

Business Processes Modelling

MPB (6 cfu, 295AA)

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22 - Diagnosis for WF nets



Object



We study suitable diagnosis techniques
for unsound Workflow nets

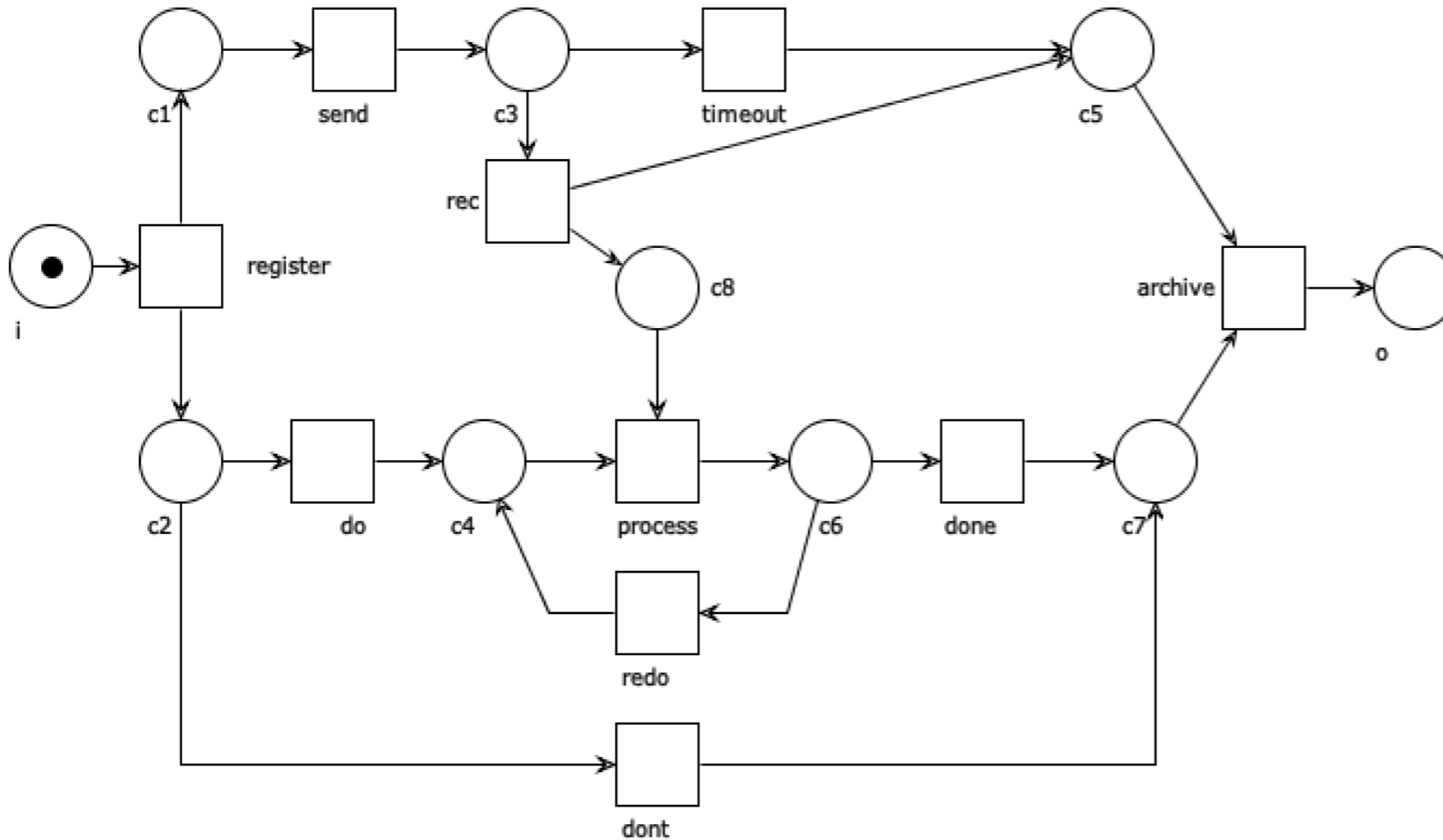
Diagnosing workflow processes using Woflan (article, optional reading)

<http://wwwis.win.tue.nl/~wvdaalst/publications/p135.pdf>

S-Coverability

Woped

what are S-components?
and why are they relevant?



Semantical analysis

Wizard Expert

- Qualitative analysis
 - Structural analysis
 - Net statistics
 - Places: 10
 - Transitions: 10
 - Operators: 0
 - Subprocesses: 0
 - Arcs: 24
 - Wrongly used operators: 0
 - Free-choice violations: 0
 - S-Components**
 - S-Components: 2
 - Places not covered by S-Component: 1
 - c8
 - Wellstructuredness
 - PT-Handles: 4
 - TP-Handles: 5
 - Soundness
 - Workflow net property
 - Initial marking
 - Boundedness
 - Liveness

Rank Theorem

(main result, proof omitted)

Theorem:

A free-choice system (P, T, F, M_0) is live and bounded
iff

1. it has at least one place and one transition
2. it is connected
3. M_0 marks every proper siphon
- 4. it has a positive S-invariant**
5. it has a positive T-invariant
6. $\text{rank}(N) = |C_N| - 1$

(where C_N is the set of clusters)

A technique to find a positive S -invariant

A case is often composed by parallel threads of control
(each thread imposing some order over its tasks)

Decompose the net N in suitable S -nets
so that any place of N belongs to some S -net
(the same place can appear in more S -nets)

Each S -net induces a uniform S -invariant

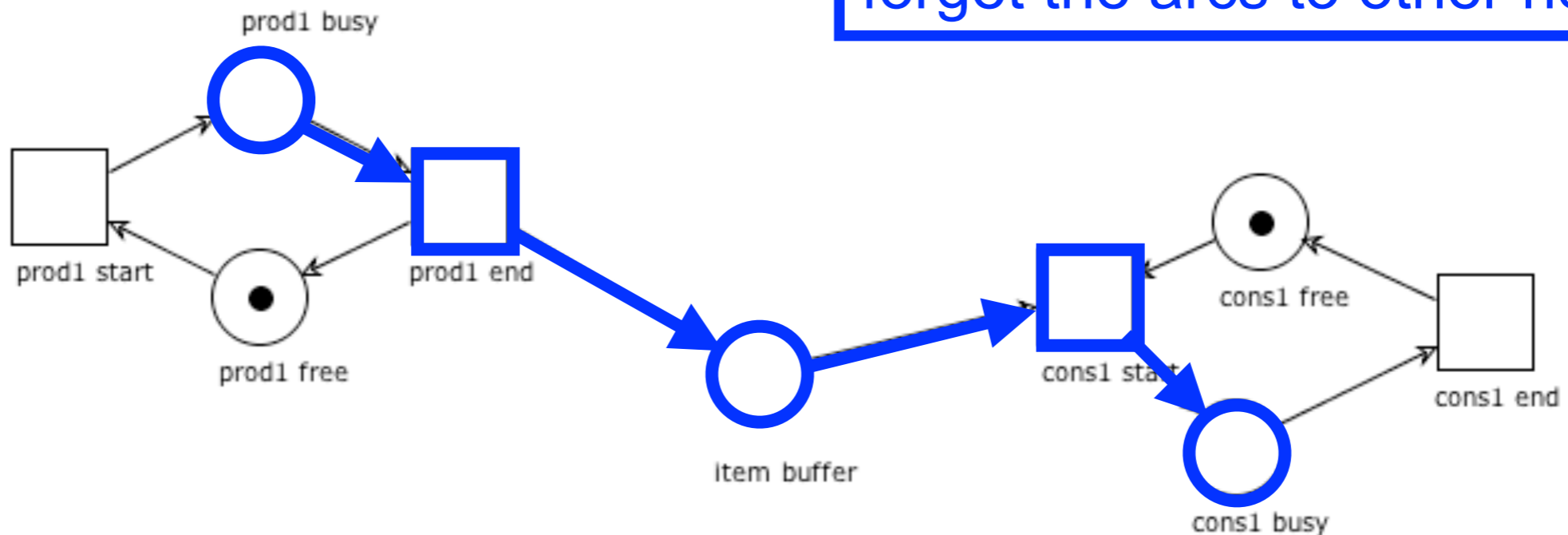
A positive S -invariant is obtained
as the sum of the S -invariants of each subnet

Subnet

take a set of nodes

Definition: Let $N = (P, T, F)$ and $\emptyset \subset X \subseteq P \cup T$
Let $N' = (P \cap X, T \cap X, F \cap (X \times X))$ be a subnet of N .

forget the arcs to other nodes



S-component

take a set of nodes

Definition: Let $N = (P, T, F)$ and $\emptyset \subset X \subseteq P \cup T$

Let $N' = (P \cap X, T \cap X, F \cap (X \times X))$ be a subnet of N .

N' is an **S-component** if

forget the arcs to other nodes

1. it is a strongly connected S-net

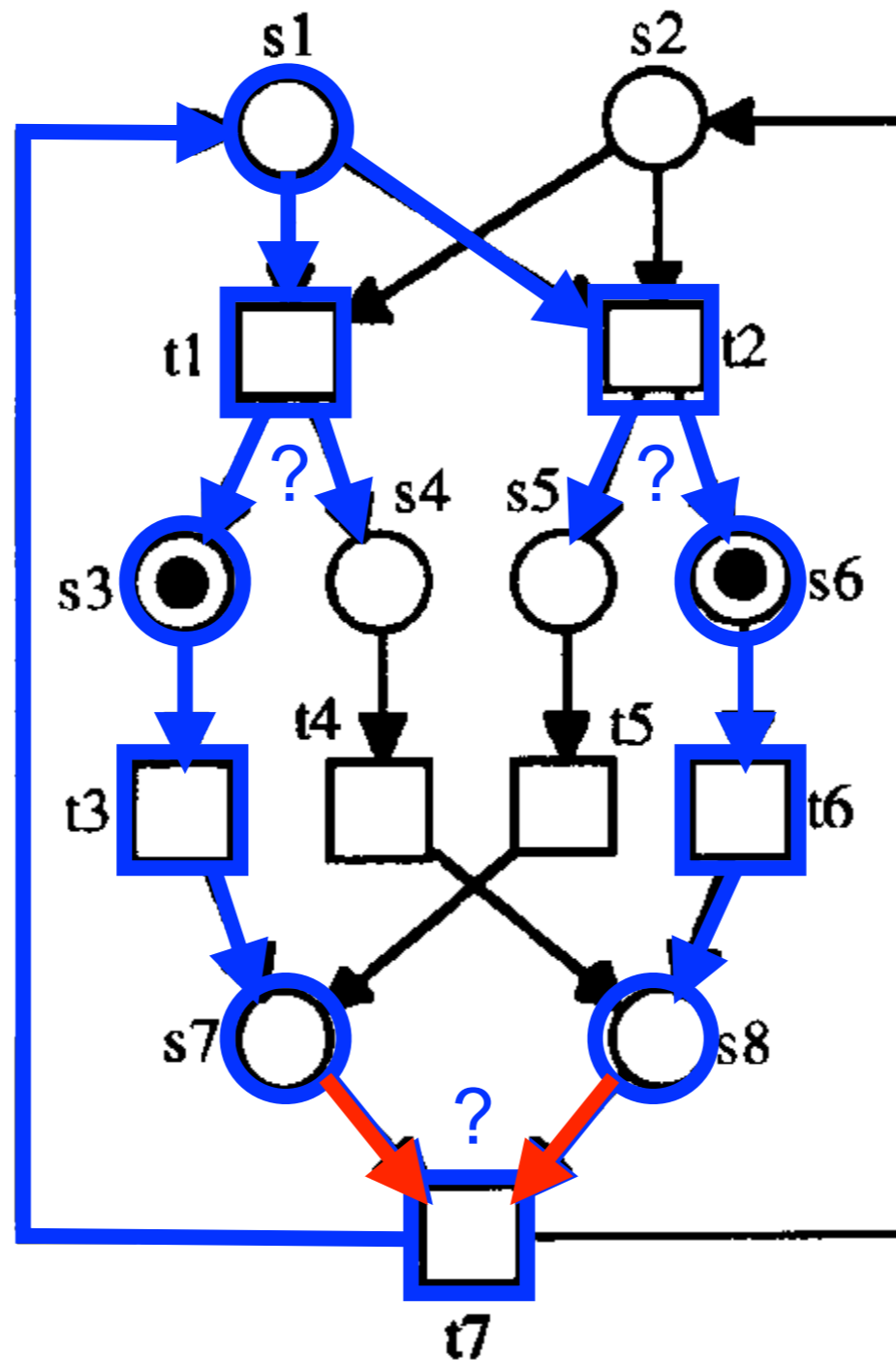
2. for every place $p \in X \cap P$, we have $\bullet p \cup p \bullet \subseteq X$

if a place p is taken

then all transitions attached to p must be selected

if a place p is taken
then all transitions attached to p must be selected

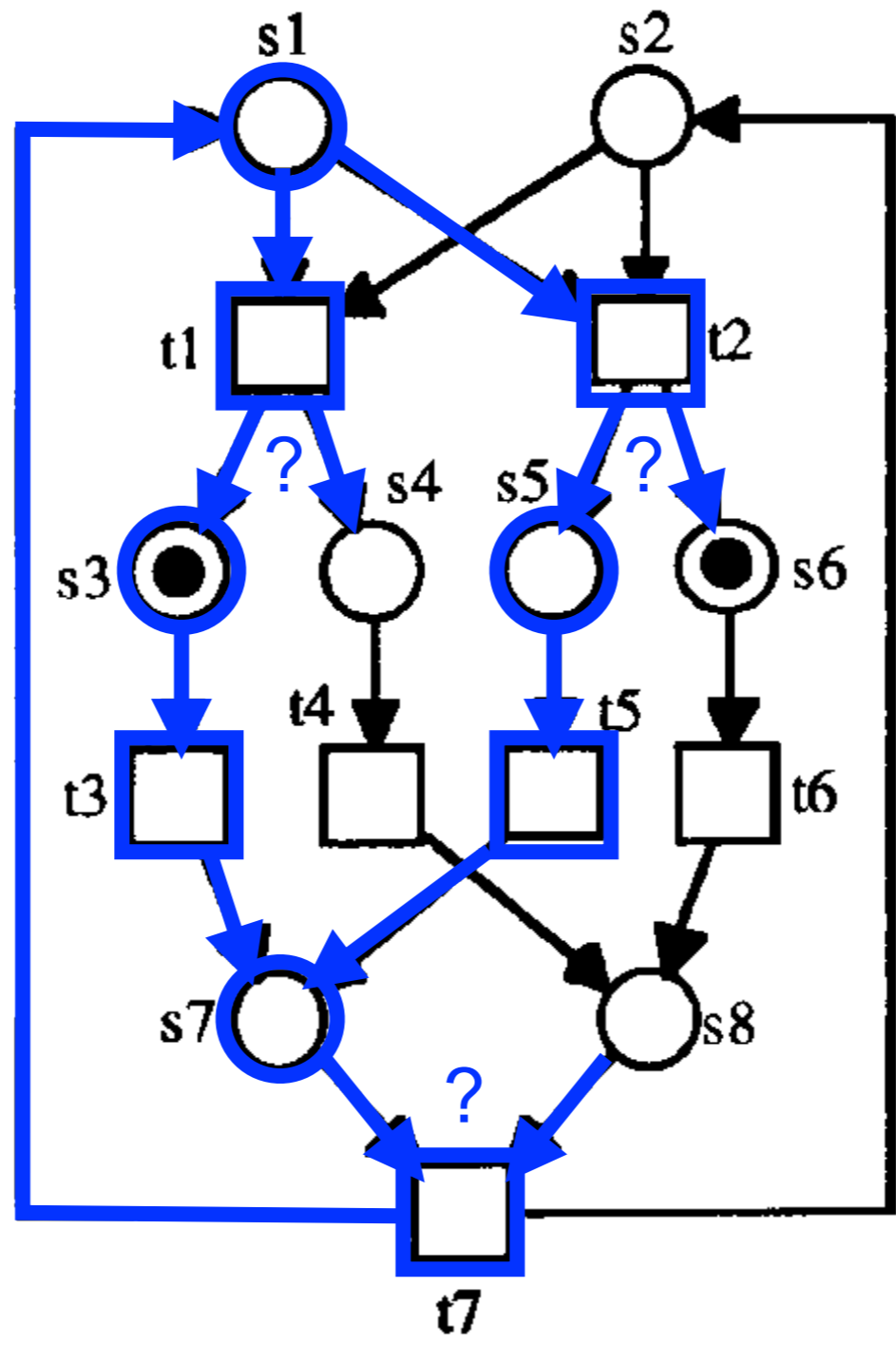
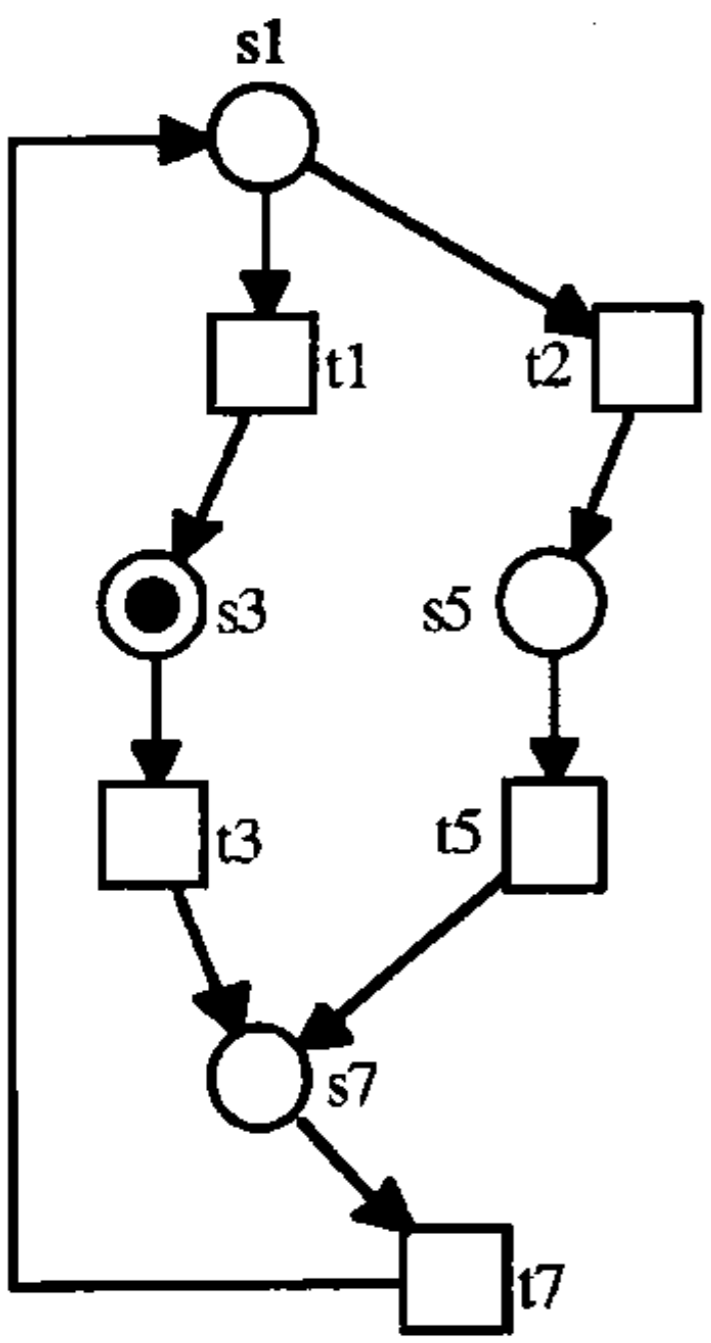
S-component: example



