



Social Network Analysis

a crash mini-course

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MAINS – DM & CRM

Complex

[adj., v. kuh m-pleks, kom-pleks; n. kompleks]

-adjective

1.

composed of many interconnected parts; compound; composite: a complex highway system.

2.

characterized by a very complicated or involved arrangement of parts, units, etc.: complex machinery.

3.

so complicated or intricate as to be hard to understand or deal with: a complex problem.

Source: Dictionary.com

Complexity, a **scientific theory** which asserts that some systems display behavioral phenomena that are completely inexplicable by any conventional analysis of the systems' constituent parts. These phenomena, commonly referred to as emergent behaviour, seem to occur in many complex systems involving living organisms, such as a stock market or the human brain.

Source: John L. Casti, Encyclopædia Britannica

Complexity

Behind each complex system there is a **network**, that defines the interactions between the components



Social, informational, technological, biological networks

The "Day of 7 Billion" has been targeted by the United States Census Bureau to be in July 2012. Wrong! It was in October 2011

The "Social Graph" behind Facebook

Keith Shepherd's "Sunday Best". http://baseballart.com/2010/07/shades-of-greatness-a-story-that-needed-to-be-told/



COLLABORATION NETWORKS: ACTOR NETWORK

Nodes: actors Links: cast jointly

IMDb Internet Movie Database



Days of Thunder (1990) Far and Away (1992) Eyes Wide Shut (1999)



N = 212,250 actors $\langle k \rangle$ =28.78

COLLABORATION NETWORKS: SCIENCE CO-AUTHORSHIP

Nodes: scientist (authors) **Links**: write paper together



STRUCTURE OF AN ORGANIZATION



BUSINESS TIES IN US BIOTECH-INDUSTRY



Financial

R&D

Information networks: the Web and Science Citation Indexes



* citation total may be skewed because of multiple authors with the same name

INTERNET









HUMANS GENES



HUMAN DISEASE NETWORK



Biological networks: Food Web

Nodes: species Links: trophic interactions



R. Sole (cond-mat/0011195)

R.J. Williams, N.D. Martinez Nature (2000)

Basic network measures

Degree of a node Distance between two nodes Clustering among three nodes

DEGREE DISTRIBUTION

Degree distribution P(k): probability that

a randomly chosen vertex has degree k

N_k = # nodes with degree k







DISTANCE IN A GRAPH



The *distance (shortest path, geodesic path)* between two nodes is defined as the **number of edges along the shortest path connecting them**.

*If the two nodes are disconnected, the distance is infinity.

In directed graphs each path needs to follow the direction of the arrows.

Thus in a digraph the distance from node A to B (on an AB path) is generally different from the distance from node B to A (on a BCA path).



Diameter: the maximum distance between any pair of nodes in the graph.

Average path length/distance for a connected graph (component) or a strongly connected (component of a) digraph.

where I_{ij} is the distance from node *i* to node j



In an undirected (symmetrical) graph $I_{ij} = I_{ji}$, we only need to count them once

$$< l > \equiv \frac{1}{L_{\max}} \sum_{i,j>i} l_{ij}$$

CLUSTERING COEFFICIENT

***** Clustering coefficient:

what portion of your neighbors are connected?

- * Node i with degree k_i
- * C_i in [0,1]





Random graphs

What are the expected basic measures emerging from random?

RANDOM NETWORK MODEL

Pául Erdös (1913-1996)





Erdös-Rényi model (1960)

Connect with probability p

p=<mark>1/6</mark> N=10 <k> ~ 1.5



RANDOM NETWORK MODEL



Definition: A **random graph** is a graph of N labeled nodes where each pair of nodes is connected by a preset probability **p**.

DEGREE DISTRIBUTION OF A RANDOM GRAPH



$$<\!k\!>=\!p(N\!-\!1) \qquad \qquad \sigma_{k}^{2} = p(1-p)(N\!-\!1)$$
$$\frac{\sigma_{k}}{<\!k\!>} = \left[\frac{1-p}{p}\frac{1}{(N\!-\!1)}\right]^{1/2} \approx \frac{1}{(N\!-\!1)^{1/2}}$$

As the network size increases, the distribution becomes increasingly narrow—we are increasingly confident that the degree of a node is in the vicinity of <k>.

