# DATA MINING 2 (Deep) Neural Networks

Riccardo Guidotti

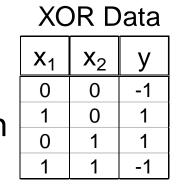
a.a. 2023/2024

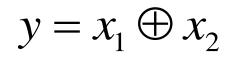
Slides edited from a set of slides titled "Introduction to Machine Learning and Neural Networks" by Davide Bacciu

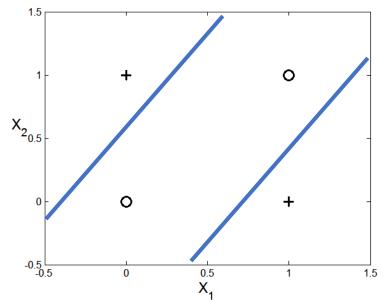


# Nonlinearly Separable Data

- Since f(w,x) is a linear combination of input variables, decision boundary is linear.
- For nonlinearly separable problems, the perceptron fails because no linear hyperplane can separate the data perfectly.
- An example of nonlinearly separable data is the XOR function.







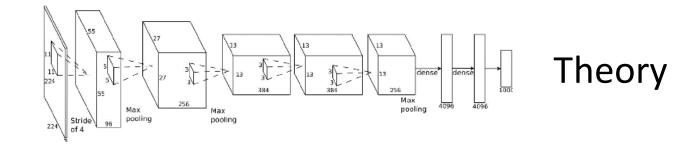
# Why Now?



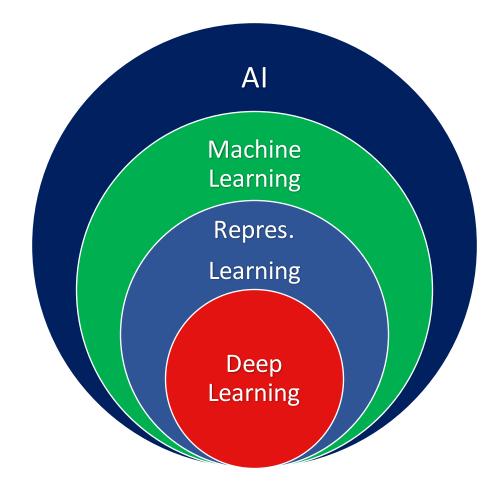
#### (Big) Data



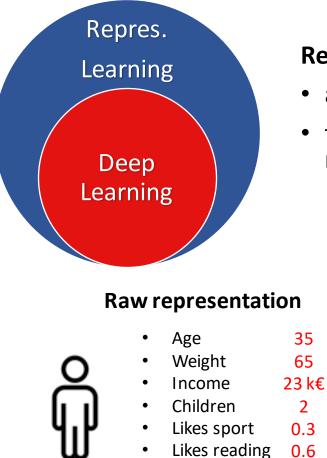
GPU



### A quick look on Deep Learning



# Deep learning



- **Representation learning** methods that
- allow a machine to be fed with raw data and
- to automatically discover the representations needed for detection or classification.

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f(x)

**Raw representation** 

Likes reading

•••

Education high

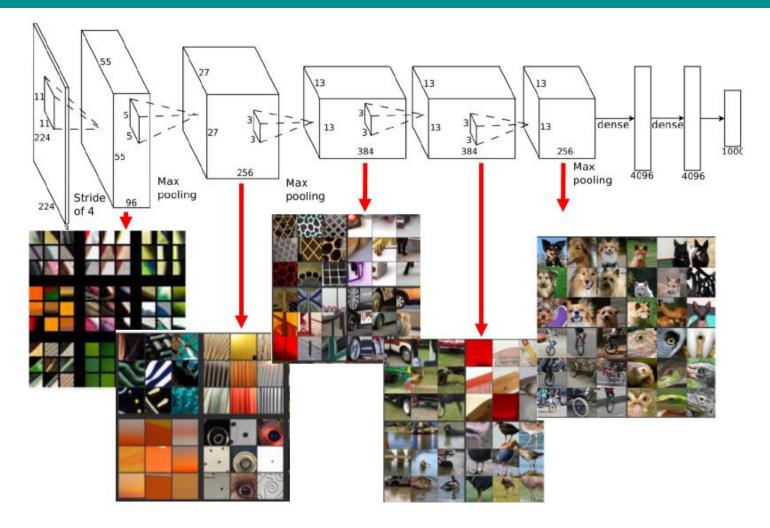
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#### **Higher-level representation**