not an S-net

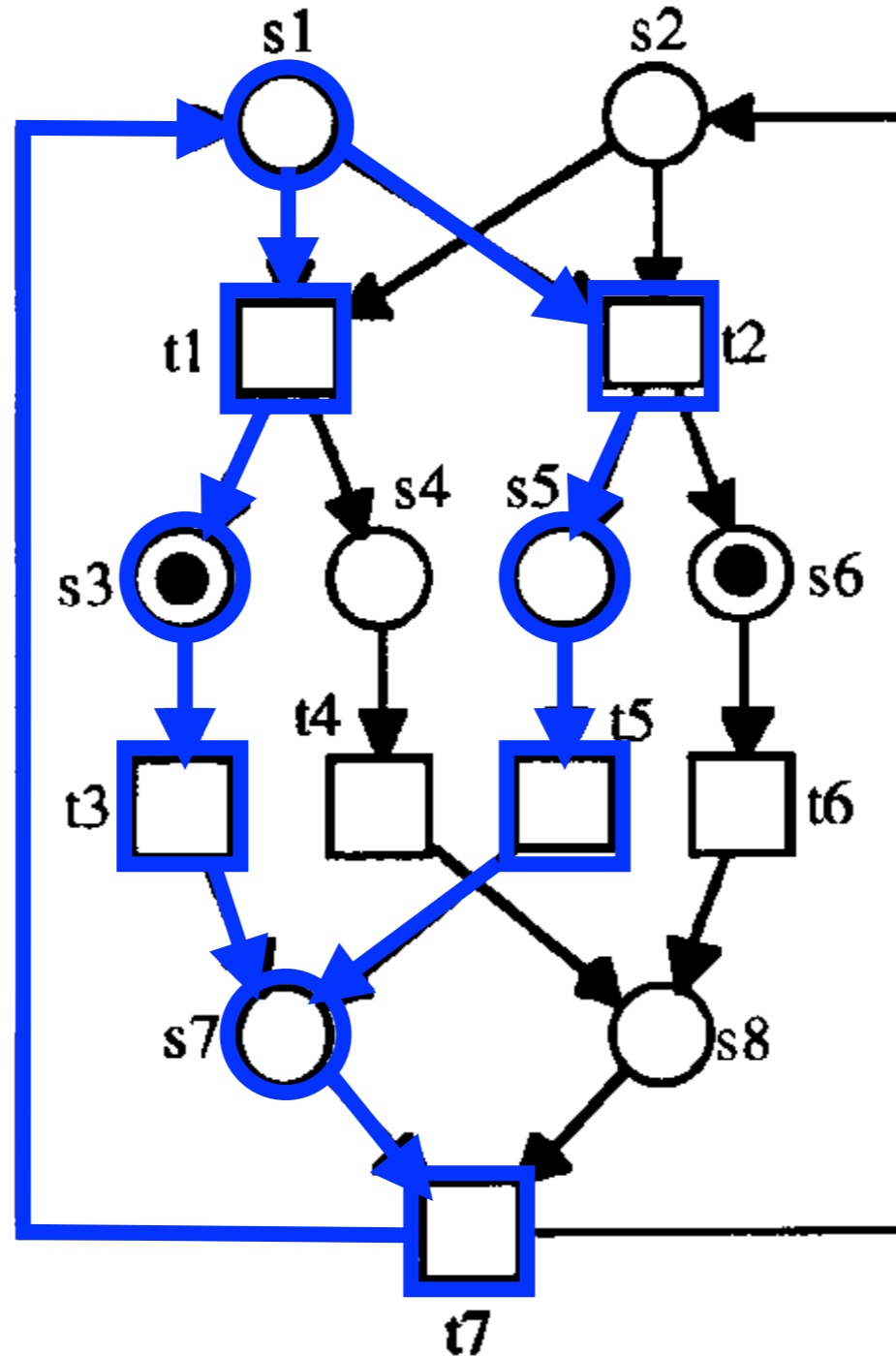
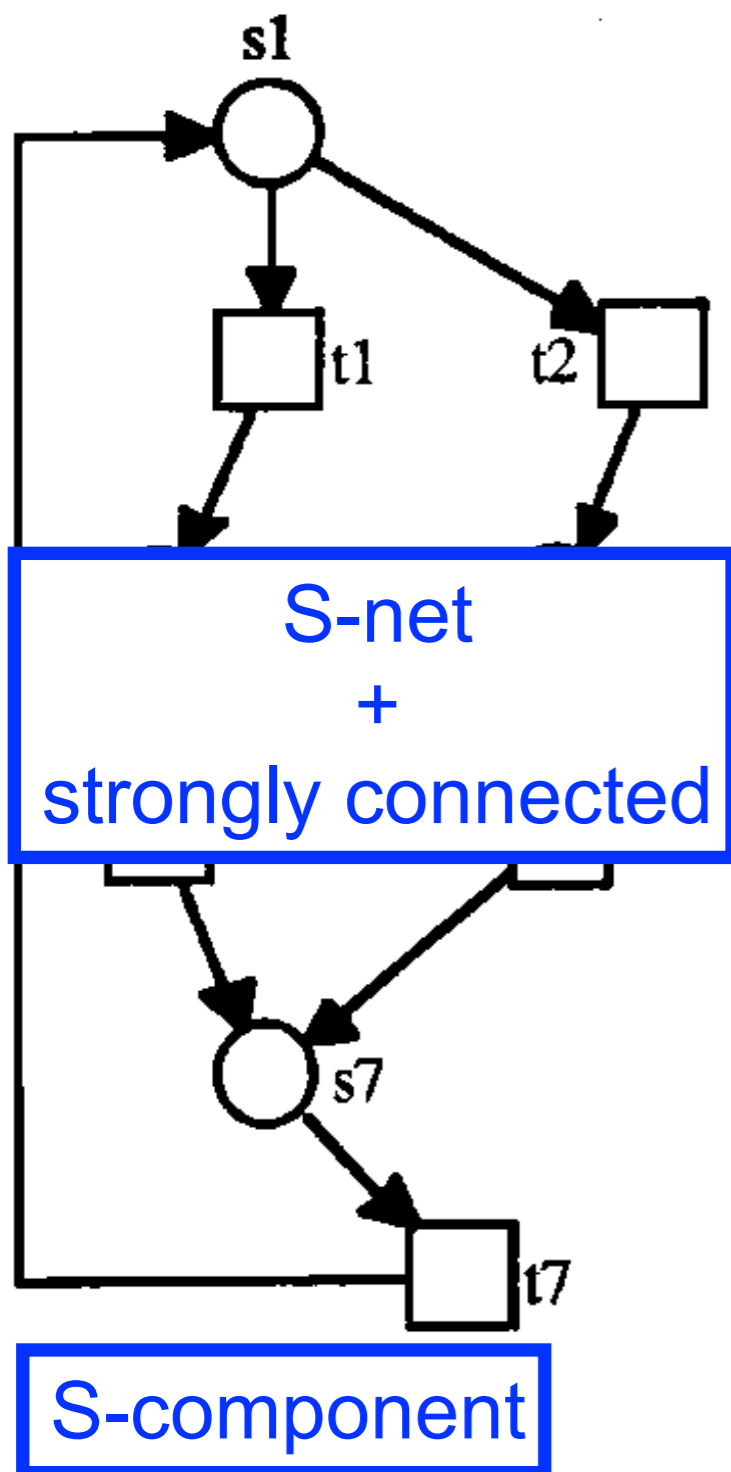
if a place p is taken
then all transitions attached to p must be selected

S-component: example



if a place p is taken
then all transitions attached to p must be selected

S-component: example



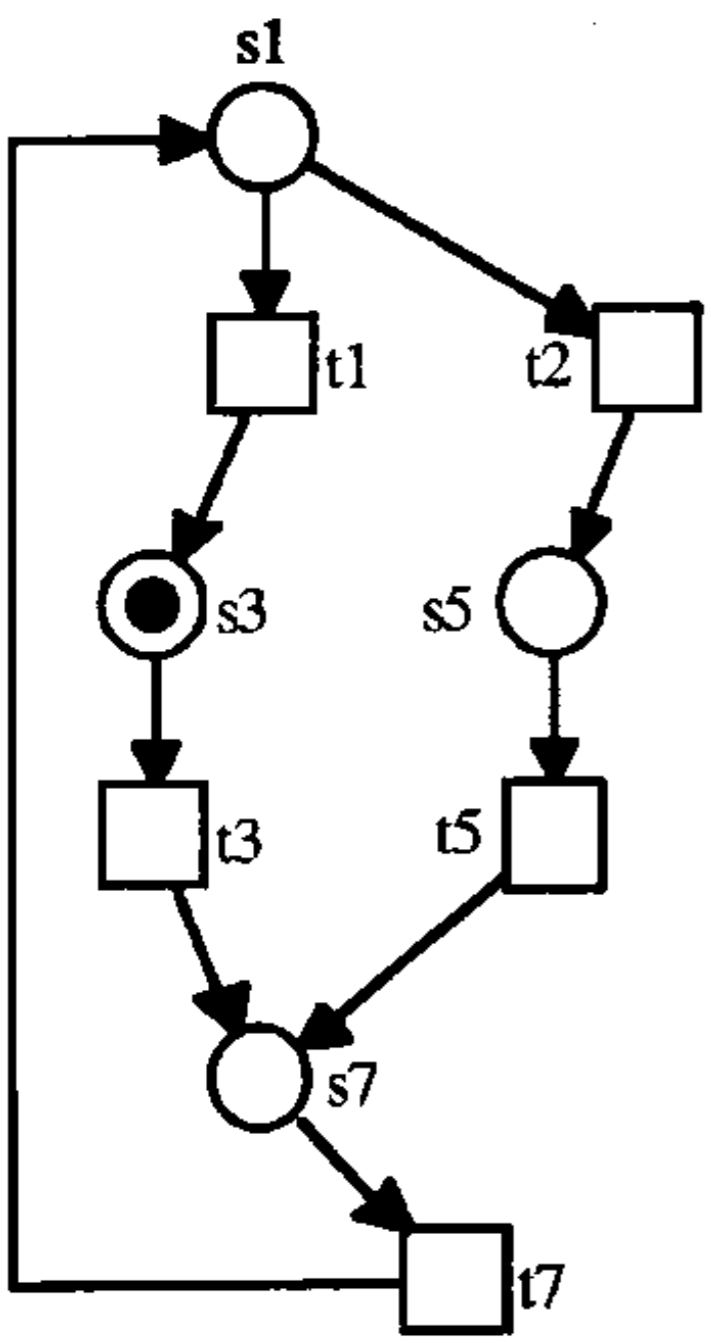
S-cover

Definition: an **S-cover** of a net N is a set C of S-components of N such that every place p of N belongs to one or more S-components in C

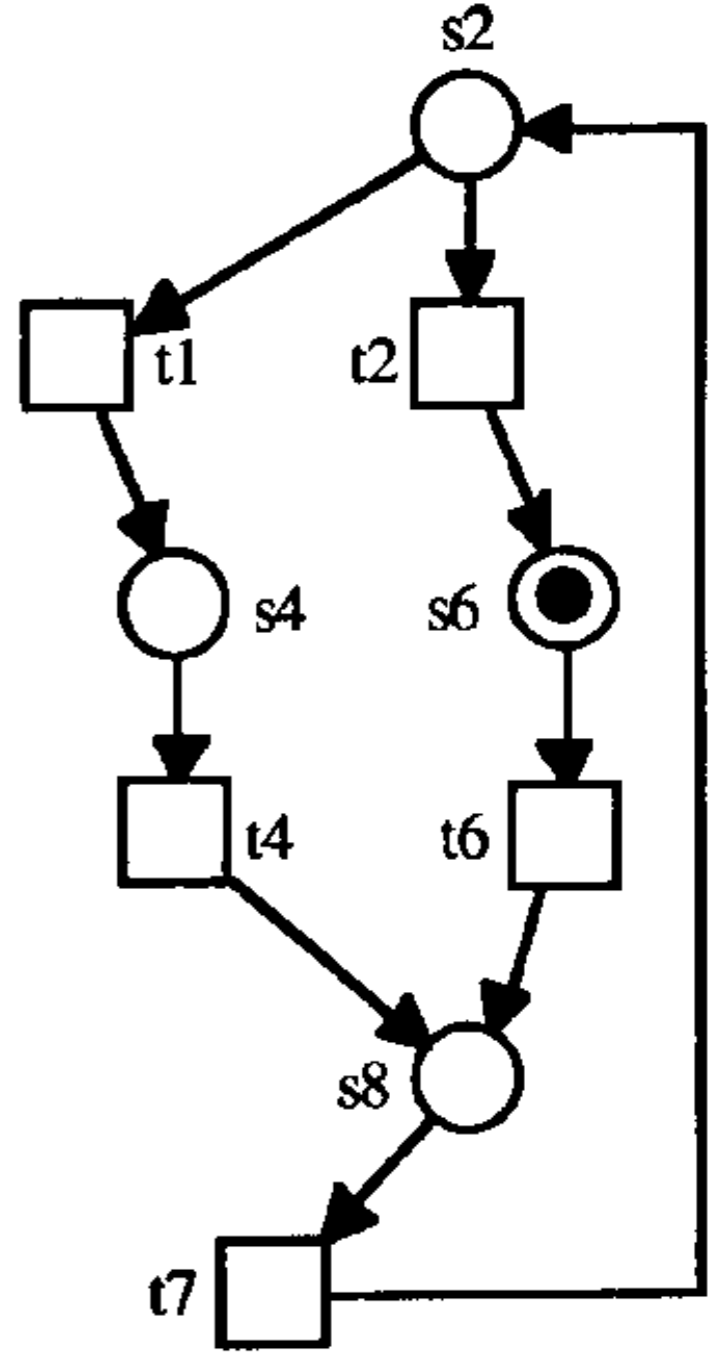
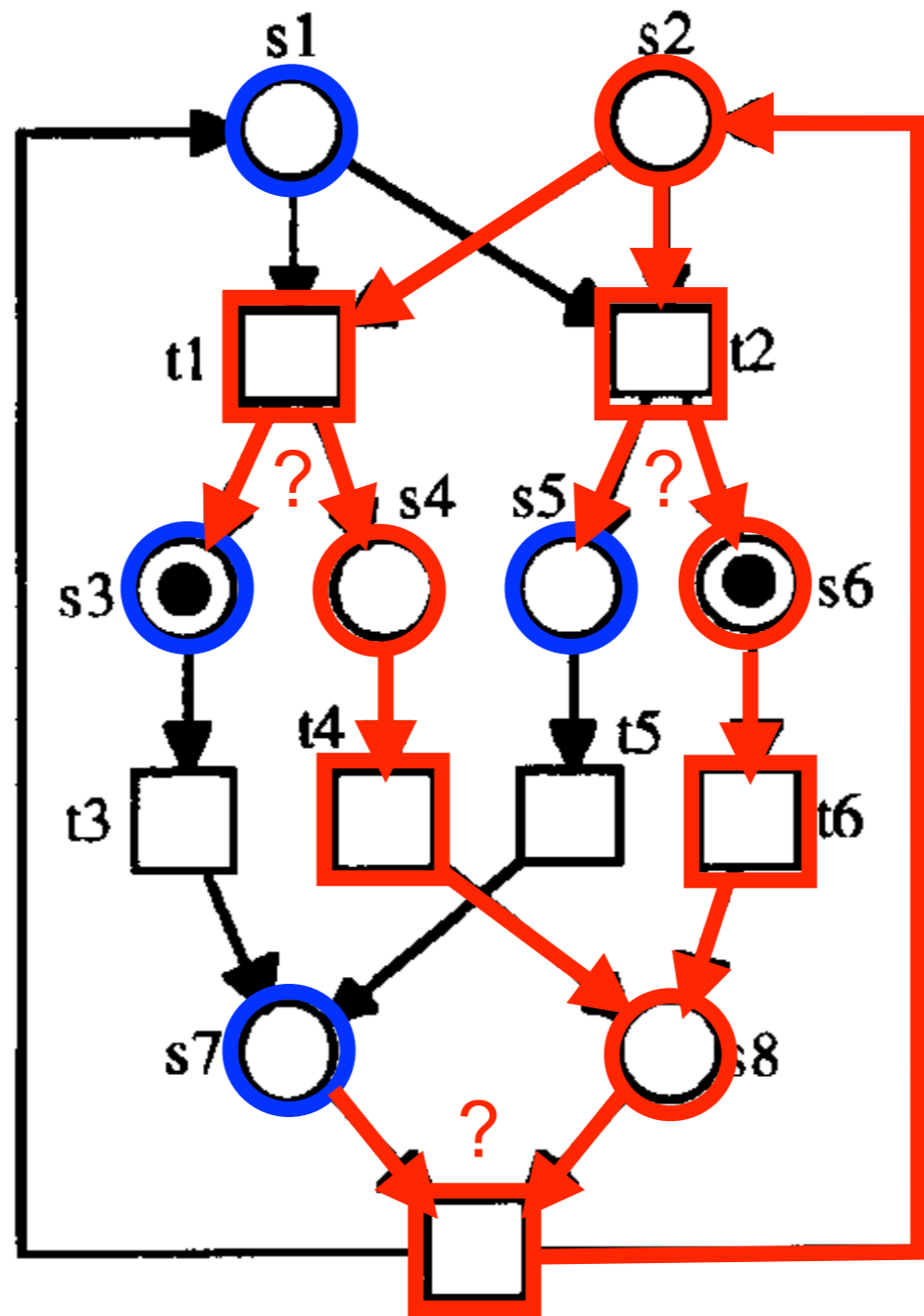
N is **S-coverable** if it has an S-cover