WORLD WIDE WEB

Nodes: WWW documents Links: URL links

Over 3 billion documents

ROBOT: collects all URL's found in a document and follows them recursively





Degree distribution of the WWW





R. Albert, H. Jeong, A-L Barabasi, Nature, 401 130 (1999).

The difference between a power law and an exponential distribution



Above a certain x value, the power law is always higher than the exponential.

The difference between a power law and an exponential distribution

This difference is particularly obvious if we plot them on a log vertical scale: for large x there are orders of magnitude differences between the two functions.



Exponential vs Power law distributions







Size of Cities

After Bill enters the arena the average income of the public ~ USD 1,000,000



~ \$50 billion



DISTANCES IN RANDOM GRAPHS

Random graphs tend to have a tree-like topology with almost constant node degrees.



- nr. of first neighbors:
- nr. of second neighbors:
- •nr. of neighbours at distance d:
- estimate maximum distance:
- $N_{1} \cong \langle \mathbf{k} \rangle$ $N_{2} \cong \langle \mathbf{k} \rangle^{2}$ $N_{d} \cong \langle \mathbf{k} \rangle^{d}$
compare with real data

1 _	log N
t _{max} –	$\overline{\log\langle k \rangle}$

Network	Size	(k)	I	I _{rand}	с	Crand	Reference	Nr
www.cita.loval.updir	150107	25 21	21	2.25	0 1070	0.00022	Adamic 1000	1
www, site level, unui	105127	252.44	5.1	5.55	0.1076	0.00025	Adamic, 1999	2
internet, domain level	3015-6209	3.52-4.11	3.7-3.76	6.36-6.18	0.18-0.3	0.001	Pastor-Satorras et al., 2001	Z
Movie actors	225226	61	3.65	2.99	0.79	0.00027	Watts and Strogatz,1998	3
LANL co-authorship	52909	9.7	5.9	4.79	0.43	1.8 x 10 ⁻⁴	Newman, 2001a, 2001b, 2001c	4
MEDLINE eo-authorship	1520251	18.1	4.6	4.91	0.066	1.1 x 10 ⁻⁵	Newman, 2001a, 2001b, 2001c	5
SPIRES co-authorship	56627	173	4.0	2.12	0.726	0.003	Newman, 2001a, 2001b, 2001c	6
NCSTRL co-authorship	11994	3.59	9.7	7.34	0.496	3 x 10 ⁻⁴	Newman, 2001a, 2001b, 2001c	7
Math. co-authorship	70975	3.9	9.5	8.2	0.59	5.4 x 10 ⁻⁵	Barabasi et al, 2001	8
Neurosci. co-authorship	209293	11.5	6	5.01	0.76	5.5 x 10 ⁻⁵	Barabasi et al, 2001	9
E. coli, sustrate graph	282	7.35	2.9	3.04	0.32	0.026	Wagner and Fell, 2000	10
E. coli, reaction graph	315	28.3	2.62	1.98	0.59	0.09	Wagner and Fell, 2000	11
Ythan estuary food web	134	8.7	2.43	2.26	0.22	0.06	Montoya and Sole, 2000	12
Silwood Park food web	154	4.75	3.40	3.23	0.15	0.03	Montoya and Sole, 2000	13
Words, co-occurrence	460902	70.13	2.67	3.03	0.437	0.0001	Ferrer i Cancho and Sole, 2001	14
Words, synonyms	22311	13.48	4.5	3.84	0.7	0.0006	Yook et al. 2001b	15
Power grid	4941	2.67	18.7	12.4	0.08	0.005	Watts and Strogatz, 1998	16
C.Elegans	282	14	2.65	2.25	0.28	0.05	Watts and Strogatz, 1998	17
							0	

Given the huge differences in scope, size, and average degree, the agreement is excellent.

