Introduction

Chapter 1 Prologo Lecture Notes prof. Paolo Ferragina

Algorithm Engineering

• Teachers

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Preliminaries

- In order to be able to understand these lectures it is necessary to know basics in algorithms and computational complexity.
- Know how to evaluate algorithms in the RAM model.
- Know how to write a program.

Otherwise study the book:

Cormen Leiserson Rivest Stein,: Introduction to Algorithms. Worldwide famous book used in the most prestigious universities.

Lecture Notes

- Almost all topics considered are contained into the Lecture Notes.
- Otherwise references will be given.
- Treated topics can be sometimes hard hence you will need a personal effort to understand them. Following the lectures is not enough.
- We will use a pseudo-code (similar to java or C) to define algorithms to be able to discard details but... you are entitled to know them!!!

Interesting problems

- We will not use a formal approach.
- We will analyze solutions for some interesting problems arising from real/useful applications.
- We will study solution of improved efficiency and increasing sophistication.
- Before: Model of Von Neumann RAM model
- Last 10 years: 2 main changes.
 - The architecture of modern PC are more and more complex
 - Explosion of input size

The RAM model is more and more unsatisfactory!

Algorithm Engineering

- Derive efficient algorithms for the new models.
- Adapt old efficient algorithms to the new models
- Exploit techniques coming from other memory models such as parallel computation.
- Derive general techniques to be adopted in different situations.

Example: Compute the sum of the integers stored in the Array A[1, n] working in a modern PC.

A modern PC



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PAST: Main memory VS External memory

NOW: Memory hierarchy



The access mechanisms are the same



Two adjacent levels are considered. Data are transferred in blocks of fixed size, called PAGES

Locality principle

- The block transfer is an expensive operation.
- Apply the locality principles to organize efficient accesses to blocks

Temporal locality: It is probable that an already requested object will be requested again in the future.

Spatial locality: It is probable that objects close to already referred ones will be requested again in the future.

2-level memory model (disk model)

- B= block (page) size
- M= internal memory size

How to evaluate the complexity of an algorithm?

number of I/Os operations

- Our algorithm takes n/B I/Os operations is optimal.
- It is independent from the block size. Very important feature for an algorithm. Cache-oblivious.

Modern PC architecture

- Nanoseconds suffice to access the caches
- Milliseconds to access data from disks.
- I/O bottelneck
- Engineering: try to reduce the impact of I/O bottleneck handling large datasets.
- Good algorithms design surpass the best technology advancements !

- Compute the sum of integers stored in array A[1, n].
- Scan and accumulate in a variable $\rightarrow \Theta(n)$
- Define a family of algorithms $A_{s,b}$ the patterns to access the items are different according to s and b.
- A is divided into blocks $A_j 0 \le j \le n/b-1$ of size b (b items)

• $A_j = A[j*b+1, (j+1)*b] , 0 \le j \le n/b$



- Sum all items of a block before moving to next block s that is s blocks apart to the right.
- A is considered cyclic.

- b block size; s number of blocks of the jump.
- s must be co-prime with n/b in order all blocks are considered.
- Otherwise: n/b=9, s=3 the same 3 blocks are examined cyclically.
- If s is co-prime with n/b: [s×i mod n/b] generates a permutation of [0, 1, ..., n/b-1] hence all blocks in A are touched.
- Varying s and b we can sum according to different patterns of memory accesses.

- Sequential scan s=1, b=1.
- Block-wise scan b=B.
- And/or random-wise access large values of s.
- All algorithms in $A_{s,b}$ are equivalent: they read and sum exactly n integers.
- Complexity:
- s=1: $A_{1,b}$ scan A rightwards and independently from the b value takes O(n/B) I/O's
- As s and b changes situation complicates!

- s=2, b<B, b divides B. Every block B consists of B/ b smaller, logical blocks of size b.
- A_{2,b} examines only half of them because s=2.
 Page is half utilized! 2n/B I/O's.
- For any s : sn/B I/O's.

The formula is an approximation to the real case: all I/ O's are considered equal while in reality the cost changes from sequential and random I/O's. But the sufficiently good and widely adopted in literature. The 2-level memory model will be adopted almost in all cases.

Algorithm Engineering

How to turn theoretically efficient algorithms into practically efficient code!