if a place p is taken
 then all transitions attached to p must be selected

S-cover: example

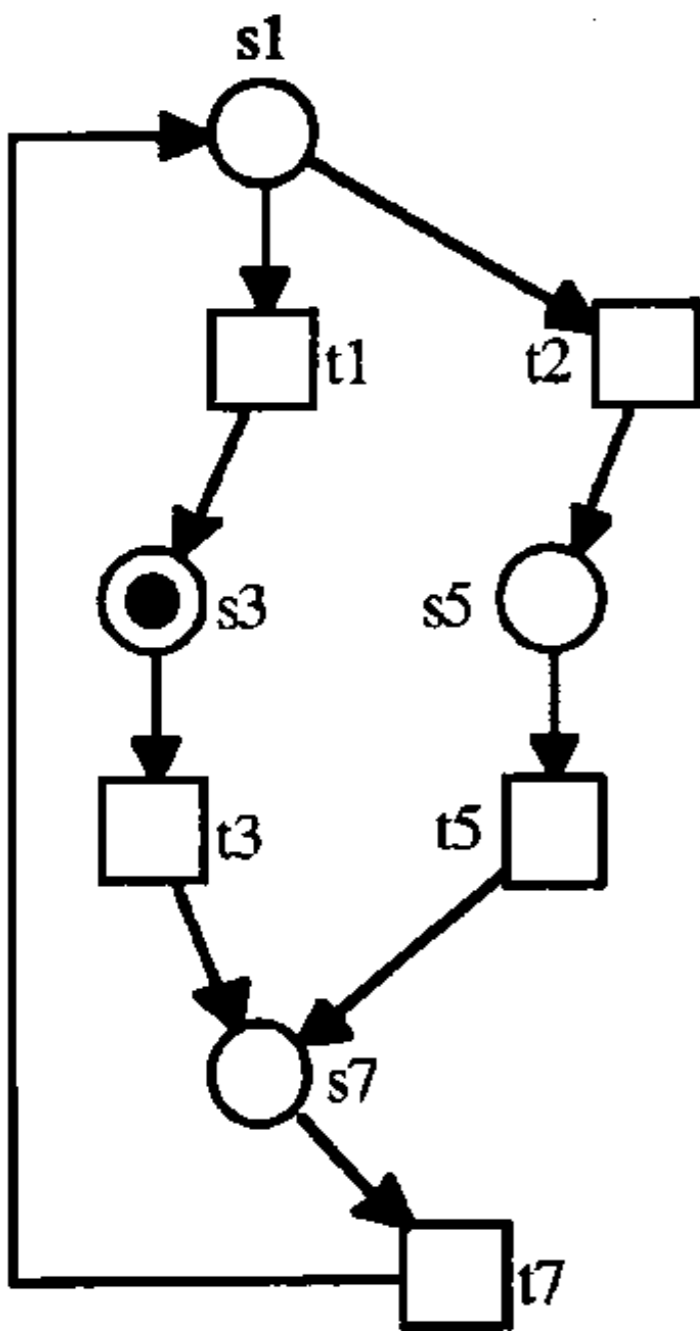


S-component

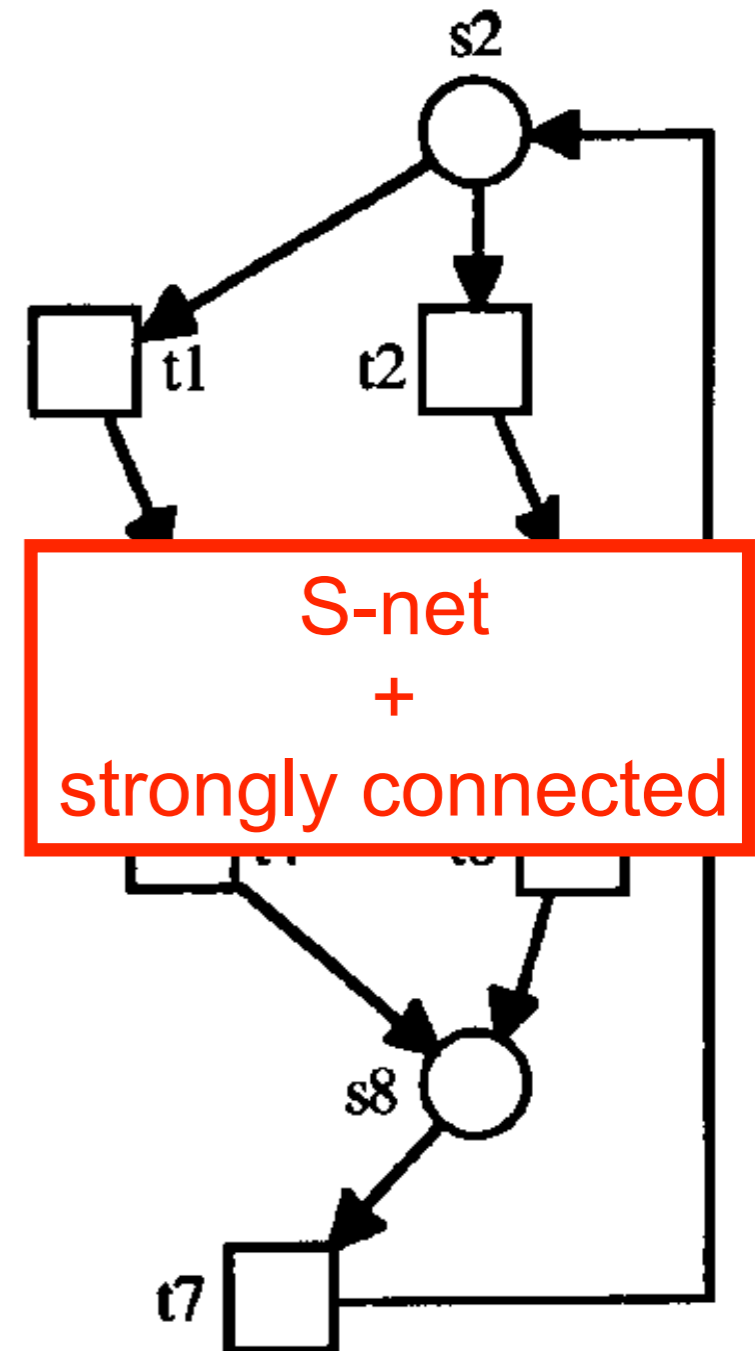
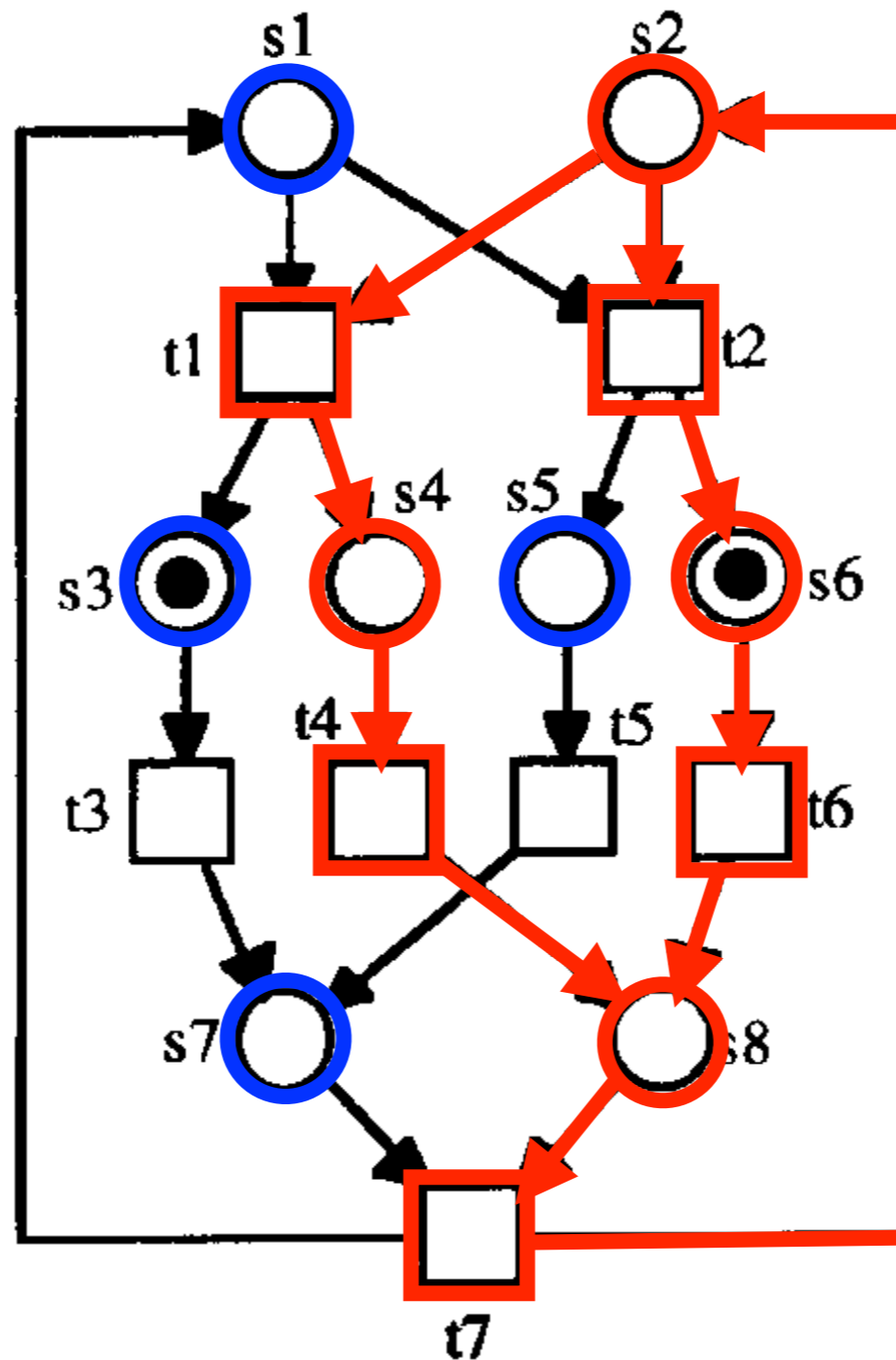


if a place p is taken
then all transitions attached to p must be selected

S-cover: example



S-component

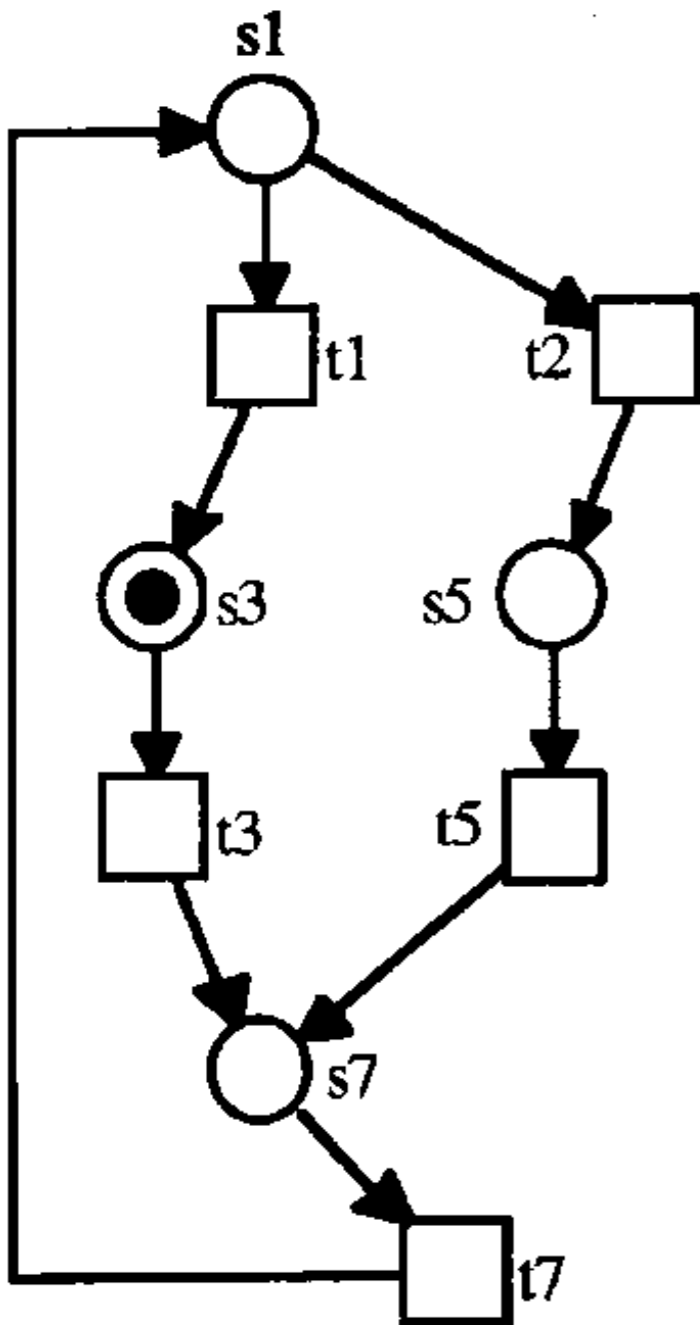


S-net
+
strongly connected

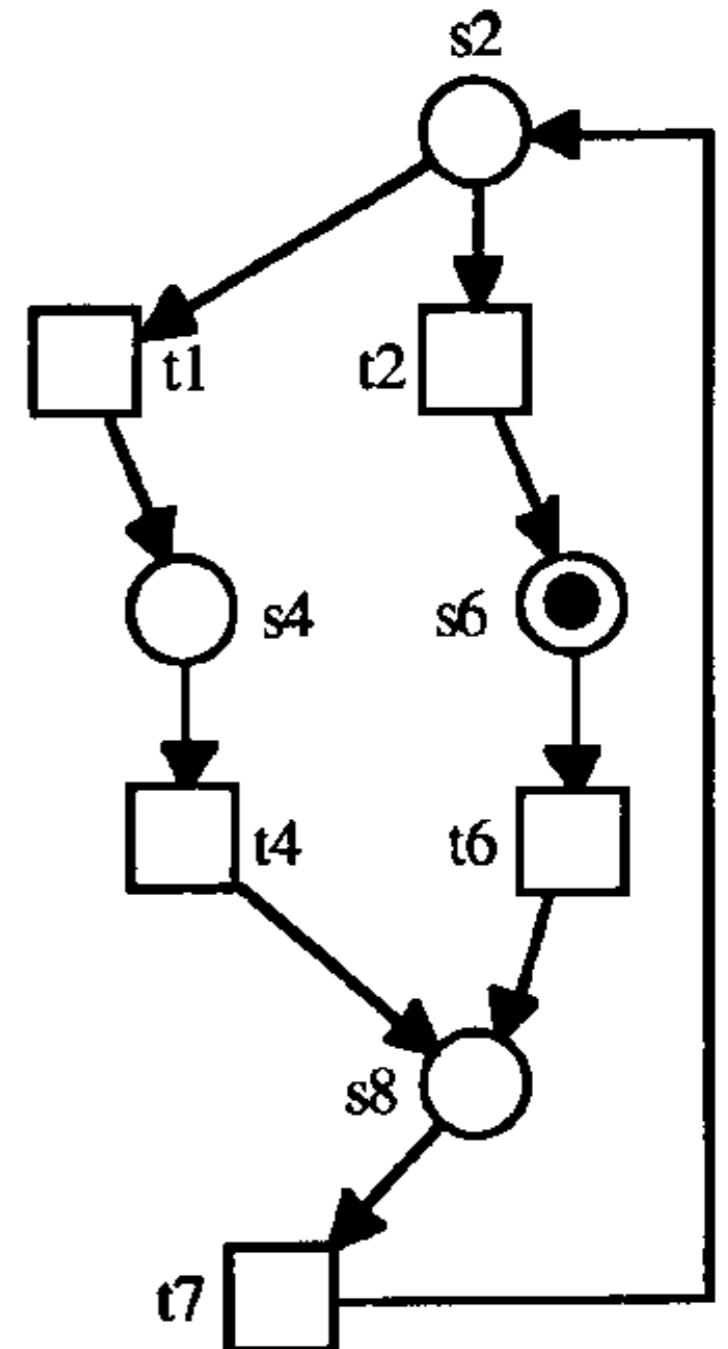
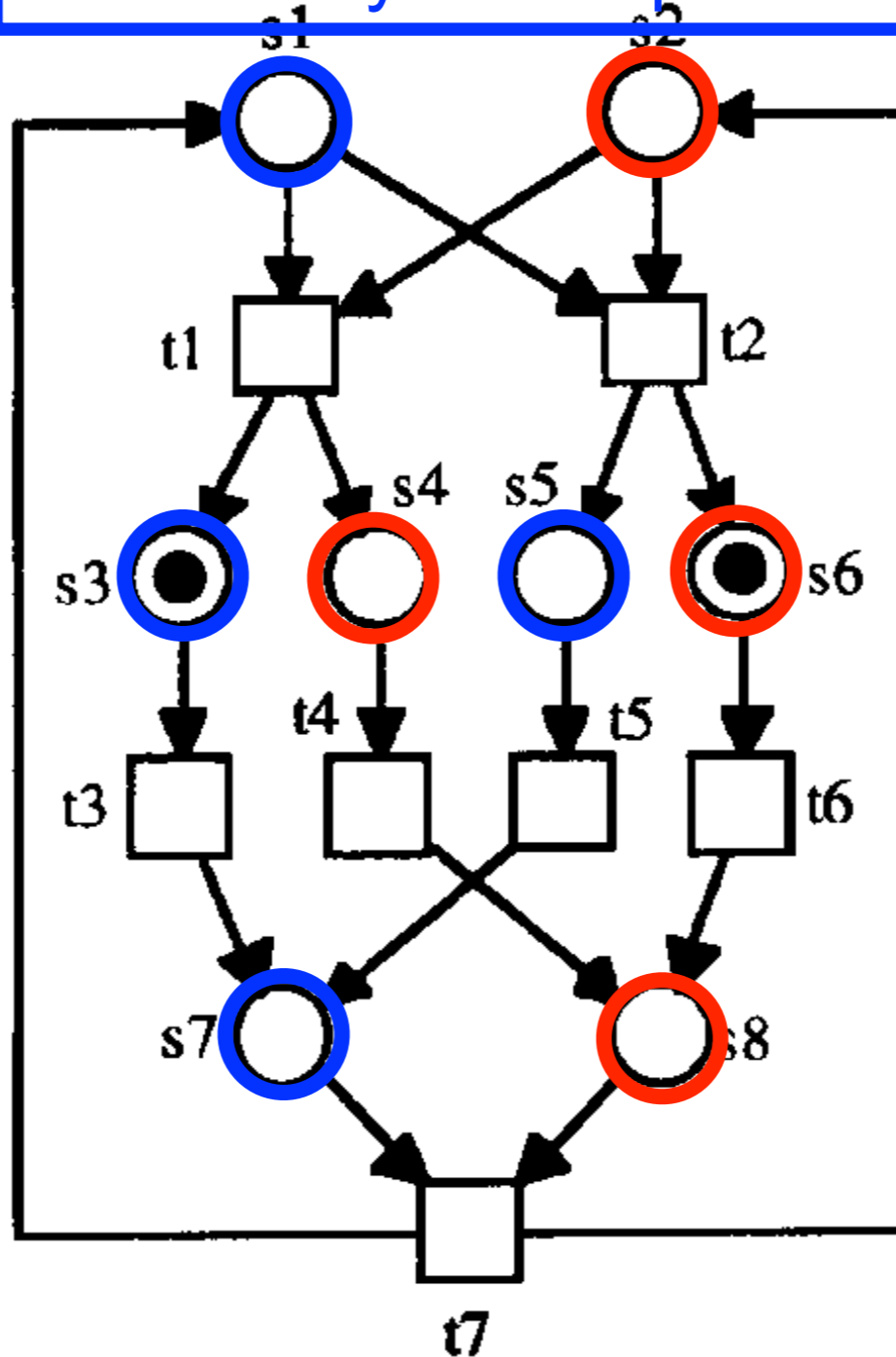
S-component