CLUSTERING COEFFICIENT

$$C_i \equiv \frac{2n_i}{k_i(k_i - 1)}$$

Since edges are independent and have the same probability *p*,

$$n_i \cong p \frac{k_i(k_i - 1)}{2} \quad \bigcirc \quad C \cong p = \frac{\langle k \rangle}{N}$$

The clustering coefficient of random graphs is small.

For fixed degree C decreases with the system size N.

CLUSTERING IN RANDOM GRAPHS

compare with real data

Network	Size	(k)	I	I _{rand}	С	Crand	Reference	Nr
www, site level, undir	153127	35.21	3.1	3.35	0.1078	0.00023	Adamic, 1999	1
Internet, domain level	3015-6209	3.52-4.11	3.7-3.76	6.36-6.18	0.18-0.3	0.001	Yook e al., 2001a, Pastor-Satorras et al., 2001	2
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Are real networks like random graphs? NO!

As quantitative data about real networks became available, we can compare their topology with the predictions of random graph theory.

Note that once we have N and <k> for a random network, from it we can derive every measurable property. Indeed, we have:

Average path length:

Clustering Coefficient:

 $< l_{rand} > \approx \frac{\log N}{\log k}$ $C_{rand} = p = \frac{\langle k \rangle}{N}$

Ę

Degree Distribution:

$$P_{rand}(k) \cong C_{N-1}^{k} p^{k} (1-p)^{N-1-k}$$

Models for «real» networks: small world





The Watts Strogatz Model: It takes a lot of randomness to ruin the clustering, but a very small amount to overcome locality *Where will the new node link to?* ER, WS models: choose randomly.

New nodes prefer to link to highly connected nodes (www, citations, IMDB).

PREFERENTIAL ATTACHMENT:

the probability that a node connects to a node with k links is proportional to k.





Barabási & Albert, Science 286, 509 (1999)

Empirical validation of social theories on big data

SIX DEGREES small worlds



Six Degrees (Stanley Milgram) Aberdeen

South

Dakota

North Platte

Lubbock

Midland

Rapid City

Scottsbluff

aramie

0.0

olorado

nta Fe e 📑

lew

aso

uahua

exico

Roswell

Artesia.

Fort Collins Sterling

gmont Denver

Colorado

Springs

Trois-Rivières Sherbrooke Ottawa_ Montréal Barne Peterborough Vermont

Val-D'Or

 Oshkosh Toronto Oshawa Kingston Michigan Sioux Falls La Crosse Madison New Kitchener Rochester Milwaukee Flint Hamp Buffalo New York Albany Mass Grand Hamilton Mass thuset Waterloo Sioux City Rockford Norfolk Rapids Lansing ODetroit Iowa Canton chicago. Cleveland Omaha Scranton Connecticut Rhode • Davenport • Joliet Nebraska Des Moines Rapids For Wayne Toledo Youngstown Peorla New York Pennsylvania Chio Akron 1 person Grand Lincom Pittsburgh York New Lersey Indiana Dayton Columbo Illinois

ault Ste

Sudbury

Marie

Springfield Indianapolis The Maryland 160 people sas city Philadelphia Cincinnati West Washington Columbia Delaware Lawrence Kansas Missouri St Louis Evansville Courselle Clexington Richmond District of • Wi hita Owensboro Kentucky Clarksville Johnson Roanoke Virginia Springfield Columbia

Clarksville City Suffolke e Virginia Fayetteville Tulsa Knoxville North Beach Memphis Jackson Chattanooga Ashevile Oklahoma Fort Smith Amarillo Carolina Greenville Norman Arkansas Albuquerque Greenvilleo Charlotte Jacksonville Lawton O Huntsville Wichita Pine Bluffz

Atlanta South Augusta Carolina Wilmington Birmingham Falls Mississippi Denton Charleston Alabama Monroe Jackson Georgia Savannah Abilene 0 Dallas Tyler Shreveport Albany Waco Montgomery, Hattiesburg San Angelo Texas Killeen Bryan Mobile --- Dothan Lake -Charles Louisiana Beaumont New (Gulfport o Jacksonville Austin • Pensacola Tallahassee Gainesville Beach Daytona