- 0.9 Young parent
- Fit sportsman 0.1
- High-educated reader 0.8
- Rich obese 0.0

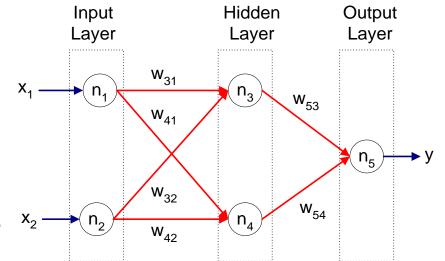
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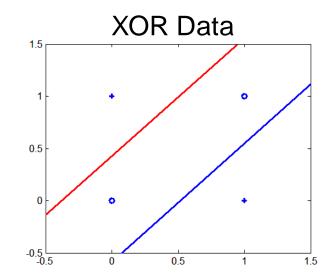
### **Multiple Levels Of Abstraction**



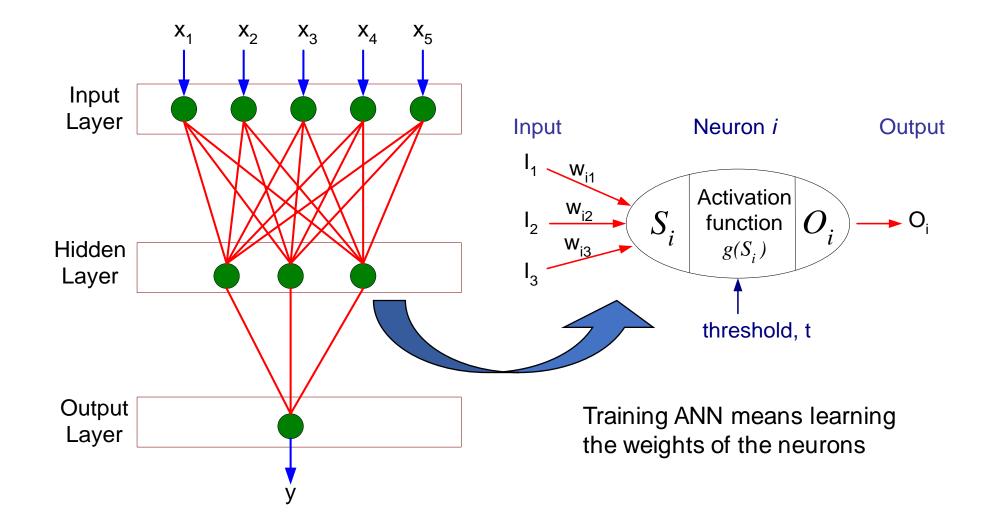
# Multilayer Neural Network

- Hidden Layers: intermediary layers between input and output layers.
- More general **activation functions** (sigmoid, linear, hyperbolic tangent, etc.).
- Multi-layer neural network can solve any type of classification task involving nonlinear decision surfaces.
- Perceptron is single layer.
- We can think to each hidden node as a perceptron that tries to construct one hyperplane, while the output node combines the results to return the decision boundary.