S-cover: example

covered by S-components



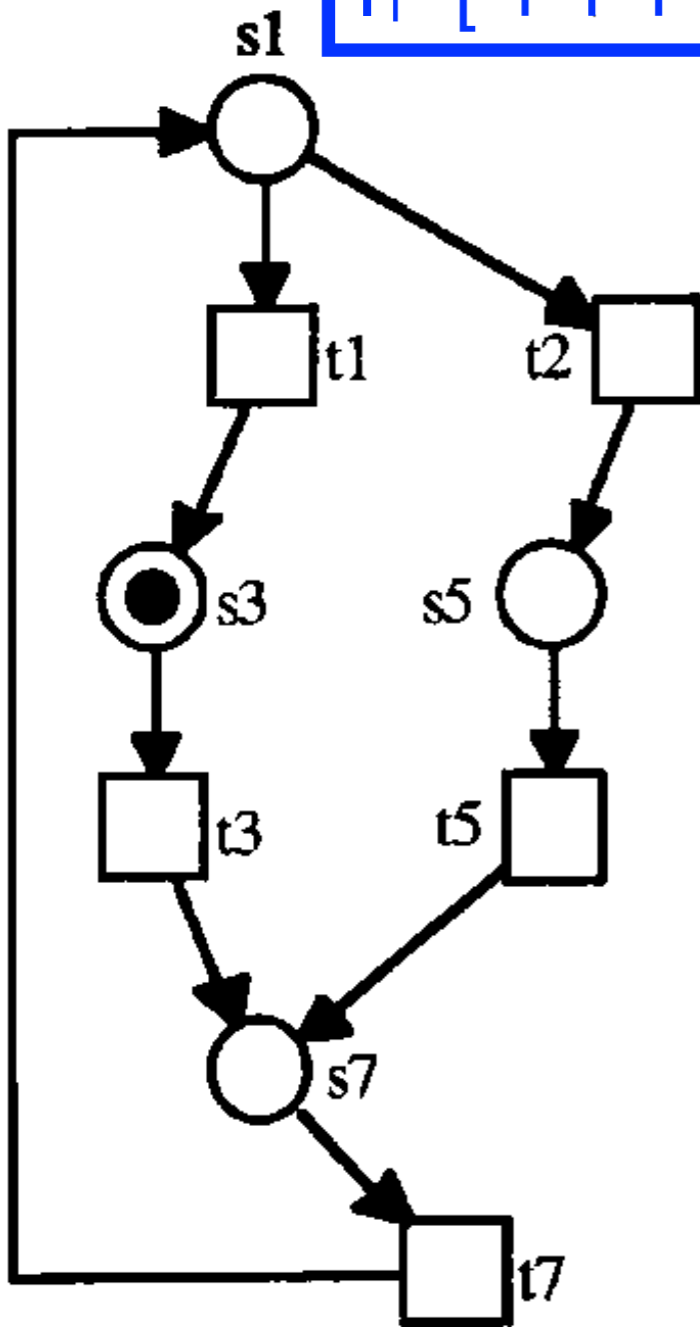
S-component



S-component

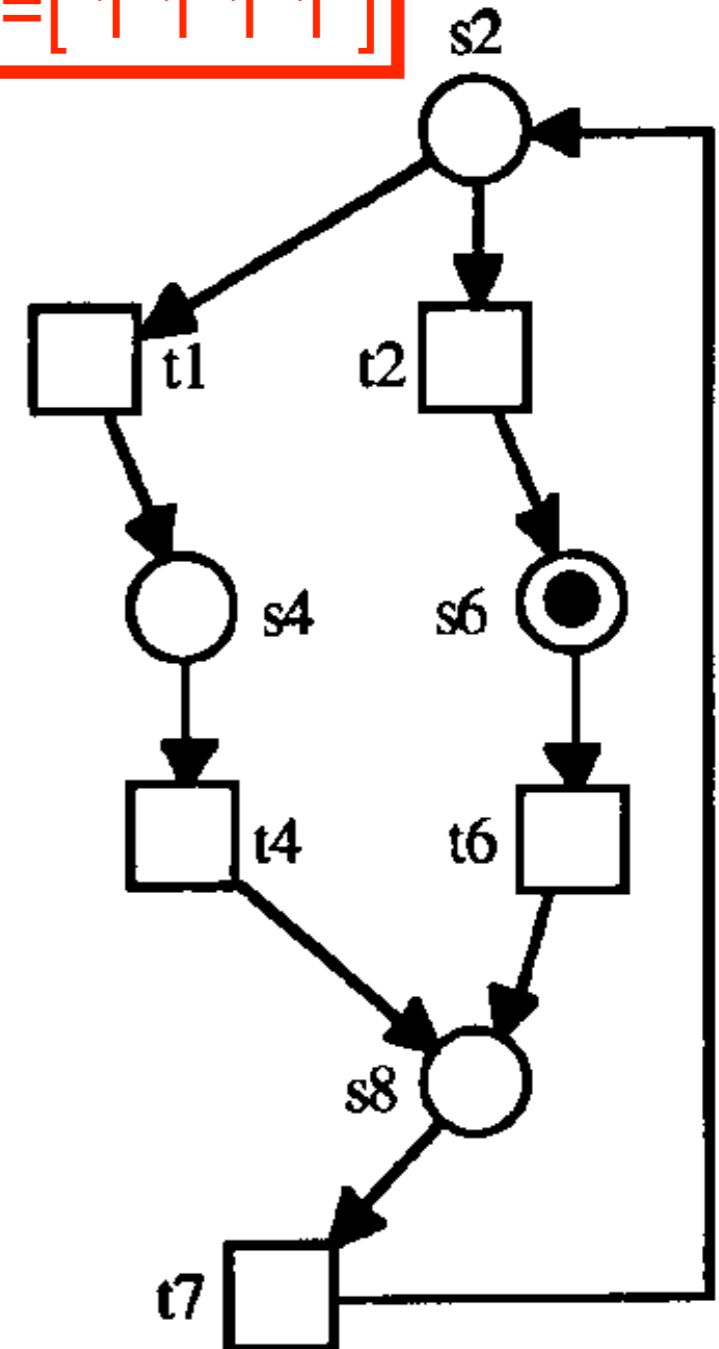
S-cover: example

$$l_1 = [1 \ 1 \ 1 \ 1]$$



S-component

$$l_2 = [1 \ 1 \ 1 \ 1]$$



S-component

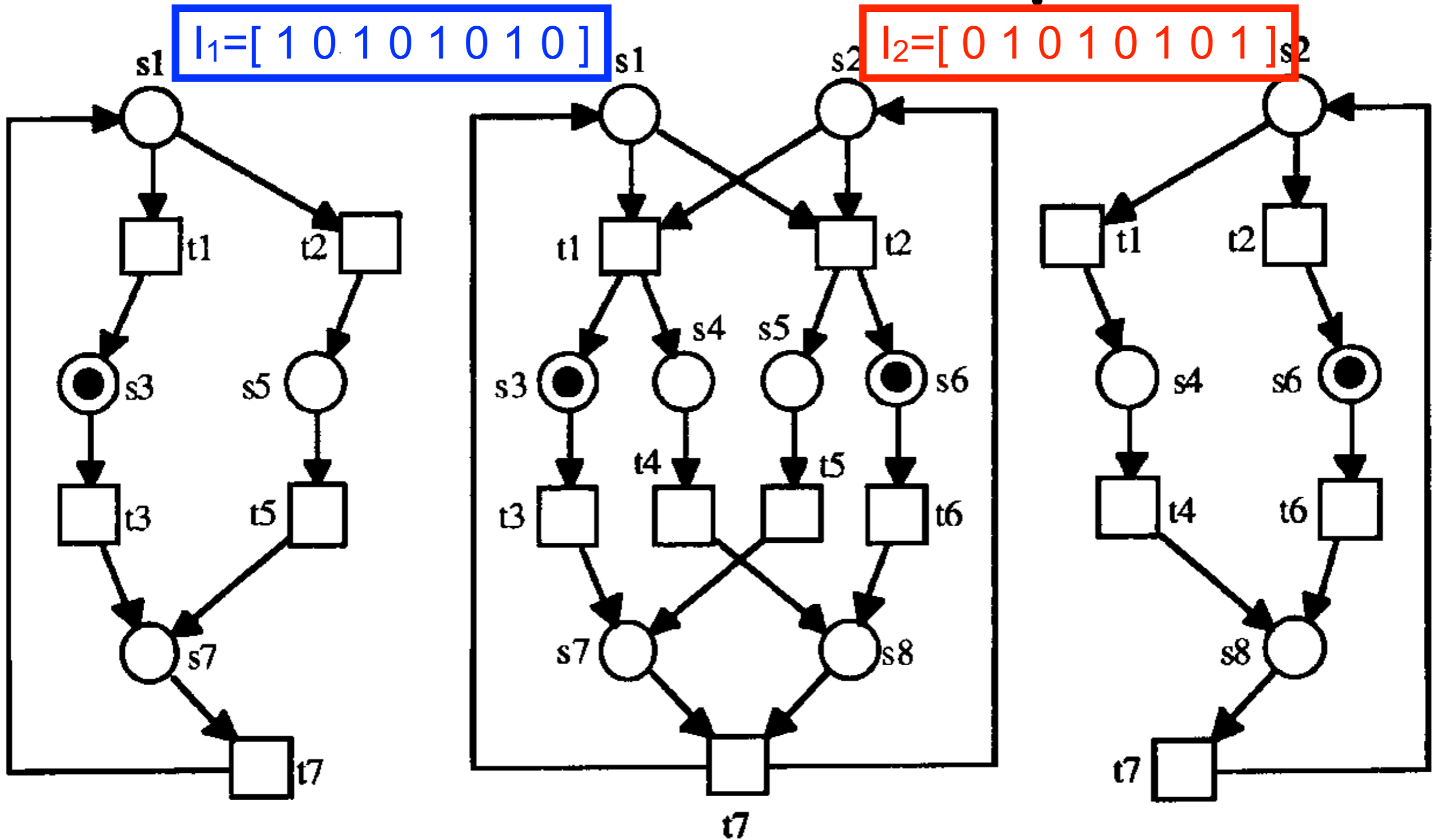
S-cover

S-invariants

Any S-invariant of an S-component induces an S-invariant for the whole net

(it is enough to assign weight 0 to all places not covered by the S-component)

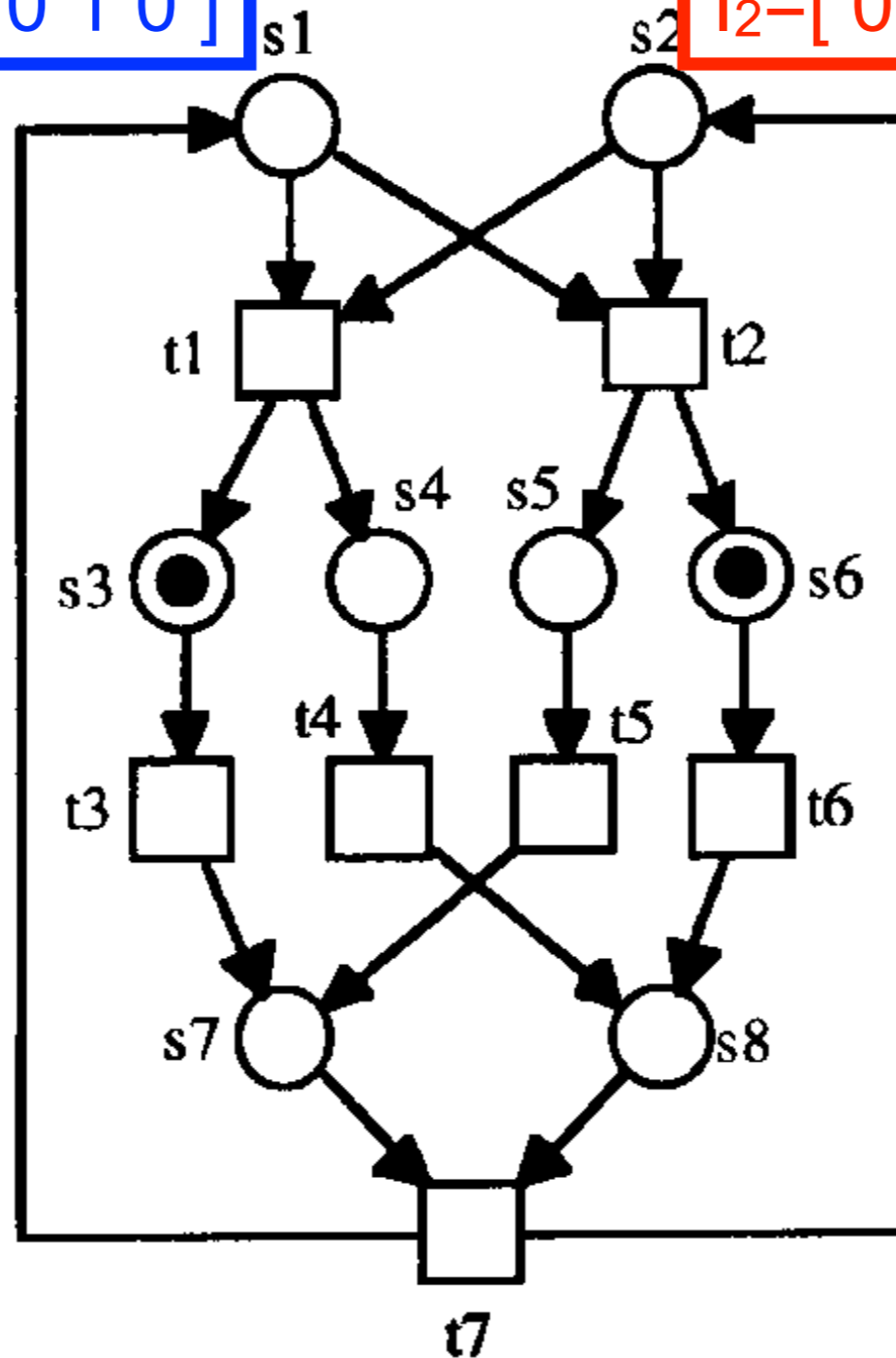
S-cover: example



S-cover: example

$$l_1 = [1\ 0\ 1\ 0\ 1\ 0\ 1\ 0]$$

$$l_2 = [0\ 1\ 0\ 1\ 0\ 1\ 0\ 1]$$



$$l_1 + l_2 = [1\ 1\ 1\ 1\ 1\ 1\ 1\ 1]$$

positive S-invariant

S-coverability theorem

Theorem: If a free-choice system is live and bounded then it is S-coverable

(proof omitted)

Consequence:

free-choice + not S-coverable \Rightarrow not (live and bounded)

S-Coverability diagnosis

N is sound iff N^* is live and bounded (Main Theorem)

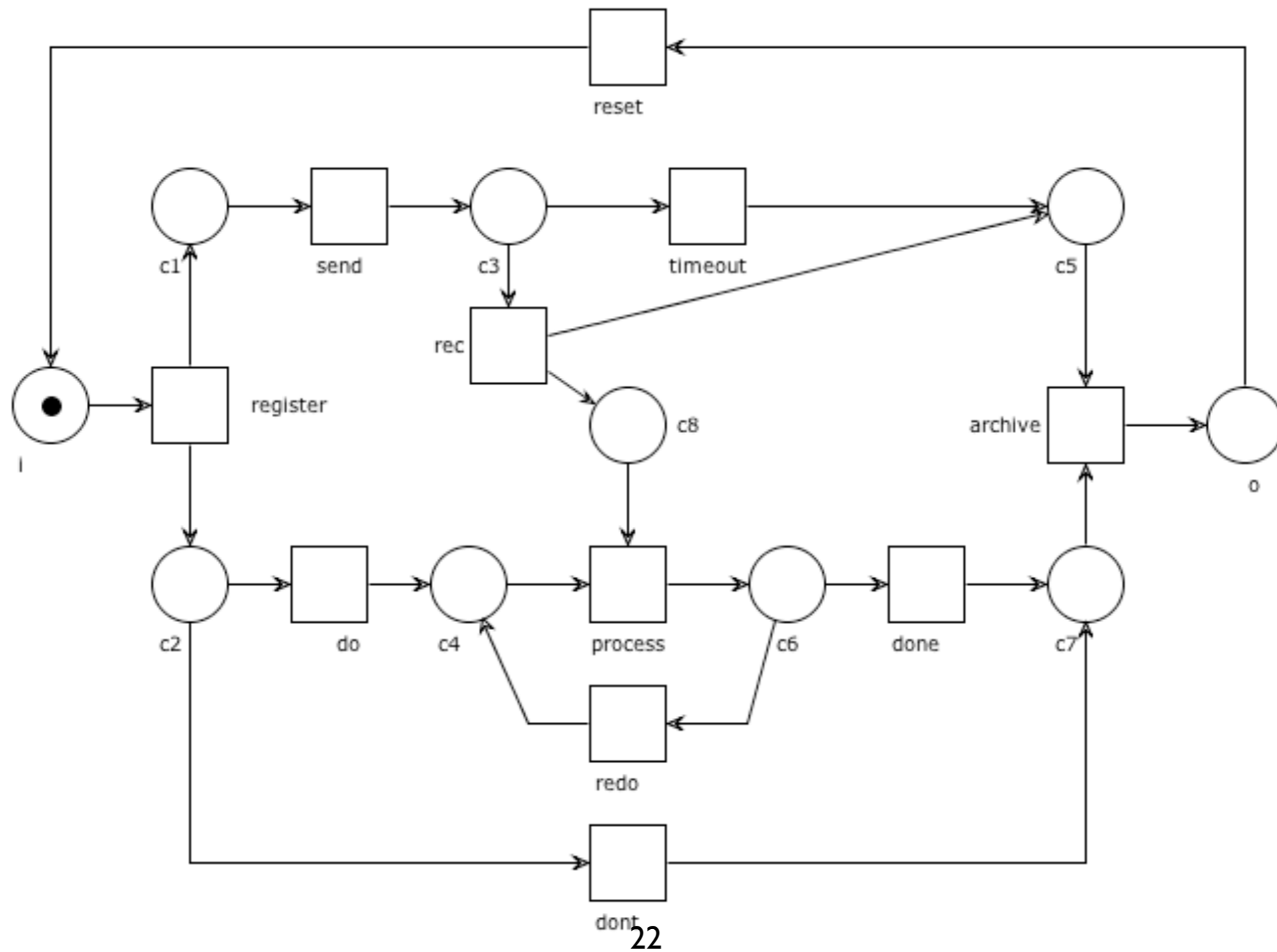
N is free-choice iff N^* is free-choice

If N^* is free-choice, live and bounded
it must be S-coverable (S-coverability theorem)

Corollary: If N is sound and free-choice,
then N^* must be S-coverable

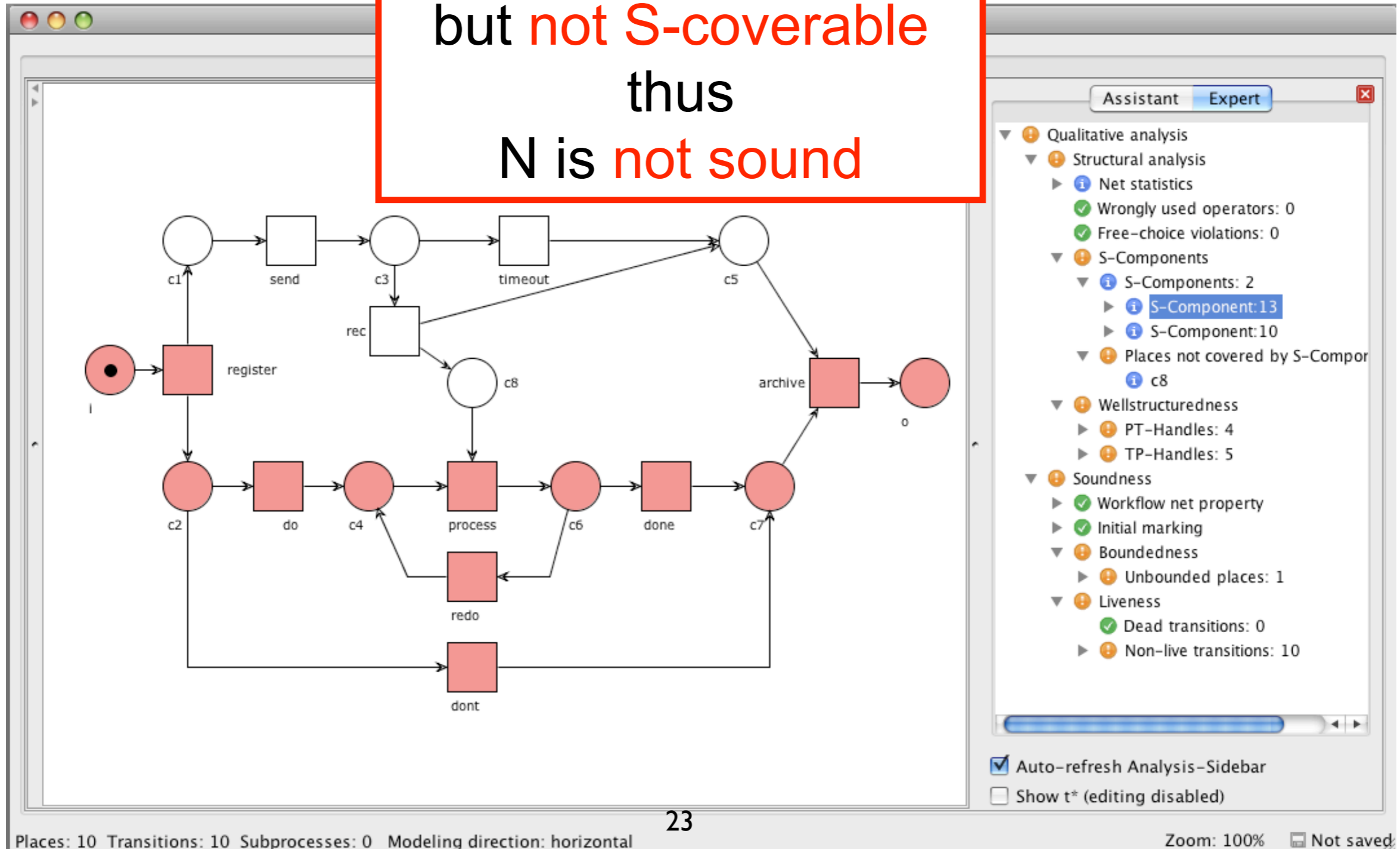
N free-choice + N^* not S-coverable \Rightarrow N not sound

S-cover for N^* ?



WoPeD Diagnosis

N^* is free-choice
but not S-coverable
thus
 N is not sound



Be careful

reset transition is implicit in WoPeD

WoPeD shows S-components for N^*
(not for N)

Compositionality of sound free-choice nets

Lemma:

If a free-choice workflow net N is sound
then it is safe

(because N^* is [S-coverable](#) and $M_0=i$ has just one token)

Proposition:

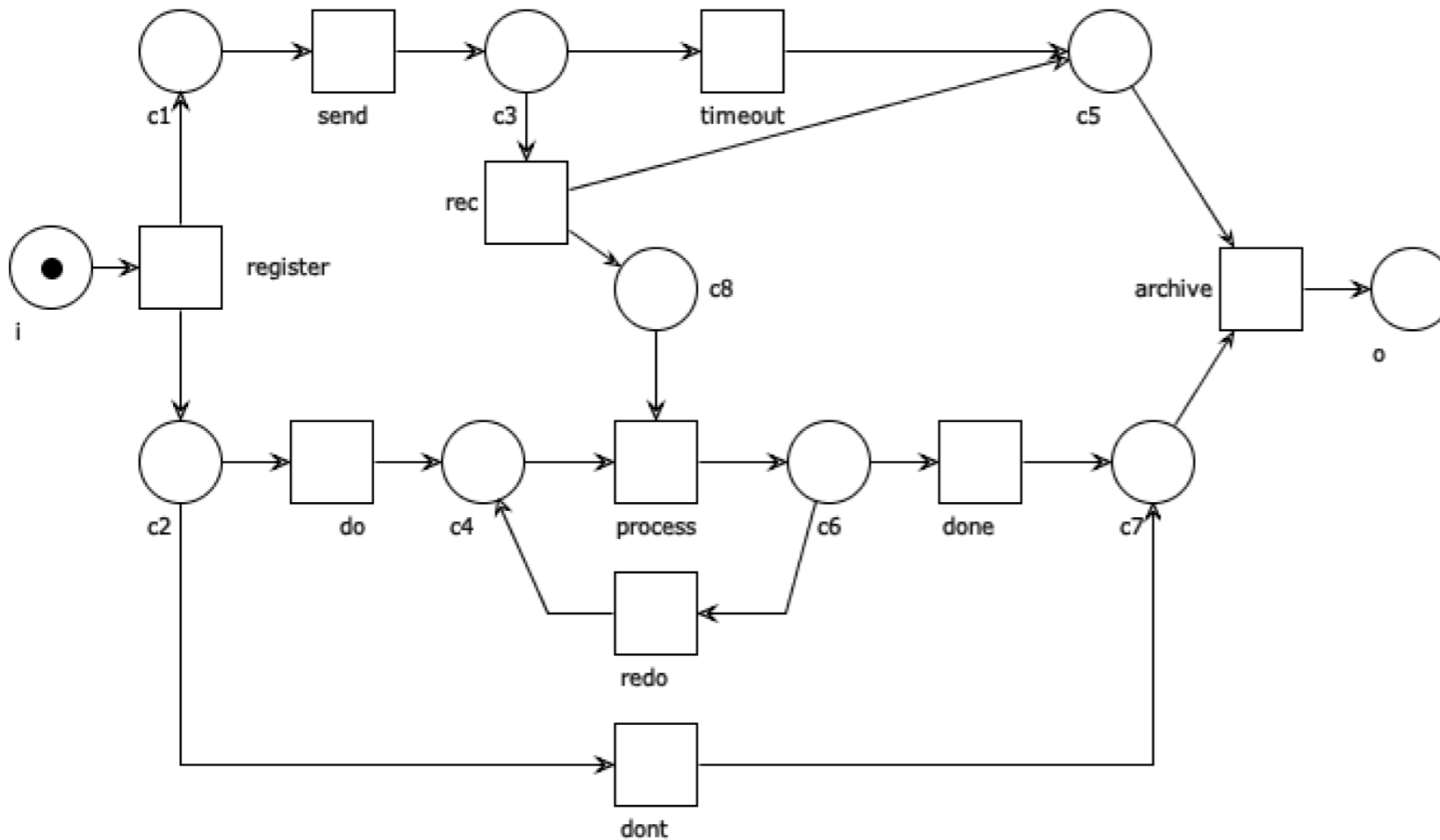
If N and N' are sound free-choice workflow nets
then $N[N'/t]$ is a sound free-choice workflow net

(N, N' are safe; we just need to show that $N[N'/t]$ is free-choice)

Well-structuredness (PT/TP-handles)

Woped

what are PT/TP-handles?
and why are they relevant?



