } t \text{ then } t_0 \text{ else } t_1 : \tau$$

$$\frac{t_0 : \tau_0 \quad t_1 : \tau_1}{(t_0, t_1) : \tau_0 * \tau_1} \quad \frac{t : \tau_0 * \tau_1}{\mathbf{fst}(t) : \tau_0} \quad \frac{t : \tau_0 * \tau_1}{\mathbf{snd}(t) : \tau_1}$$

$$\frac{x : \tau_0 \quad t : \tau_1}{\lambda x. \ t : \tau_0 \rightarrow \tau_1} \quad \frac{t_1 : \tau_0 \rightarrow \tau_1 \quad t_0 : \tau_0}{t_1 \ t_0 : \tau_1}$$

$$\frac{x : \tau \quad t : \tau}{\mathbf{rec} \ x. \ t : \tau}$$

# Semantica Op. Lazy

$$\frac{t_0 : \tau_0 \quad t_1 : \tau_1 \quad t_0, t_1 \text{ closed}}{(t_0, t_1) \rightarrow (t_0, t_1)} \quad \frac{\lambda x. t : \tau_0 \rightarrow \tau_1 \quad \lambda x. t \text{ closed}}{\lambda x. t \rightarrow \lambda x. t}$$

$$\frac{t_0 \rightarrow n_0 \quad t_1 \rightarrow n_1}{t_0 \text{ op } t_1 \rightarrow n_0 \text{ op } n_1} \quad \frac{t \rightarrow 0 \quad t_0 \rightarrow c_0}{\text{if } t \text{ then } t_0 \text{ else } t_1 \rightarrow c_0} \quad \frac{t \rightarrow (t_0, t_1) \quad t_0 \rightarrow c_0}{\text{fst}(t) \rightarrow c_0}$$

$$\frac{t \left[ \text{rec } x. t / x \right] \rightarrow c}{\text{rec } x. t \rightarrow c} \quad \frac{t \rightarrow n \quad n \neq 0 \quad t_1 \rightarrow c_1}{\text{if } t \text{ then } t_0 \text{ else } t_1 \rightarrow c_1} \quad \frac{t \rightarrow (t_0, t_1) \quad t_1 \rightarrow c_1}{\text{snd}(t) \rightarrow c_1}$$

$$\frac{t_1 \rightarrow \lambda x. t'_1 \quad t'_1[t^0 / x] \rightarrow c}{(t_1 \ t_0) \rightarrow c} \quad (\text{lazy})$$