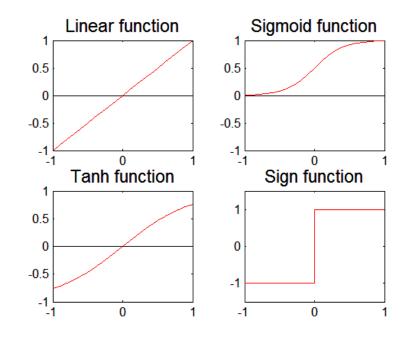
### General Structure of ANN



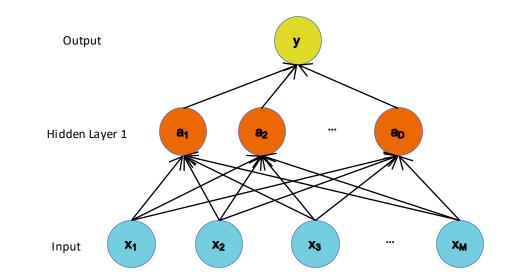
# Artificial Neural Networks (ANN)

- Various types of neural network topology
  - single-layered network (perceptron) versus multi-layered network
  - Feed-forward versus recurrent network
- Various types of activation functions (f)

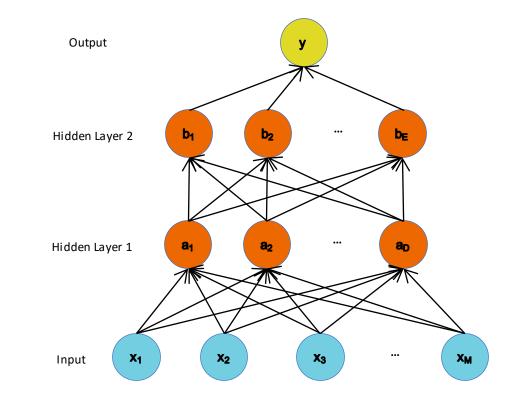
$$Y = f(\sum_{i} w_i X_i)$$



### **Deep Neural Networks**

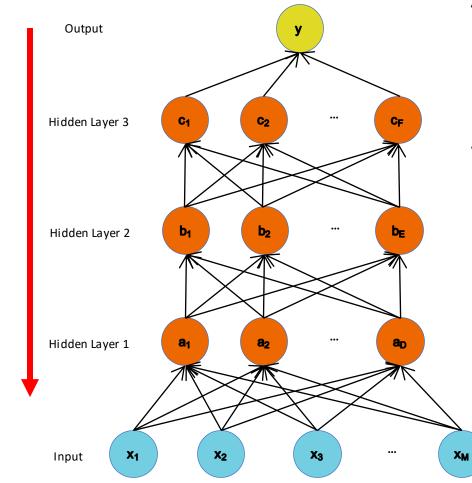


### **Deep Neural Networks**



### **Deep Neural Networks**

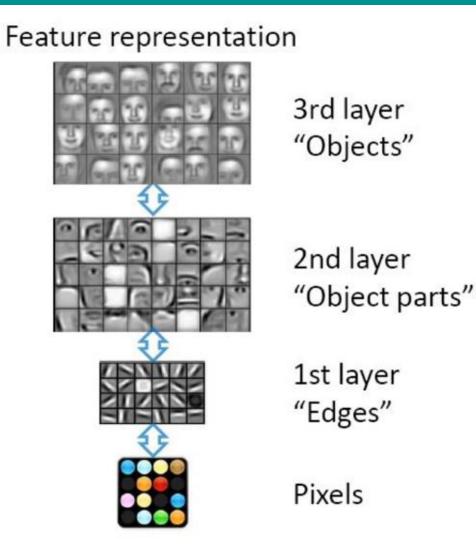
Backpropagation through many layers has numerical problems that makes learning not-straightforward (Gradient Vanish/Explosion)



Actually deep learning is way more than having neural networks with a lot of layers

# **Representation Learning**

- We don't know the "right" levels of abstraction of information that is good for the machine
- So let the model figure it out!