Semantical analysis

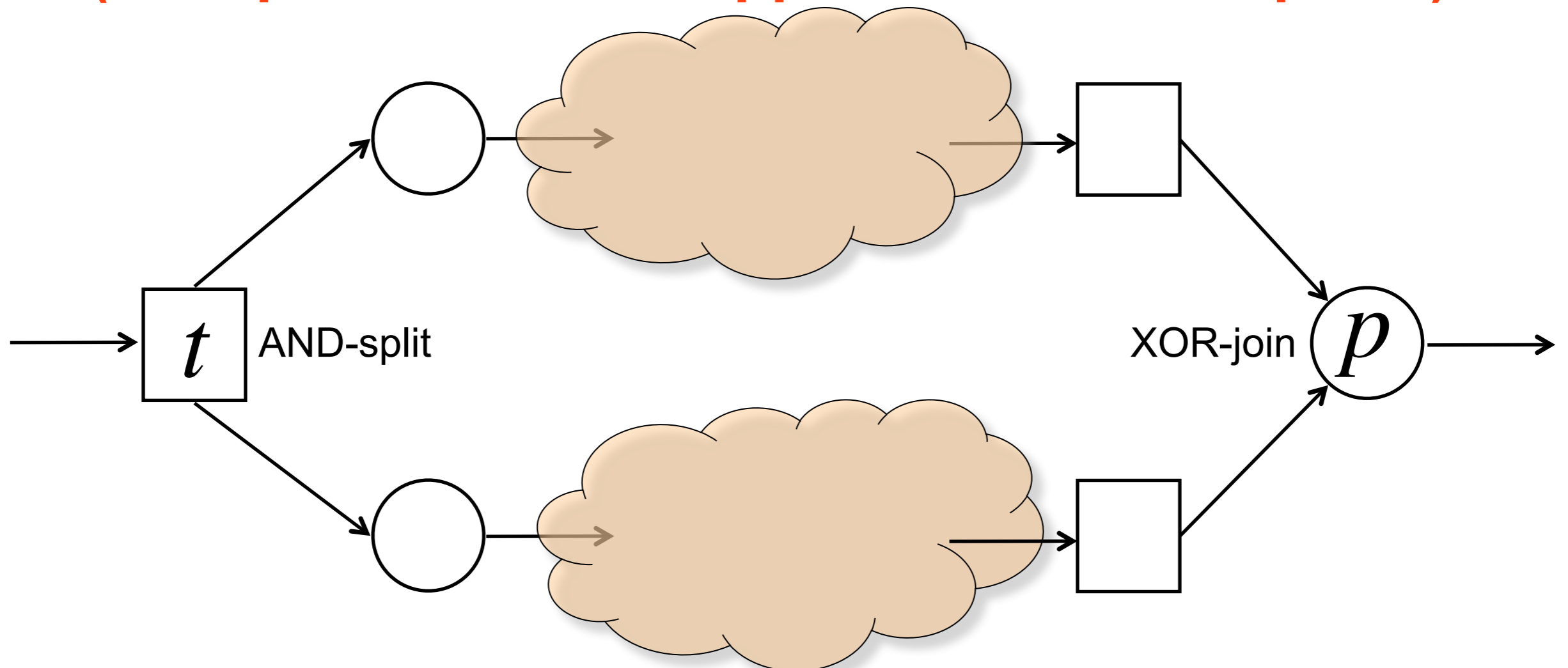
Wizard Expert

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TP-handles

Two parallel flows initiated by an AND-split should not be joined by a XOR-join

(multiple tokens can appear in the same place)



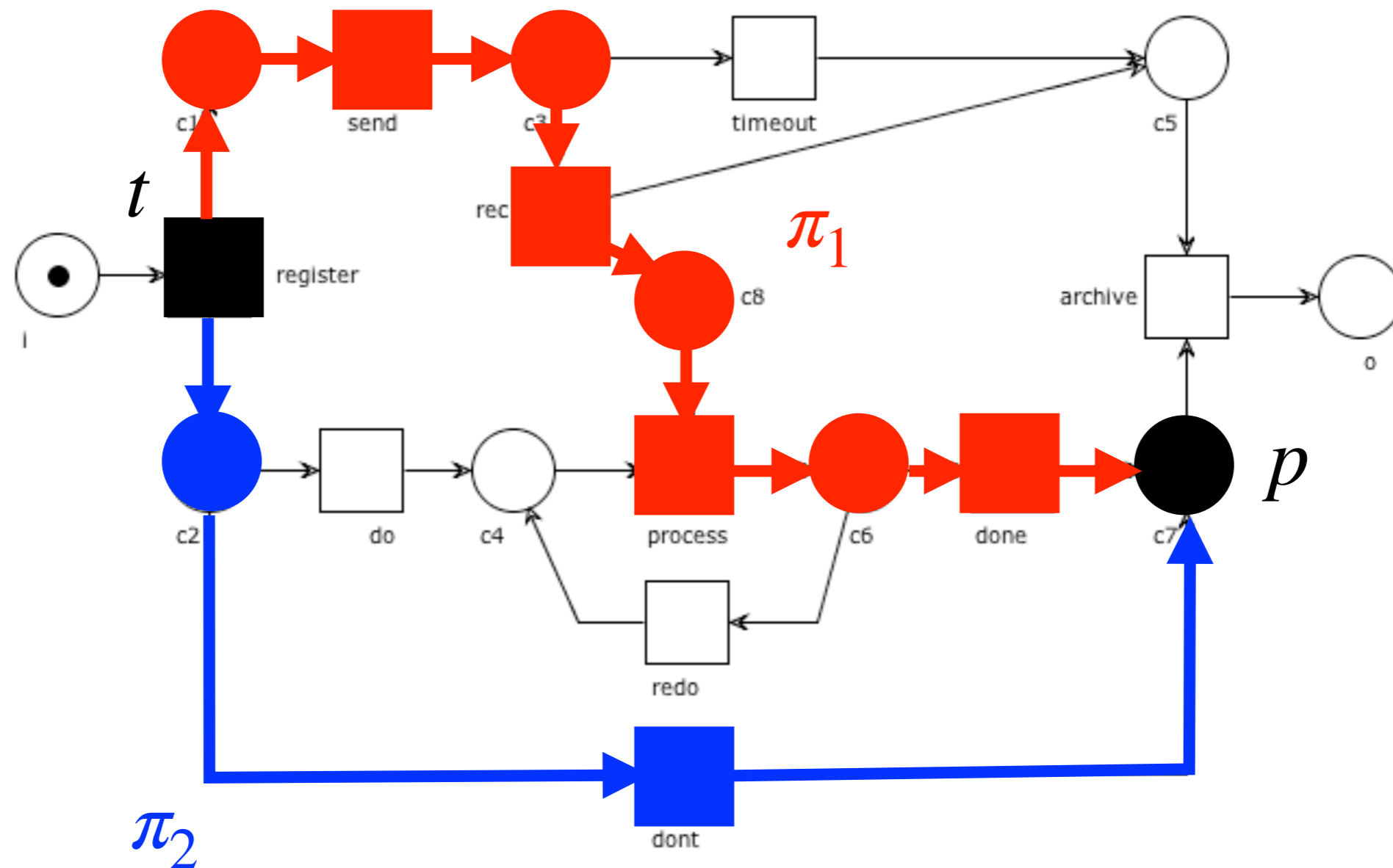
TP-handles

Definition:

A transition t and a place p form a **TP-handle** if there are

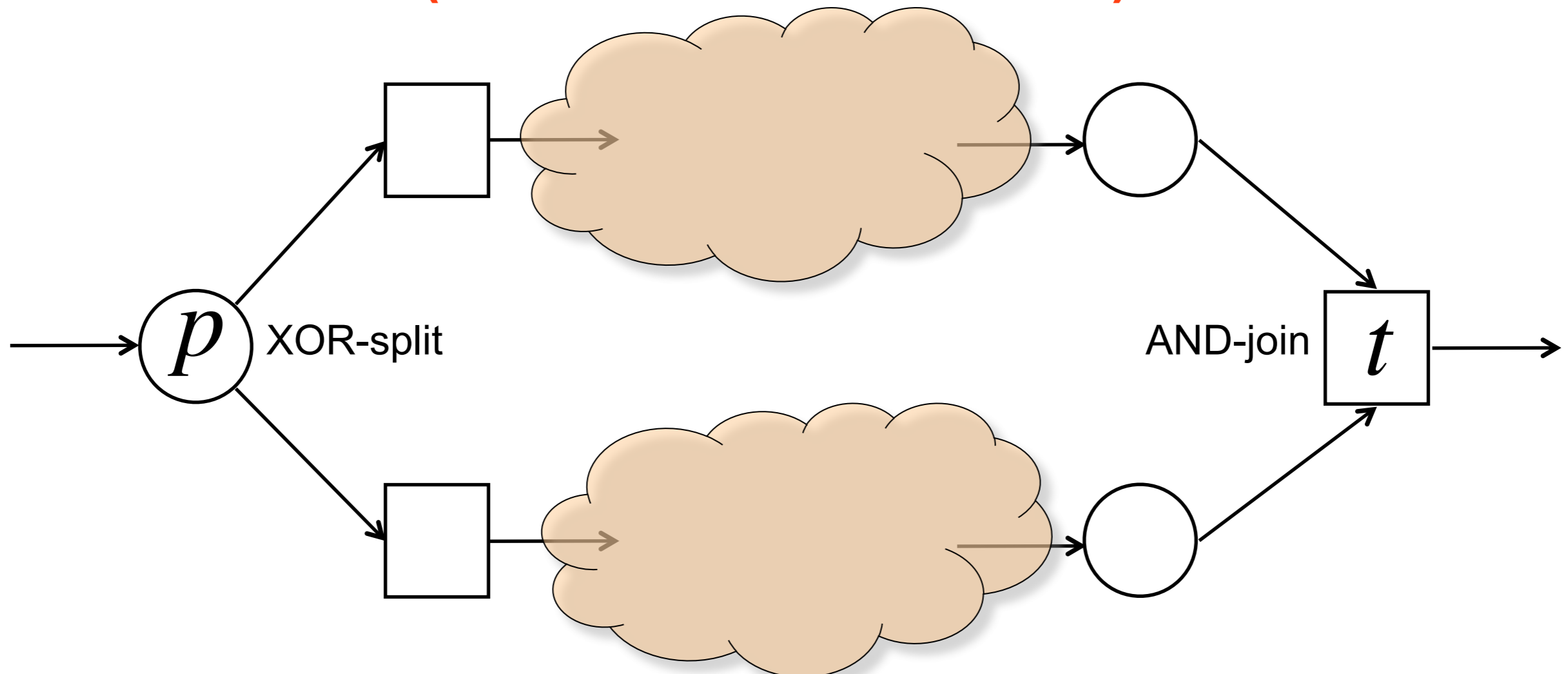
two distinct elementary paths π_1 and π_2 from t to p such that the only nodes they have in common are t, p

Example: TP-handle



PT-handles

Two alternative flows created via a XOR-split
should not be synchronized by an AND-join
(the net could deadlock)



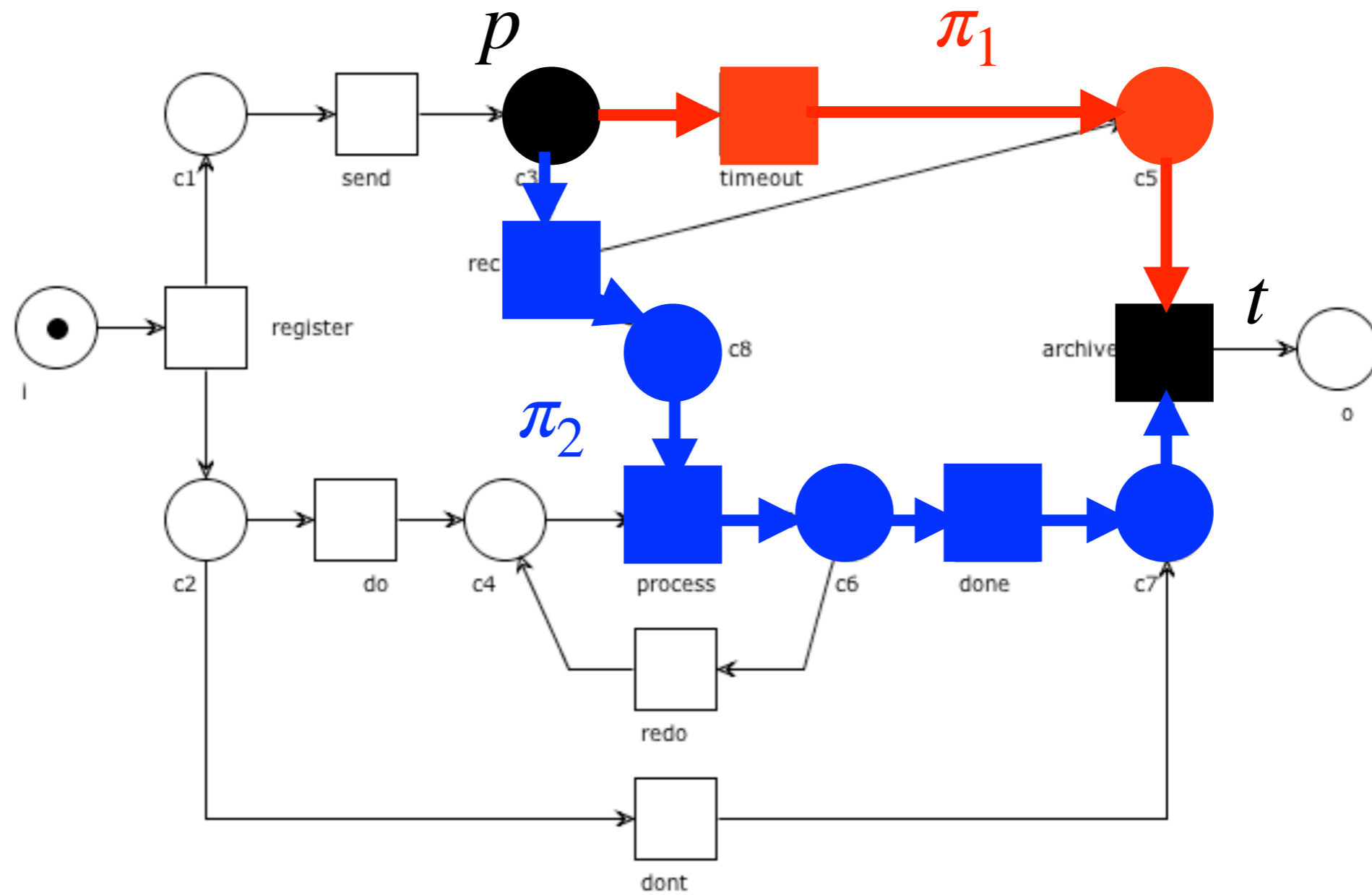
PT-handles

Definition:

A place p and a transition t form a **PT-handle** if there are

two distinct elementary paths π_1 and π_2 from p to t such that the only nodes they have in common are p, t

Example: PT-handle



Well-Structured Nets

Definition: A net is **well-handled** if it has neither TP-handles nor PT-handles

Definition: A workflow net N is **well-structured** if N^* is well-handled

Be careful

N well-structured = N^* well-handled

reset transition is implicit in WoPeD

WoPeD marks PT/TP-handles over N^*
(not over N)

WoPeD Diagnosis

The image displays the WoPeD Diagnosis interface for a Petri net model named 'wfnet-unsound.pnml'. The interface is divided into several sections:

- Process Resources BPEL preview:** A navigation bar at the top of the main window.
- Diagram:** A Petri net diagram with places $c1, c2, c3, c4, c5, c6, c7, c8$ and transitions $i, o, register, send, rec, timeout, do, process, redo, dont, archive$. Places $c3$ and $process$ are highlighted in red. A red circle labeled p is positioned above $c3$, and a red square labeled t is positioned below $process$.
- Semantical analysis:** A panel on the right side with 'Wizard' and 'Expert' tabs. It shows a tree of analysis results:
 - Qualitative analysis
 - Structural analysis
 - Net statistics
 - Wrongly used operators: 0
 - Free-choice violations: 0
 - S-Components
 - Wellstructuredness
 - PT-Handles: 4
 - PT-Handle pair #1
 - PT-Handle pair #2
 - PT-Handle pair #3
 - PT-Handle pair #4** (highlighted)
 - $c3$
 - $process$
 - TP-Handles: 5
 - TP-Handle pair #1
 - $register$
 - $c7$
 - TP-Handle pair #2
 - TP-Handle pair #3
 - TP-Handle pair #4
 - TP-Handle pair #5
 - Soundness

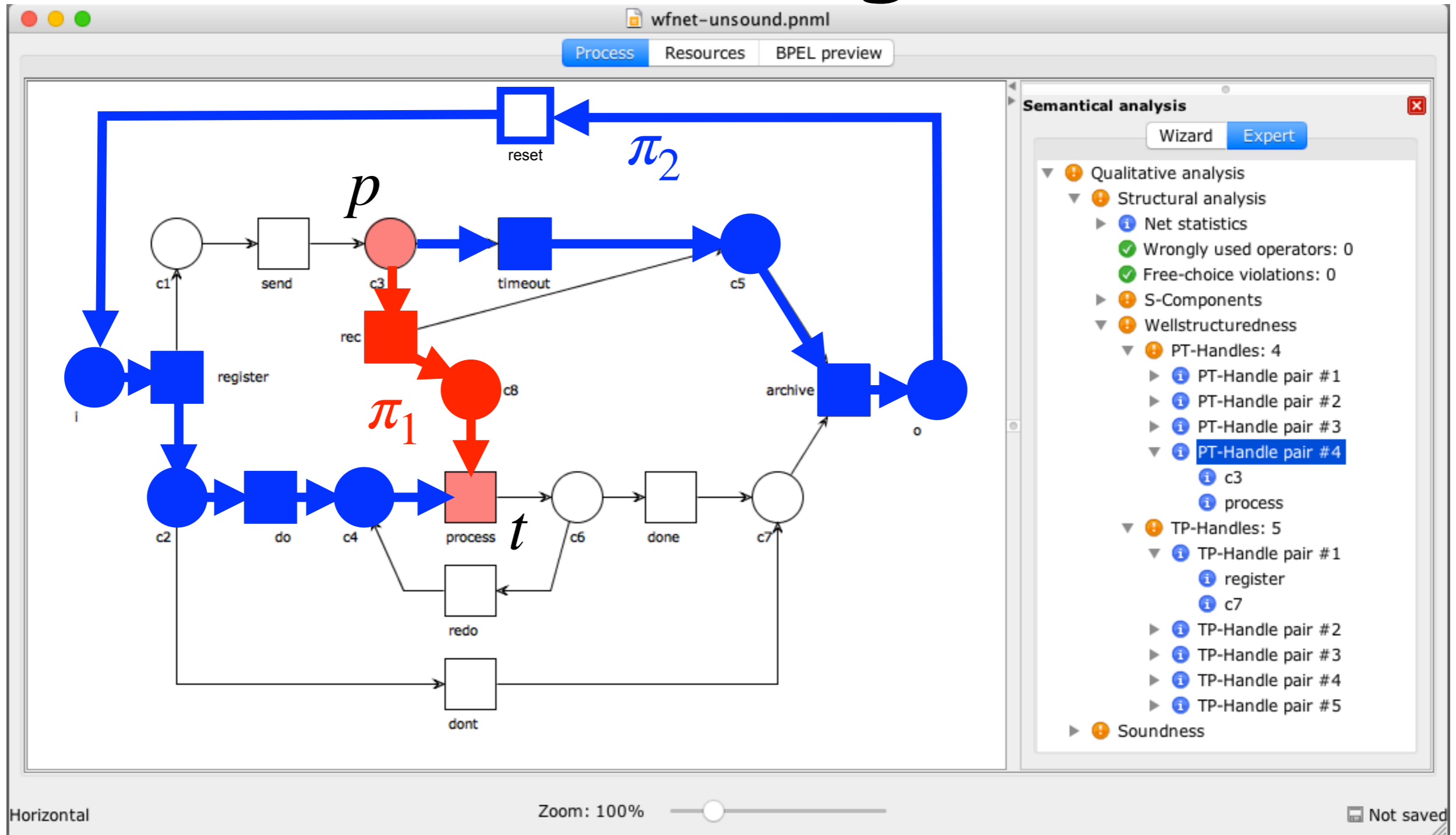
WoPeD Diagnosis

The image displays the WoPeD Diagnosis interface for a workflow net (wfnet-unsound.pnml). The main window shows a Petri net diagram with places c_1 through c_8 and transitions labeled with activities: `register`, `send`, `rec`, `do`, `process`, `redo`, `dont`, `timeout`, and `archive`. The initial place is i and the final place is o . A red circle c_3 is labeled p , and a red square `process` is labeled π_1 . A red arrow points from c_3 to `process`. A red circle c_8 is also highlighted with a red arrow pointing to `process`. The diagram is annotated with a t near the `process` transition.