Minneapolis . Esu Claire Waysau

Rochester

Wisconsin

San Antonio Houston Orleans Galveston Riedras Negras Victoria Corpus Christi Laredo

Reynosa Monterrey 0 Brownsville

Gulf of AMexispdi reti sociali - Aprile 2011 Miami

Spring Hill Ocala

Tampa P Florida

Sarasota Port St

Cape Coral Luce Lauderdale

Fort

The Bahamas

Stanley Milgram

Rivière-Du-Loup Québec

O

Maine

N

Brun

Munic



The Small-world experiment

- 64 chains completed:
 - 6.2 on the average, thus "6 degrees of separation"
- Further observations:



People from the Boston area have even closer paths: 4.4



IM communication network

Buddy graph

- 240 million people (people that login in June '06)
- 9.1 billion buddy edges (friendship links)
- <u>Communication graph</u> (take only 2-user conversations)
 - Edge if the users exchanged at least 1 message
 - 180 million people
 - 1.3 billion edges
 - 30 billion conversations



The strength of weak ties

- Mark S. Granovetter, 1973
- His PhD thesis: how people get to know about new jobs?
- Through personal contacts
- Surprise: often acquaintances, **not** close friends



The Strength of Weak Ties

Mark S. Granovetter

American Journal of Sociology, Volume 78, Issue 6 (May, 1973), 1360-1380.





Tie strength in real data

- For many years the Granovetter's theory was not tested
- But, today we have large who-talks-to-whom graphs:
 - Email, Messenger, Cell phones, Facebook
- Onnela et al. 2007:
 - Cell-phone network of 20% of country's population

Country-wide mobile phone data





Social proximity and tie strength

- How connected are u and v in the social network.
 - Various well-established measures of network proximity, based on the common neighbors (Jaccard, Adamic-Adar) or the structure of the paths (Katz) connecting u and v in the who-calls-whom network.
- How intense is the interaction between u and v.
 - Number of calls as strength of tie

Neighborhood Overlap

- Overlap: $O_{ij} = \underline{n(i)} \cap \underline{n(j)}$ $n(i) \cup n(j)$ • $n(i) \dots$ set of
 - neighbors of A
- Overlap = 0 when an edge is a local bridge



Strength of weak ties

- Large scale empirical validation of Granovetter's theory
 - Social proximity increases with tie strength
 - Weak ties span across different communities
- J.-P. Onnela, J. Saramaki, J. Hyvonen, G. Szabo, D. Lazer, K. Kaski, J. Kertesz, A.-L. Barabási. Structure and tie strengths in mobile communication networks. PNAS 104 (18), 7332-7336 (2007).





Human mobility, social ties and link prediction

Dashun Wang, Dino Pedreschi, Chaoming Song, Fosca Giannotti, Albert-Lászlo Barabási

SIGKDD Int. Conf. on Knowledge Discovery and Data Mining – KDD 2011

Colocation, social proximity, tie strength

- How similar is the movement of users u and v
 - Various co-location measures, quantifying the similarity between the movement routines of u and v (mobile homophily)
- How connected are u and v in the social network.
 - Various well-established measures of network proximity, based on the common neighbors (Jaccard, Adamic-Adar) or the structure of the paths (Katz) connecting u and v in the who-calls-whom network.
- How intense is the interaction between u and v.
 - Number of calls as strength of tie

mobility dimension of the "strength of weak ties"



- co-location, network proximity and tie strength strongly correlate with each other
- measured on 3 months of calls, 6 Million users, nation-wide (large European country)





The strength of weak ties ...

• For information **diffusion** (**spreading** of news and rumors on a social network)



The weakness of weak ties

Diffusion of innovation / adoption



Figure 19.10: The years of first awareness and first adoption for hybrid seed corn in the Ryan-Gross study. (Image from [358].)