The **Semantical analysis** panel on the right shows the following structure:

- Qualitative analysis
 - Structural analysis
 - Net statistics
 - Wrongly used operators: 0
 - Free-choice violations: 0
 - S-Components
 - Wellstructuredness
 - PT-Handles: 4
 - PT-Handle pair #1
 - PT-Handle pair #2
 - PT-Handle pair #3
 - PT-Handle pair #4**
 - c_3
 - process
 - TP-Handles: 5
 - TP-Handle pair #1
 - register
 - c_7
 - TP-Handle pair #2
 - TP-Handle pair #3
 - TP-Handle pair #4
 - TP-Handle pair #5
- Soundness

WoPeD Diagnosis



Well-structuredness, S-coverability and Soundness

Theorem: If N is sound and well-structured,
then N^* is S-coverable
(proof omitted)

Consequence:

N well-structured + N^* not S-coverable \Rightarrow N not sound

Error sequences

Woflan

<http://www.win.tue.nl/woflan/>

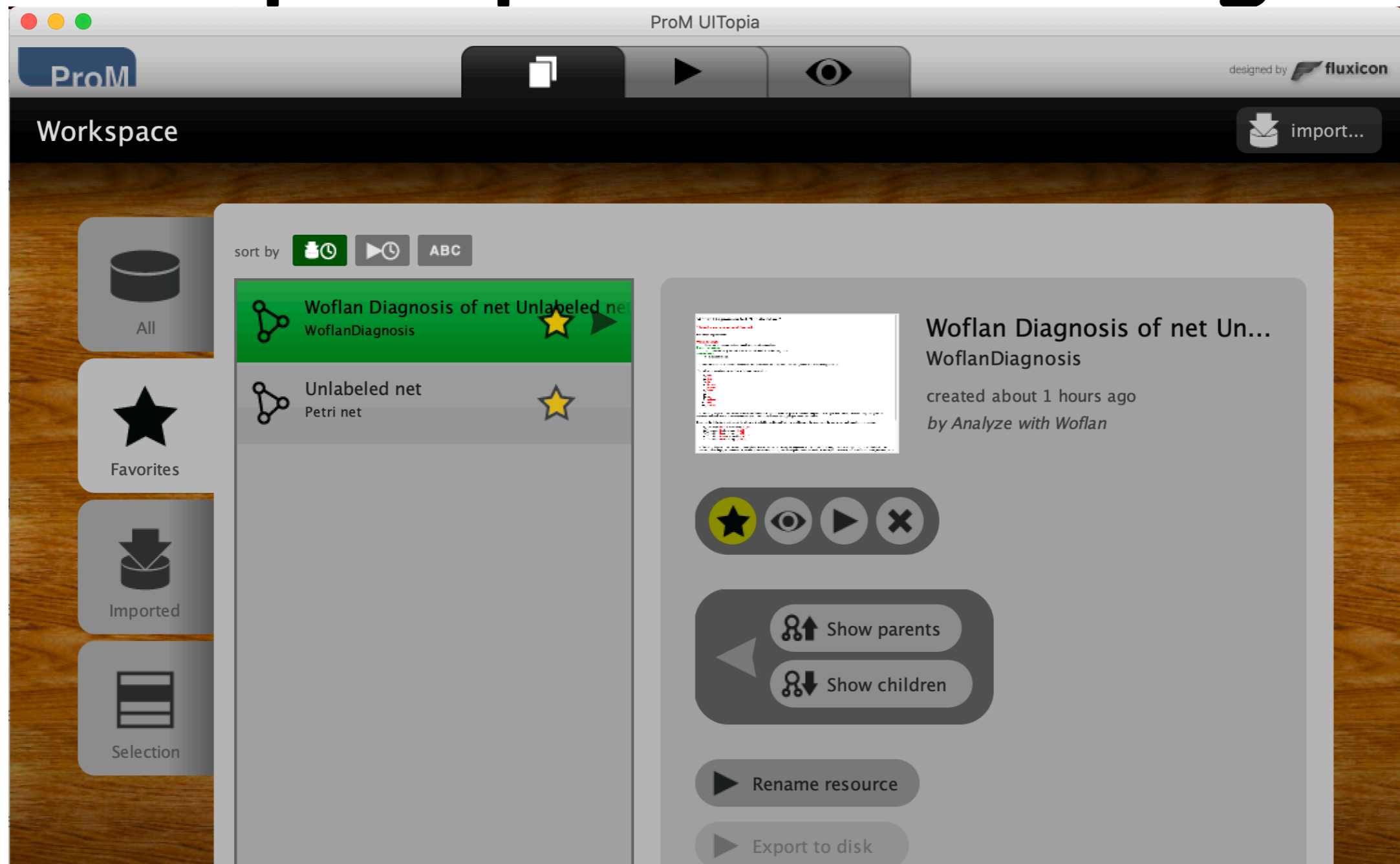
WOrkFLow ANalyzer
(Microsoft Windows only)



Woflan tells us if N is a sound workflow net
(Is N a workflow net? Is N^* bounded? Is N^* live?)
if not, provides some diagnostic information

Woflan now a ProM plugin

<http://promtools.org/>



Woflan (in ProM)

ProM UI Topia

ProM

Woflan Diagnosis of net Unlabeled net

Select visualisation ...

The net is not a sound workflow net.

Soundness requirements

Option to complete
Whatever happens, an instance can always mark the sink place

Proper completion
On completion, only the sink place is marked, and it is marked only once

No dead tasks
No transition is dead

Disabling the following transitions at the following (reachable) markings effectively would restrict the behavior to the bounded safe haven:

1. Transition **rec** at marking [c7,c3]
2. Transition **dont** at marking [c5,c8,c2]

what are the reasons for these suggestions?

Soundness requirements

Option to complete
Whatever happens, an instance can always mark the sink place

Proper completion
On completion, only the sink place is marked, and it is marked only once

No dead tasks
No transition is dead

Disabling the following transitions at the following (reachable) markings effectively would restrict the behavior to the part from which completion is possible:

1. Transition **timeout** at marking [c2,c3].
2. Transition **do** at marking [c2,c3].
3. Transition **do** at marking [c1,c2].
4. Transition **timeout** at marking [c3,c7].
5. Transition **do** at marking [c8,c5,c2].

Diagnostic information

The sets of:
unbounded places of N^*
dead transitions of N^*
non-live transitions of N^*

may provide useful information for
the diagnosis of behavioural errors

Unfortunately, this information is not always sufficient
to determine the exact cause of the error

Behavioural error sequences help us to locate problems

Error sequences

Rationale:

We want to find firing sequences such that:

1. every continuation of such sequences will lead to an error
2. they are as short as possible
(none of their prefixes satisfies the above property)

Informally:

error sequences are scenarios that capture the essence of errors made in the workflow design (violate “option to complete” or “proper completion”)

Error sequences:
Non-live sequences

Non-Live sequences: informally

A **non-live sequence** is a firing sequence as short as possible such that **completion of the case is no longer possible**

i.e. a witness for transition reset being non-live in N^*

Non-Live sequences: fundamental property

Let N be such that:
 N^* is bounded
 N (or equivalently N^*) has no dead task

Then, N^* is live
iff
 N has no non-live sequences

Non-Live sequences: graphically

The analysis is possible in bounded systems only

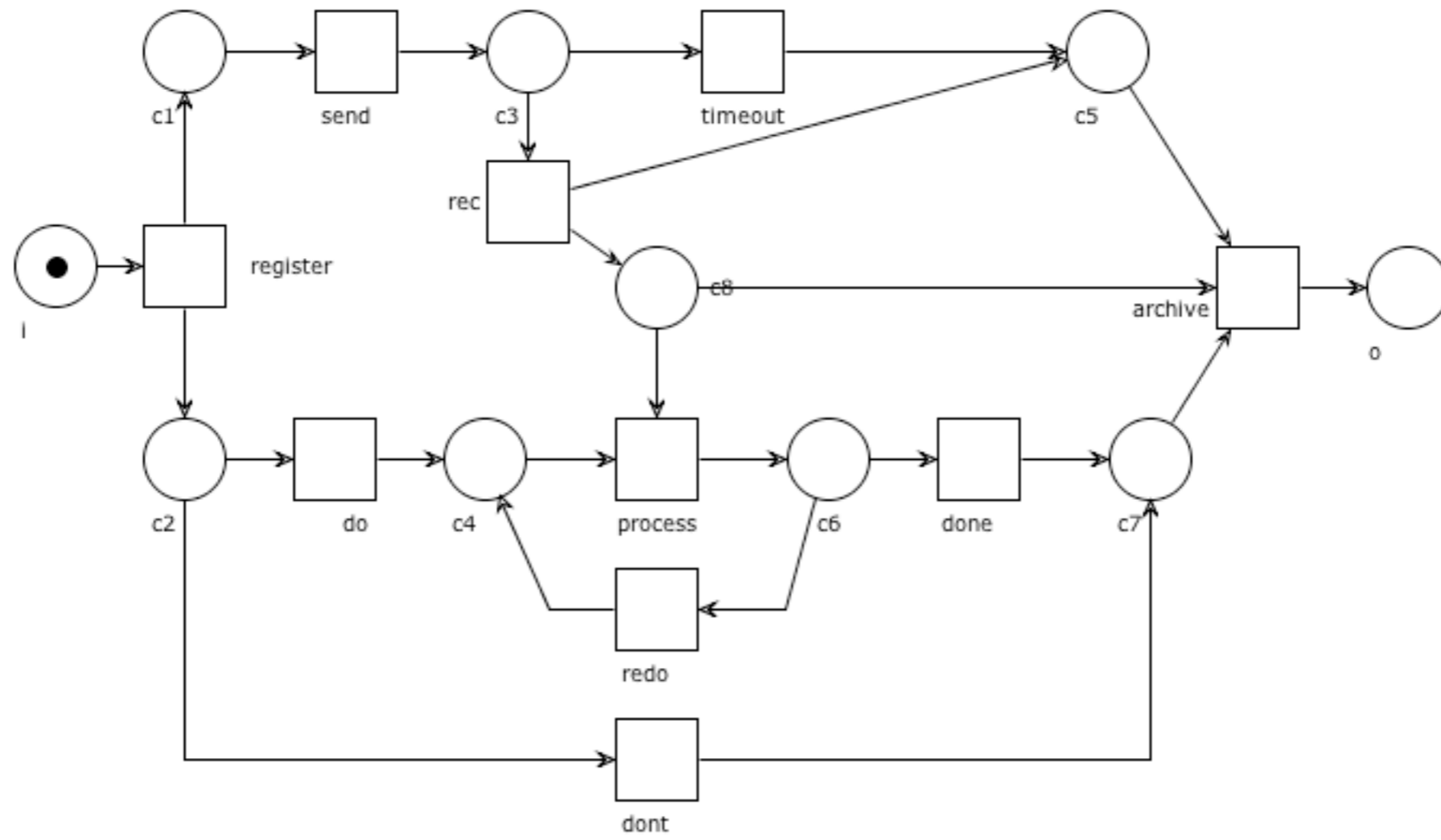
Compute the RG of N^*

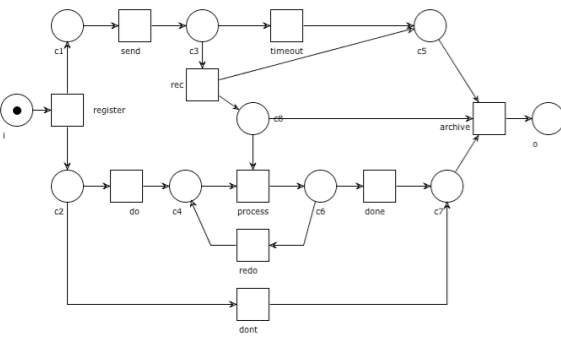
Color in **red** all nodes from which there is **no path** to o

Color in **green** all nodes from which **all paths** lead to o

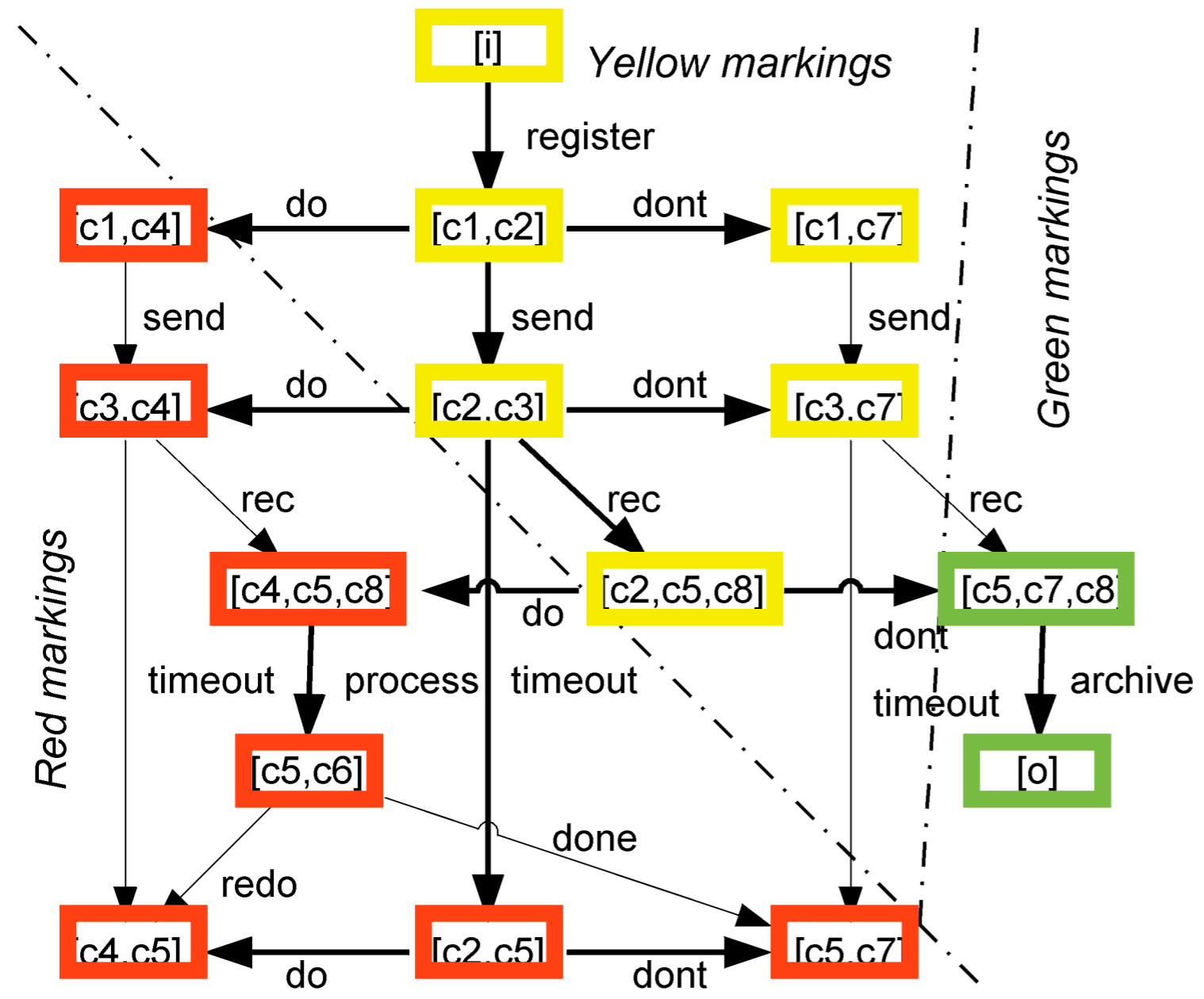
Color in **yellow** all remaining nodes
(some but not all paths lead to o)

Example: N





Example: RG (N)



Non-live sequences:

register, do

register, send, do

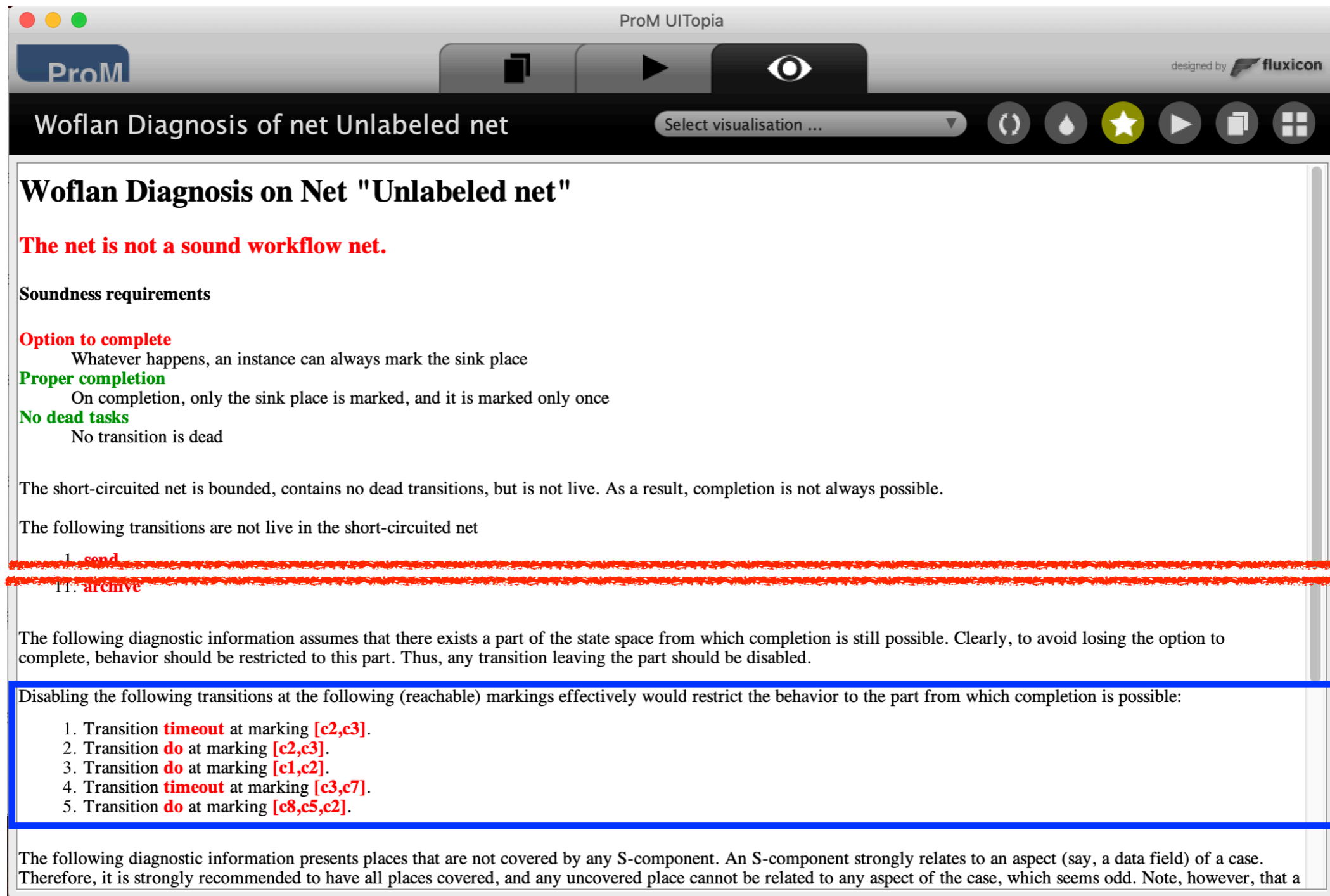
register, send, timeout

register, send, rec, do

register, send, dont, timeout

register, dont, send, timeout

Woflan (in ProM)



The screenshot shows the ProM UI with the title "Woflan Diagnosis of net Unlabeled net". The main content area displays the following text:

Woflan Diagnosis on Net "Unlabeled net"

The net is not a sound workflow net.

Soundness requirements

- Option to complete**
Whatever happens, an instance can always mark the sink place
- Proper completion**
On completion, only the sink place is marked, and it is marked only once
- No dead tasks**
No transition is dead

The short-circuited net is bounded, contains no dead transitions, but is not live. As a result, completion is not always possible.

The following transitions are not live in the short-circuited net

1. ~~send~~
11. ~~archive~~

The following diagnostic information assumes that there exists a part of the state space from which completion is still possible. Clearly, to avoid losing the option to complete, behavior should be restricted to this part. Thus, any transition leaving the part should be disabled.

Disabling the following transitions at the following (reachable) markings effectively would restrict the behavior to the part from which completion is possible:

1. Transition **timeout** at marking [c2,c3].
2. Transition **do** at marking [c2,c3].
3. Transition **do** at marking [c1,c2].
4. Transition **timeout** at marking [c3,c7].
5. Transition **do** at marking [c8,c5,c2].

The following diagnostic information presents places that are not covered by any S-component. An S-component strongly relates to an aspect (say, a data field) of a case. Therefore, it is strongly recommended to have all places covered, and any uncovered place cannot be related to any aspect of the case, which seems odd. Note, however, that a

Error sequences:
Unbounded sequences

Unbounded sequences: informally

An **unbounded sequence** is a firing sequence of **minimal length** such that every continuation **invalidates proper completion**

i.e. a witness for unboundedness

Unbounded sequences: fundamental property

N^* is bounded
iff

N has no unbounded sequences

Undesired markings:
infinite-weighted markings or markings greater than 0

Unbounded sequences: graphically

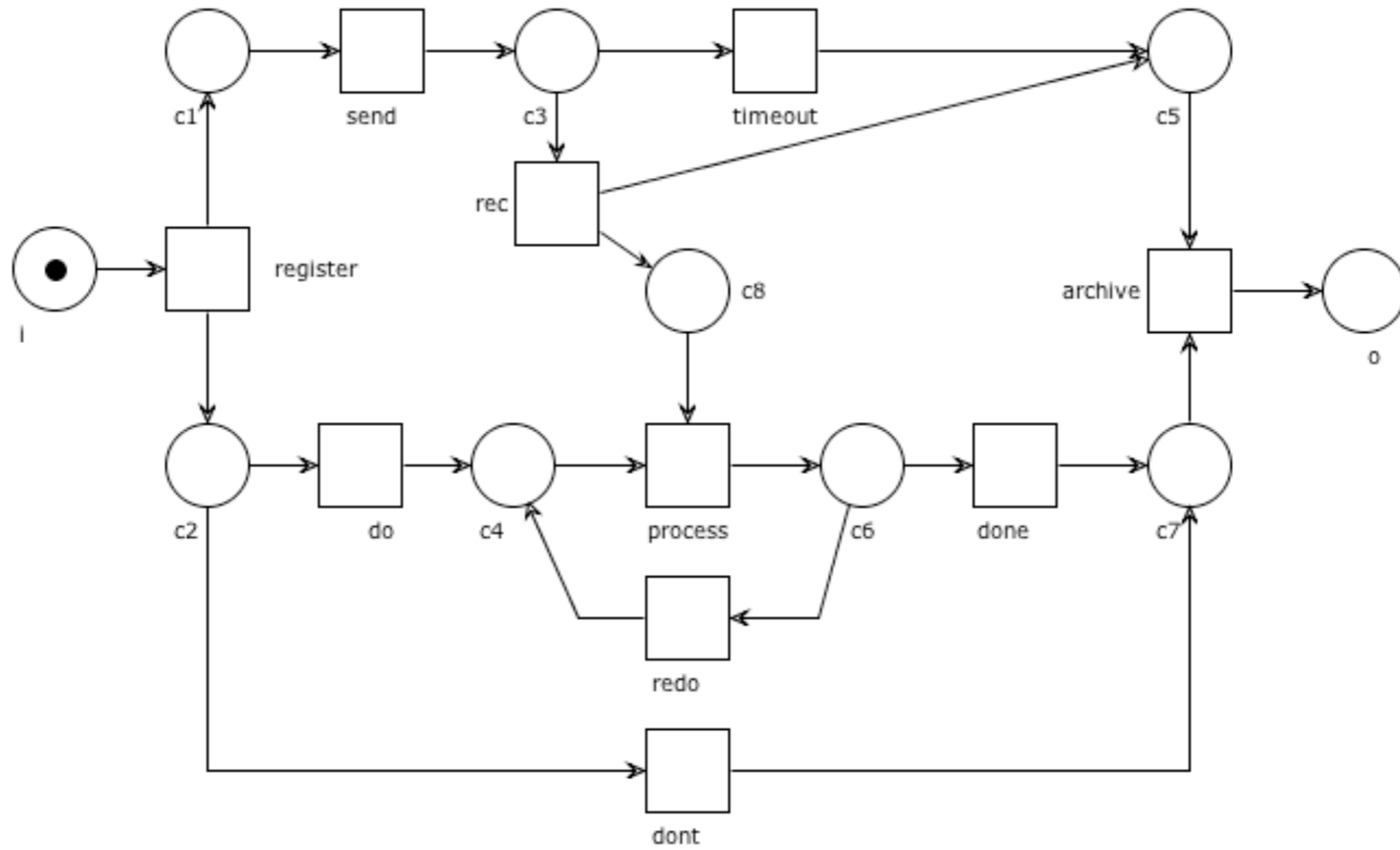
Compute the CG of N^*

Color in **green** all nodes from which
undesired markings are not reachable

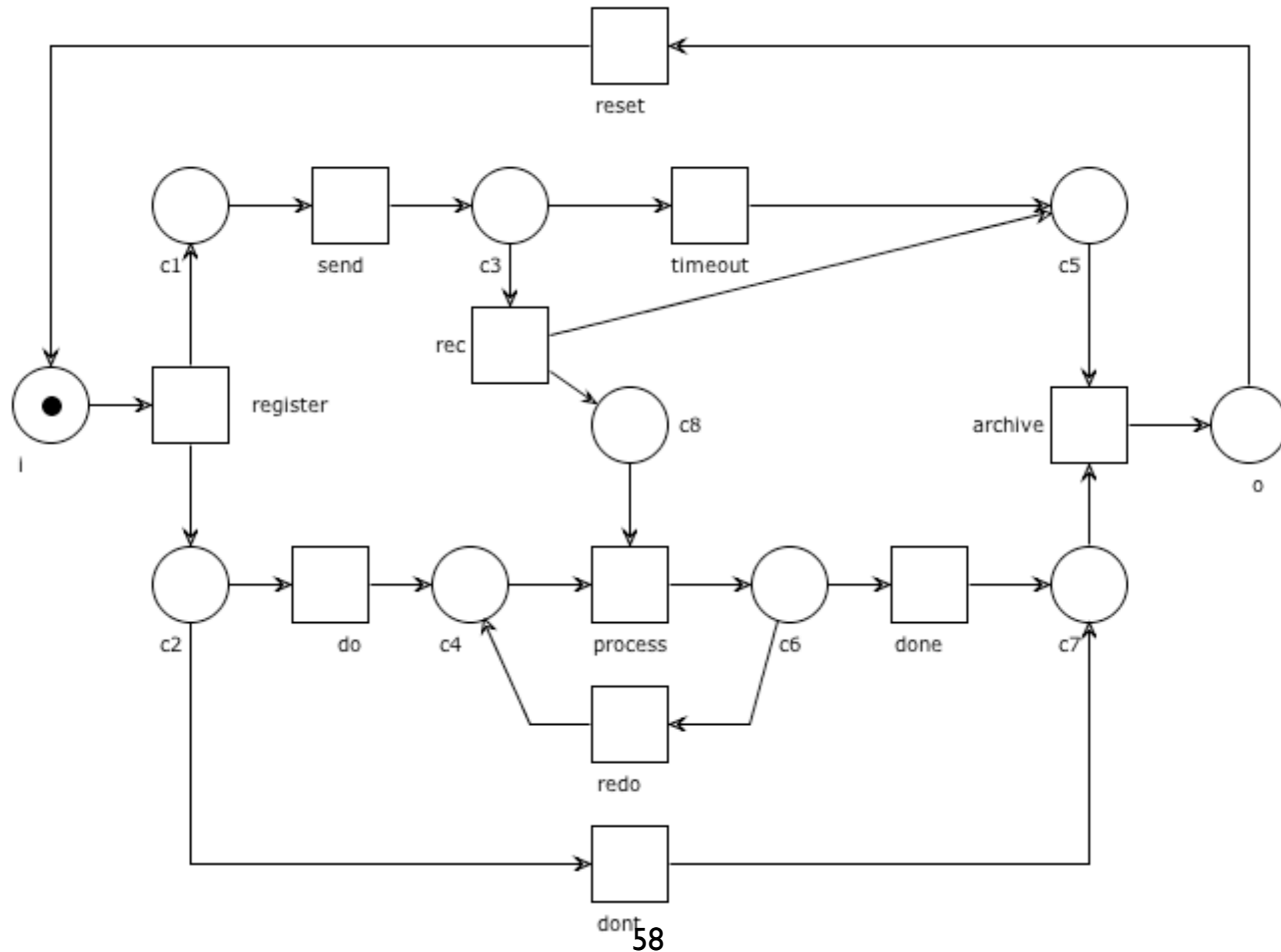
Color in **red** all nodes from which
no green marking is reachable
(undesired markings are unavoidable)

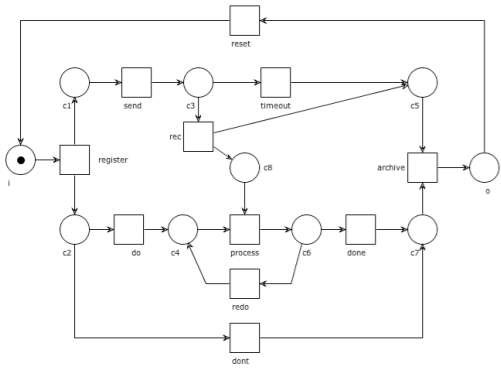
Color in **yellow** all remaining nodes
(undesired markings are reachable but avoidable)

Example: N

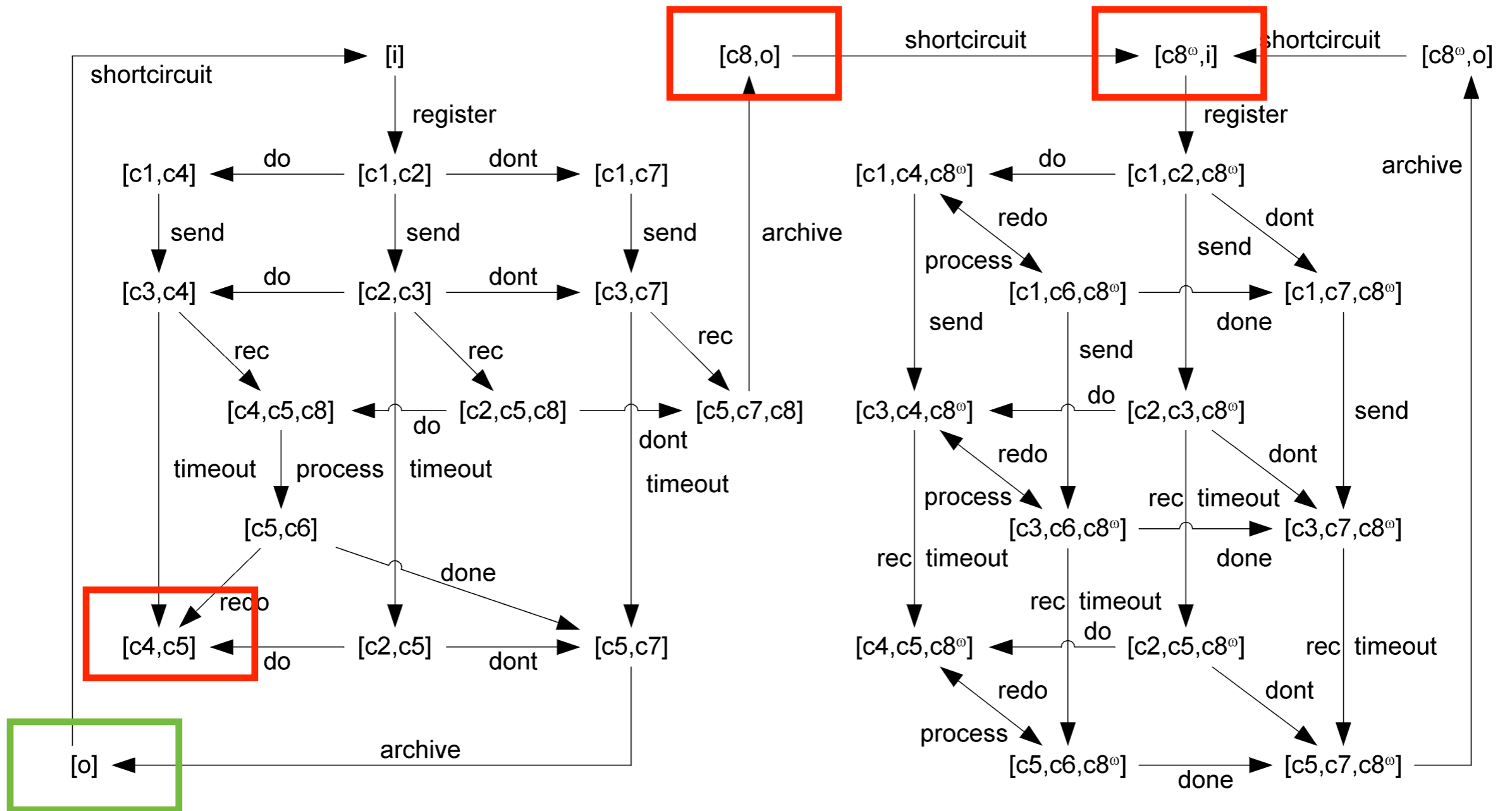


Example: N^*





Example: CG (N^*)



Restricted coverability graph (RCG)

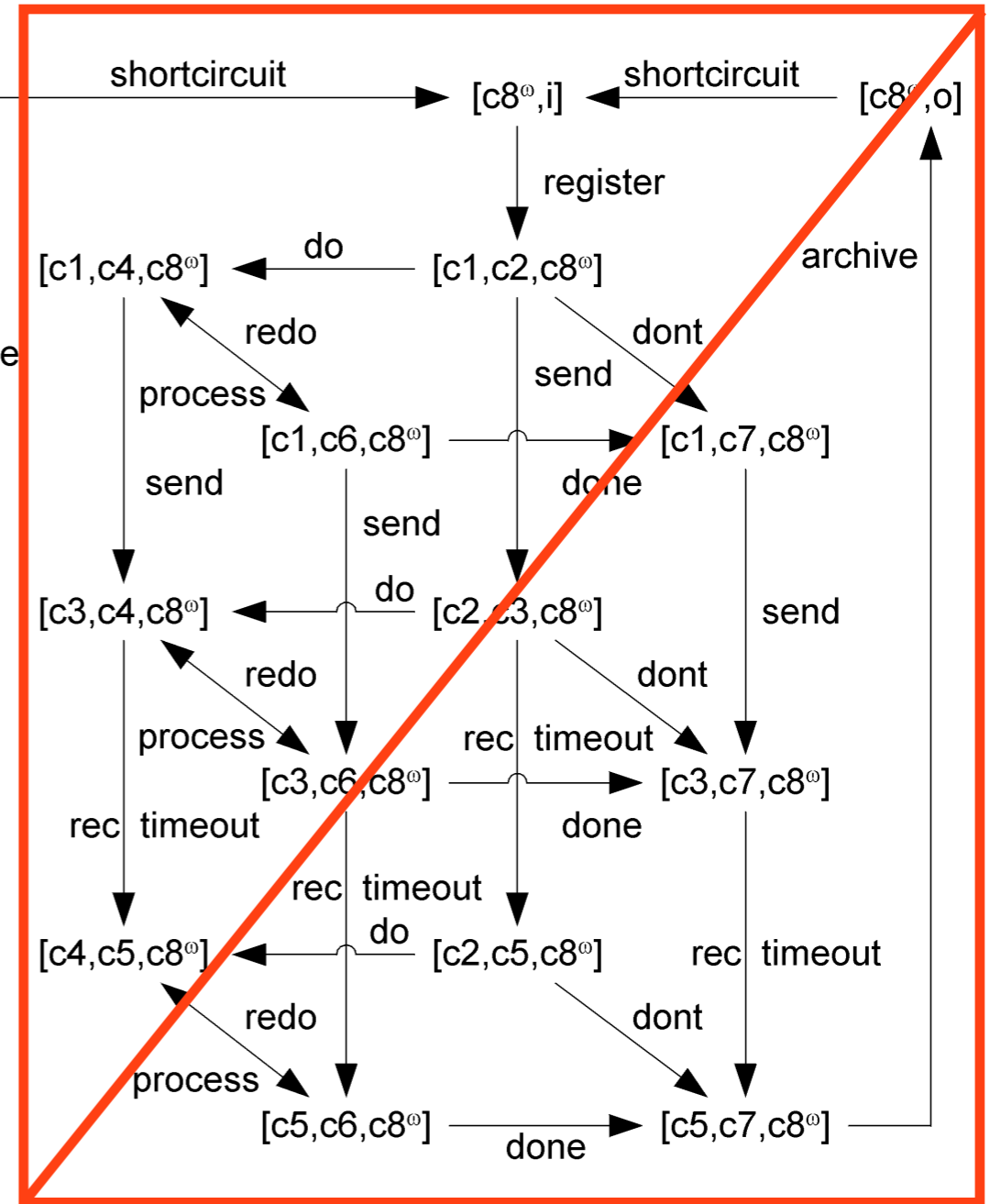
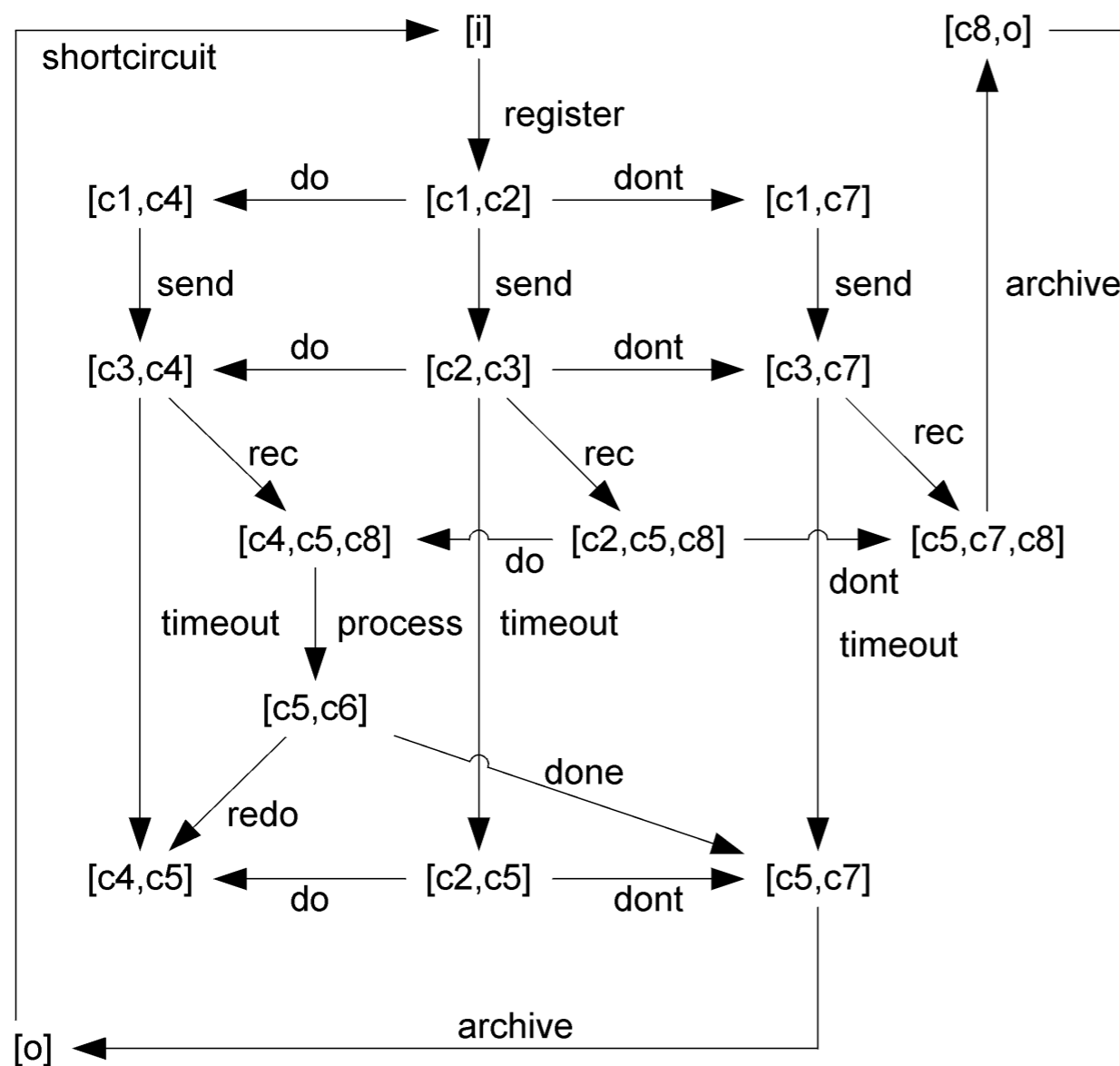
CG can become very large

Basic observation:

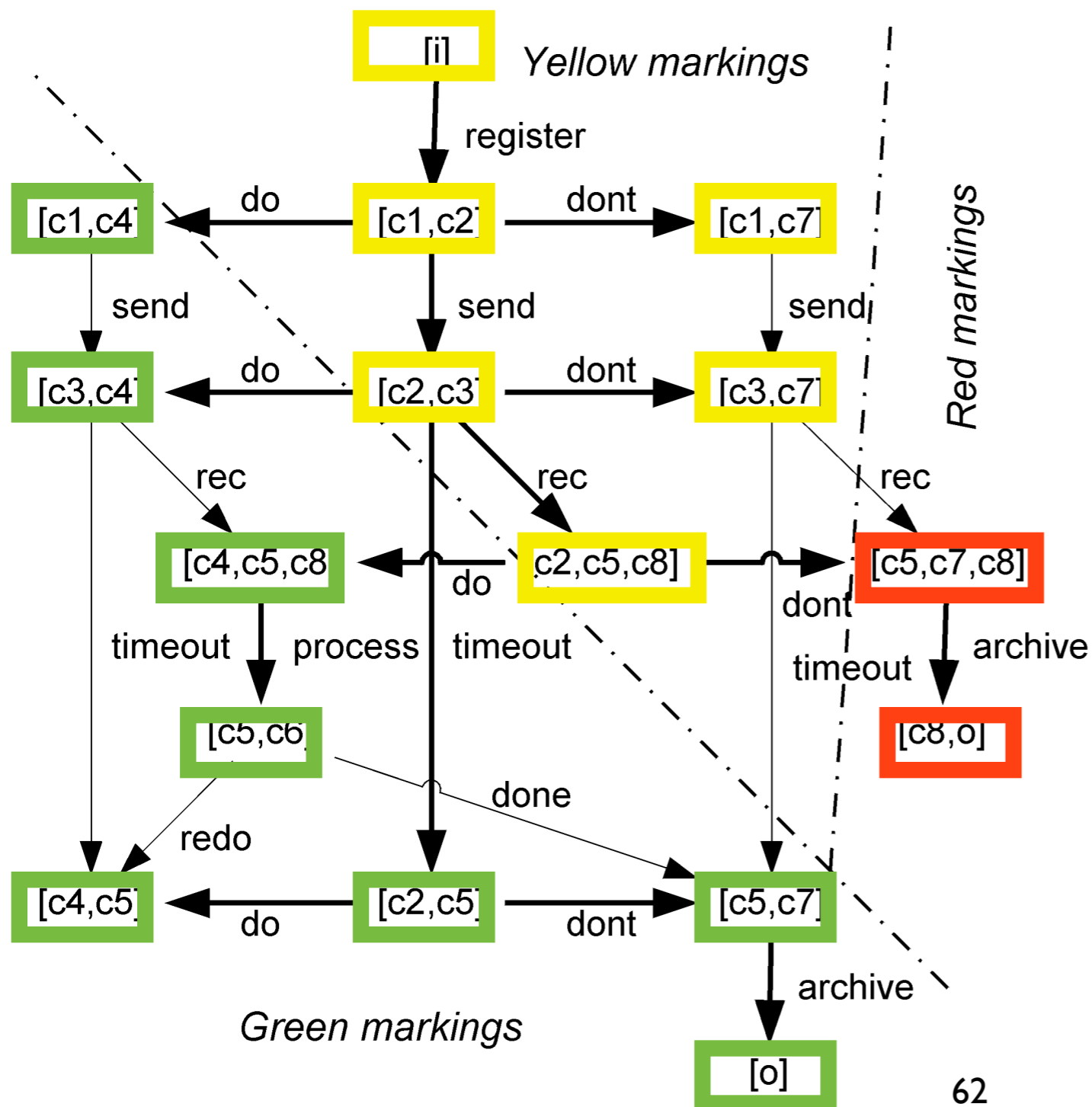
infinite-weighted markings leads to infinite-weighted markings
and they will be all red

We can just avoid computing them!