The strength of the strong ties for the







Diffusion in Viral Marketing

 Senders and followers of recommendations receive discounts on products



- Data: Incentivized Viral Marketing program
 - 16 million recommendations
 - 4 million people, 500k products

[Leskovec et al., TWEB '07]

Adoption Curve: Validation



Social network mining 1: link prediction

Which new links will appear in the social network?

Link prediction in social networks



Potential links with common neighbors

Unsupervised precision

Katz	9.1%
Adamic-Adar	7.8%
SCos	5.6%
Weighted SCos	5.6%
Extra-role <i>CoL</i>	5.1%
Weighted CoL	5.1%
CN	5.1%
CoL	5.0%
Jaccard	3.0%

	Pred. class=0	Pred. class=1
actual class=0	6,627	82
actual class=1	117	228

Classification

decision-tree: *AA*>0.5 and *SCoL*>0.7 73.5% precision and 66.1% recall

Combining topology and mobility measures is the key to achieving high precision and recall.

People is predictable!

Probability of a new link between two (disconnected) random users:

10-6

• Best prediction accuracy using only social features:

10%

• Best prediction accuracy using **social + mobility** features:

75%

A small detour on human predicatibility


To what degree is human motion predictable?

Predictability

0%

Random walk models (RW, LF, CTRW)

100% Periodic motion

Entropy of human trajectories

Recorded Trajectory



 $-\sum_{T'_i \subset T_i} P(T'_i) \log_2[P(T'_i)]$

Entropy Distribution Across the Population



 $S = 0.8 \rightarrow$ the real uncertainty in the user's whereabouts is $2^{0.8} = 1.74$. $S \in [0, S^{max}], S^{max} = \log_2 N$

Daily routines are highly predictable

□ A potential **93%** average predictability in user mobility.

□ Lack of variability in predictability across the population.

Tiny dependence on demographic and external parameters

Song, Qu, Blumm, Barabasi, Science 327,108(2010)

Social network mining 2: community discovery

How to highlight the modular structure of a network?



Communities

Communities







Are these two different networks?



No!



DEMON Algorithm

- For each node X:
 - Extract the Ego Network of X
 - Remove X from the Ego Network
 - Discover communities in the Ego Network (easy)
 - Put back X into each discovered community C
- Then, merge the discovered communities bottom-up
 - Coscia, Giannotti, Pedreschi, Rossetti. KDD 2012

Community discovery

- Challenging task
- Many competing approaches
- Huge literature
- A recent survey:
 - Michele Coscia, Fosca Giannotti, Dino Pedreschi: A classification for community discovery methods in complex networks. *Statistical Analysis and Data Mining* 4(5): 512-546 (2011)

[Girvan-Newman PNAS 'oz]

Method 1: Girvan-Newman

 Divisive hierarchical clustering based on the notion of edge betweenness:

Number of shortest paths passing through the edge

- Remove edges in decreasing betweenness
- Example:





120 cuts

500 cuts

Textbooks and course-ware

Books

- David Easley, Jon Kleinberg: Networks, Crowds, and Markets.
 <u>http://www.cs.cornell.edu/home/kleinber/networks-book/</u>
- M. E. J. Newman: The structure and function of complex networks, *SIAM Review*, Vol. 45, p. 167-256, 2003.

http://didawiki.cli.di.unipi.it/lib/exe/fetch.php/wma/ newman_2003.pdf

• A.-L. Barabasi. *Linked*. Plume, 2002

Courses

- Pedreschi + Giannotti @ University of Pisa
 - <u>http://didawiki.cli.di.unipi.it/doku.php/wma/start</u>
- Barabasi @ Northeastern University
 - <u>http://barabasilab.neu.edu/courses/phys5116/</u>
- Leskovec @ Stanford University
 - <u>http://www.stanford.edu/class/cs224w/handouts.</u>
 <u>html</u>
- Slides from this course are freely adapted from those of Laszlo Barabasi, Jure Leskovec, Fosca Giannotti, besides my own. Thanks!

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