Example: Restricted CG vs CG



Example: RCG (N*)



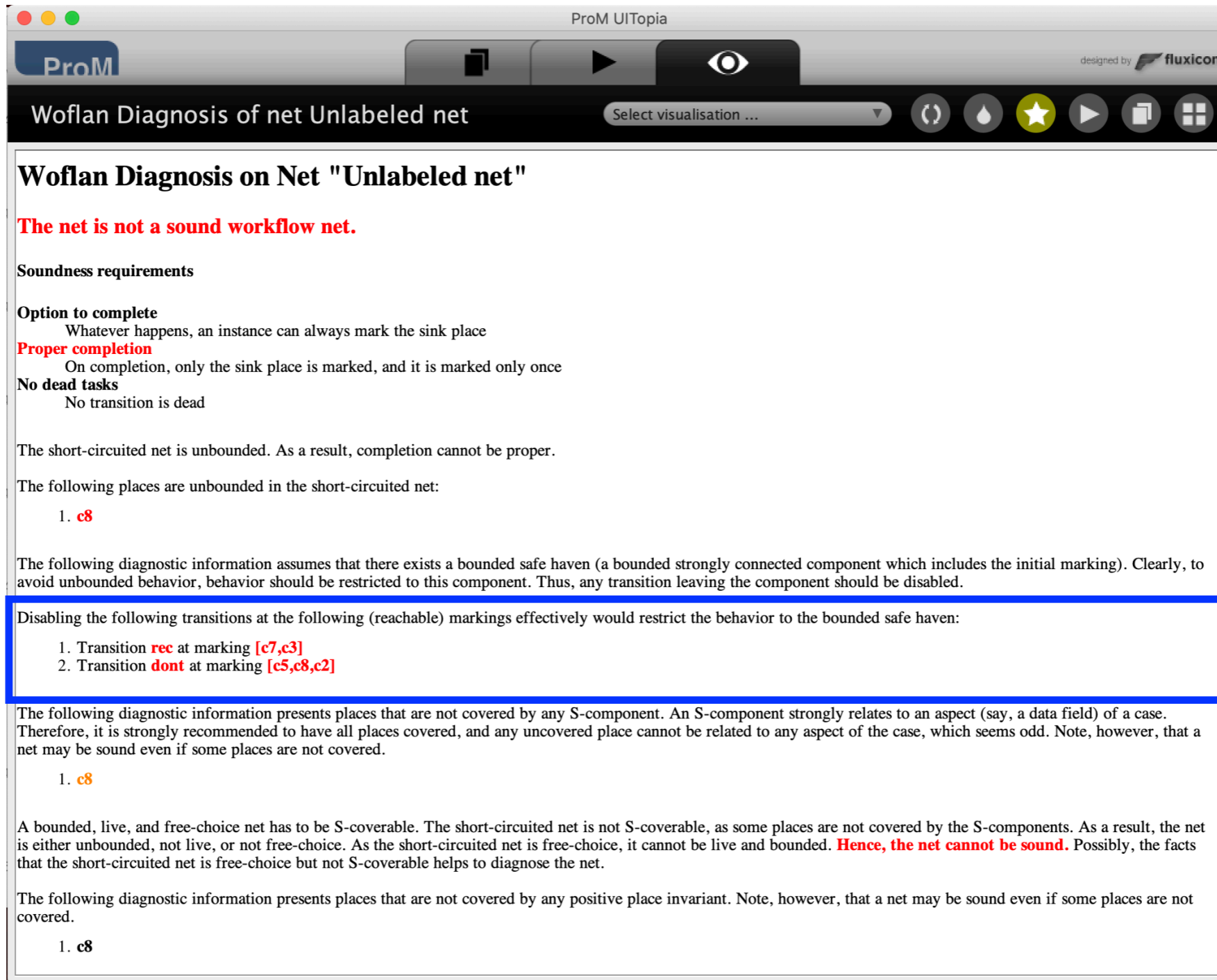
Unbounded sequences:

register, dont, send, **rec**

register, send, dont, **rec**

register, send, rec, **dont**

Woflan (in ProM)



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Soundness requirements

Option to complete
Whatever happens, an instance can always mark the sink place

Proper completion
On completion, only the sink place is marked, and it is marked only once

No dead tasks
No transition is dead

The short-circuited net is unbounded. As a result, completion cannot be proper.

The following places are unbounded in the short-circuited net:

1. **c8**

The following diagnostic information assumes that there exists a bounded safe haven (a bounded strongly connected component which includes the initial marking). Clearly, to avoid unbounded behavior, behavior should be restricted to this component. Thus, any transition leaving the component should be disabled.

Disabling the following transitions at the following (reachable) markings effectively would restrict the behavior to the bounded safe haven:

1. Transition **rec** at marking **[c7,c3]**
2. Transition **dont** at marking **[c5,c8,c2]**

The following diagnostic information presents places that are not covered by any S-component. An S-component strongly relates to an aspect (say, a data field) of a case. Therefore, it is strongly recommended to have all places covered, and any uncovered place cannot be related to any aspect of the case, which seems odd. Note, however, that a net may be sound even if some places are not covered.

1. **c8**

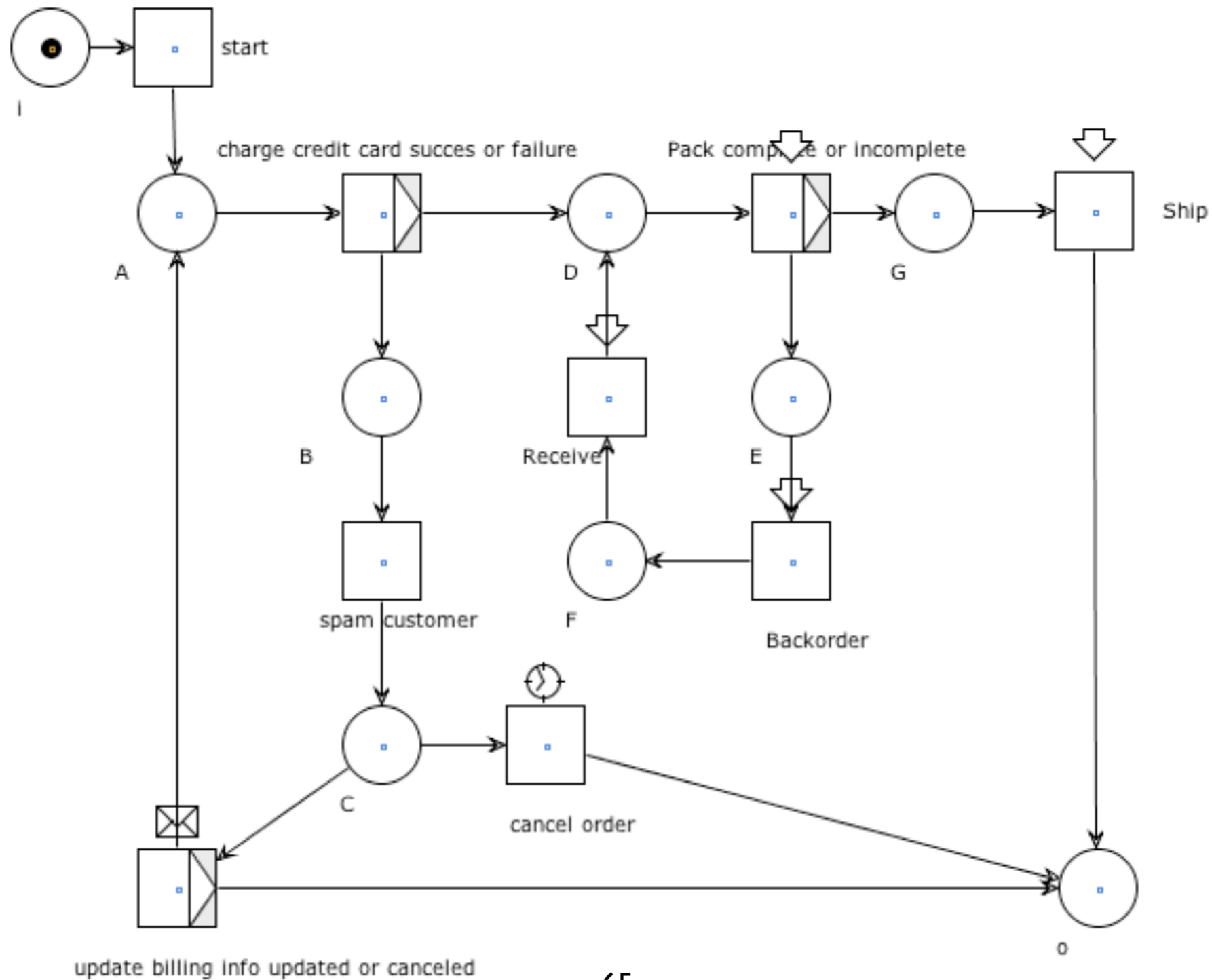
A bounded, live, and free-choice net has to be S-coverable. The short-circuited net is not S-coverable, as some places are not covered by the S-components. As a result, the net is either unbounded, not live, or not free-choice. As the short-circuited net is free-choice, it cannot be live and bounded. **Hence, the net cannot be sound.** Possibly, the facts that the short-circuited net is free-choice but not S-coverable helps to diagnose the net.

The following diagnostic information presents places that are not covered by any positive place invariant. Note, however, that a net may be sound even if some places are not covered.

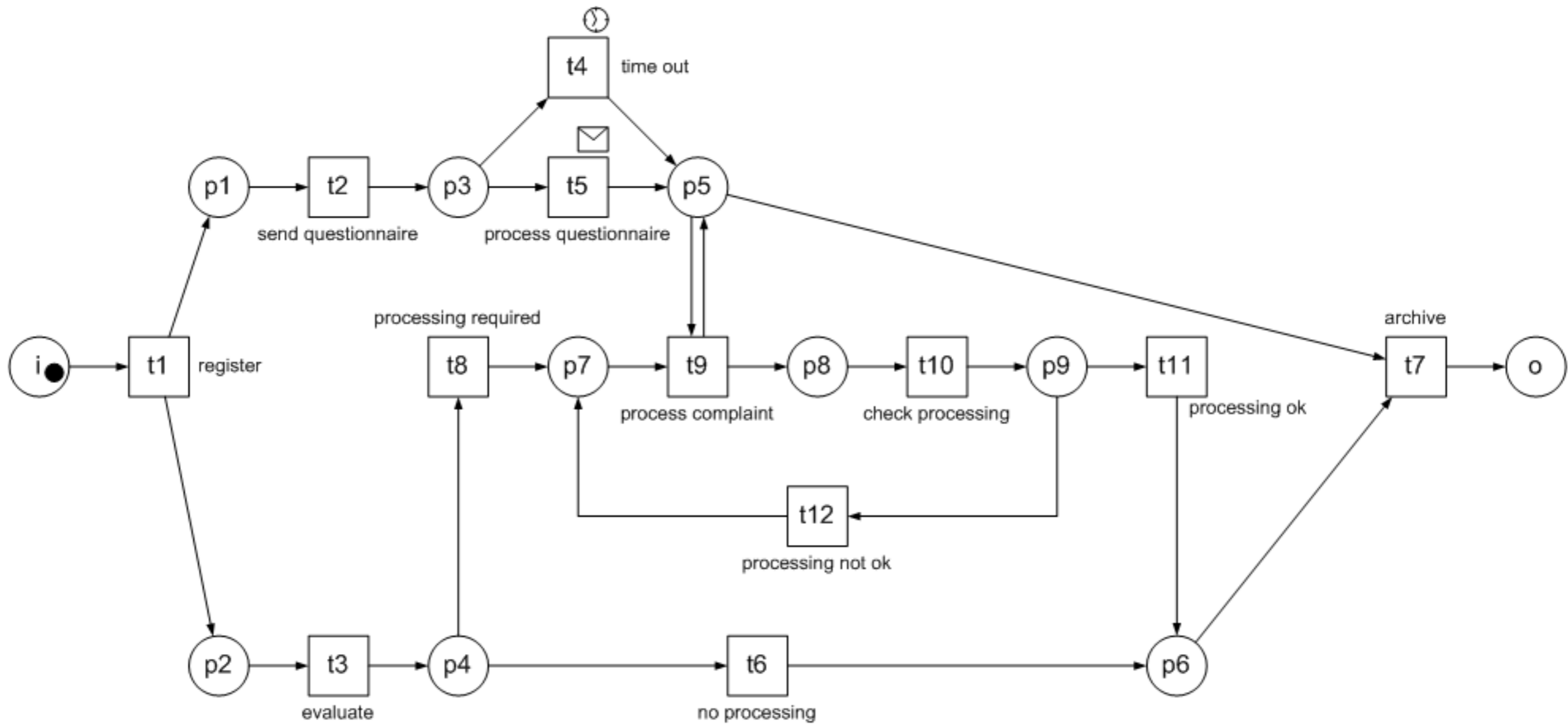
1. **c8**

Practice with WoPeD (and Woflan)

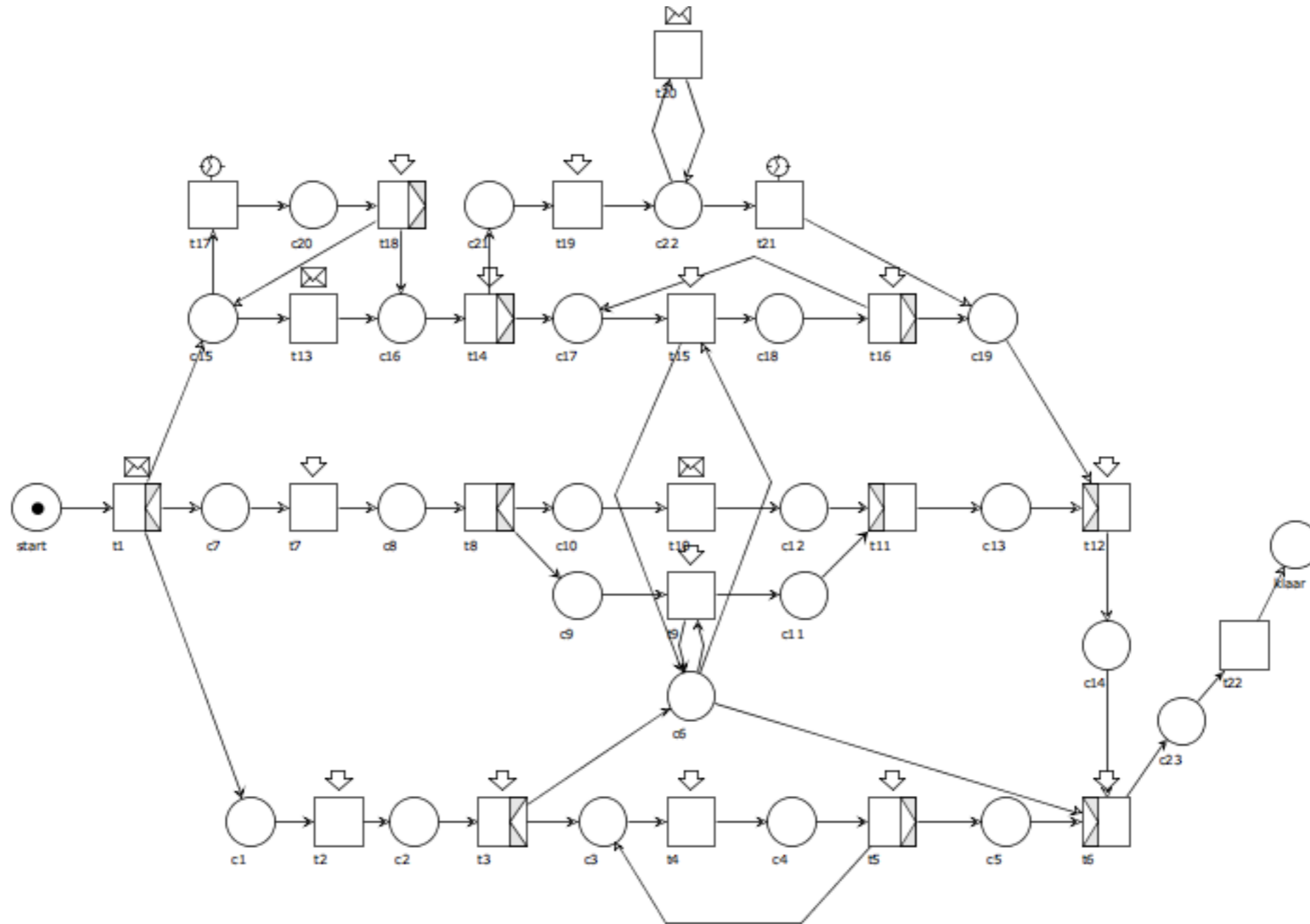
Analyse this net



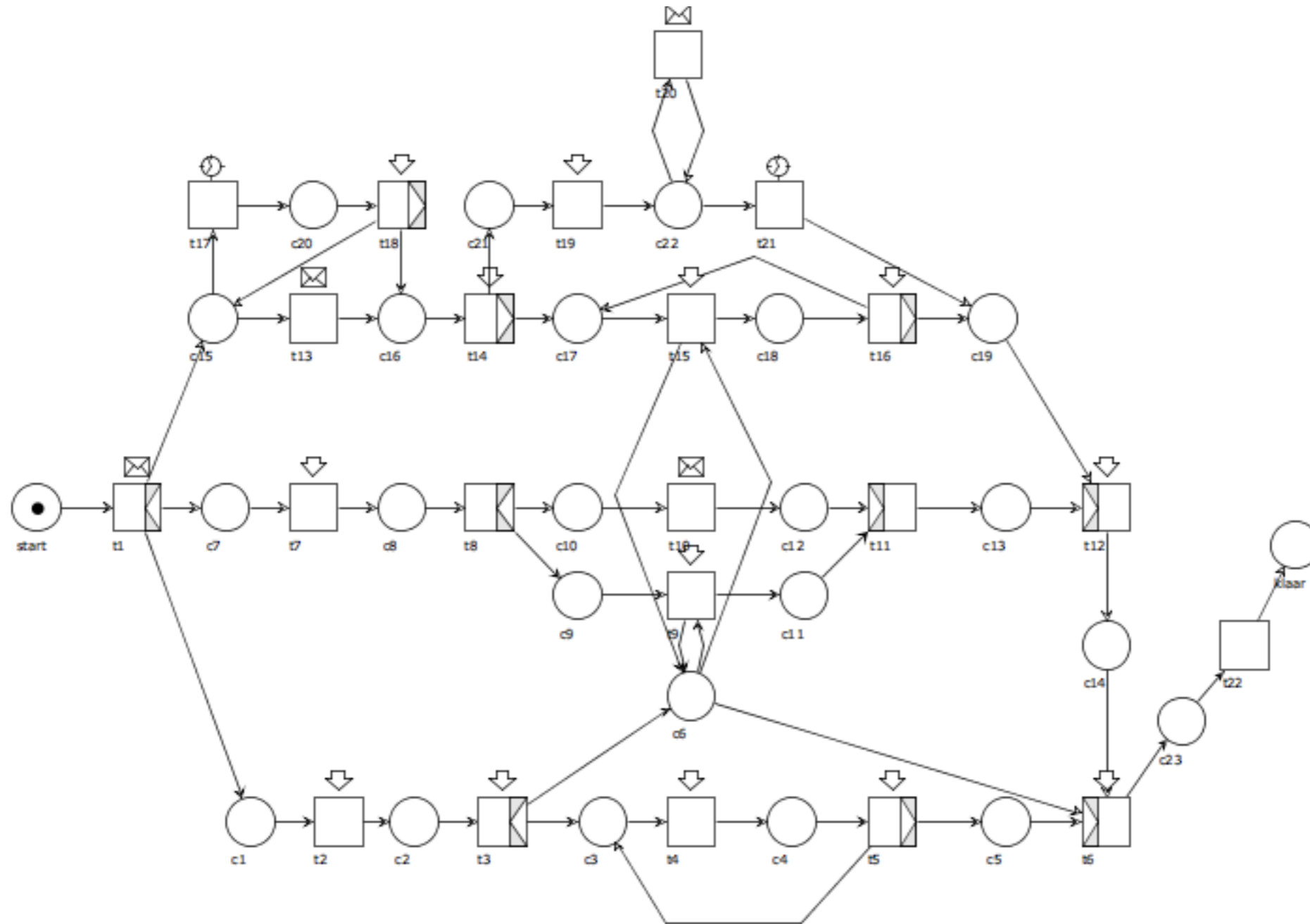
Analyse this net



Is this net free-choice?



Is this net S-coverable?



Is this net sound?