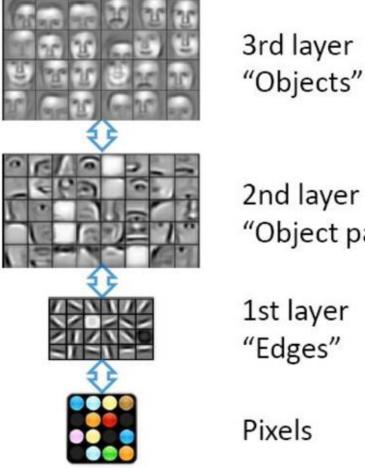


# **Representation Learning**

#### **Face Recognition:**

- Deep Network can build up increasingly higher levels of abstraction
- Lines, parts, regions

Feature representation

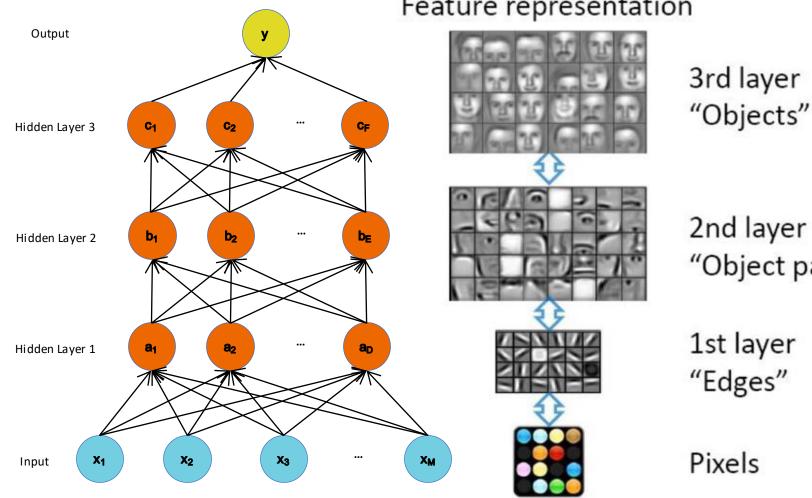


2nd layer "Object parts"

1st layer "Edges"

Example from Honglak Lee (NIPS 2010)

# **Representation Learning**



Feature representation

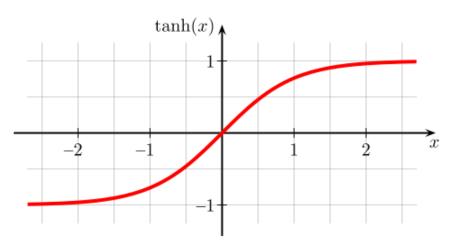
2nd layer "Object parts"

1st layer "Edges"

Example from Honglak Lee (NIPS 2010)

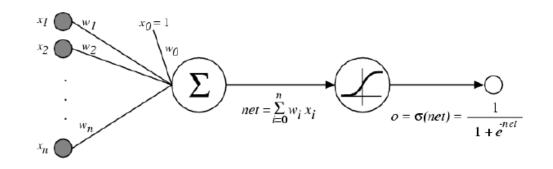
# **Activation Functions**

- A new change: modifying the nonlinearity
  - The logistic is not widely used in modern ANNs

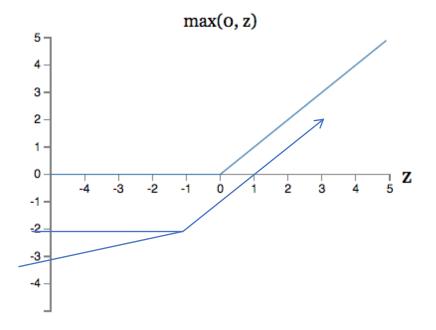


Alternative 1: tanh

Like logistic function but shifted to range [-1, +1]



### **Activation Functions**



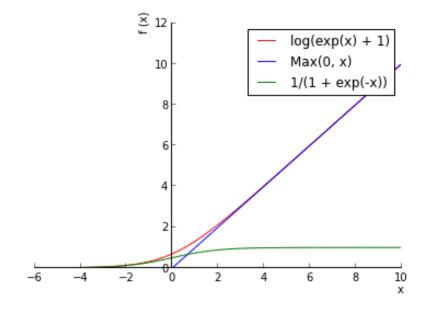
Alternative 2: rectified linear unit

Linear with a cutoff at zero

(Implementation: clip the gradient when you pass zero)

 $\max(0, w \cdot x + b).$ 

### **Activation Functions**

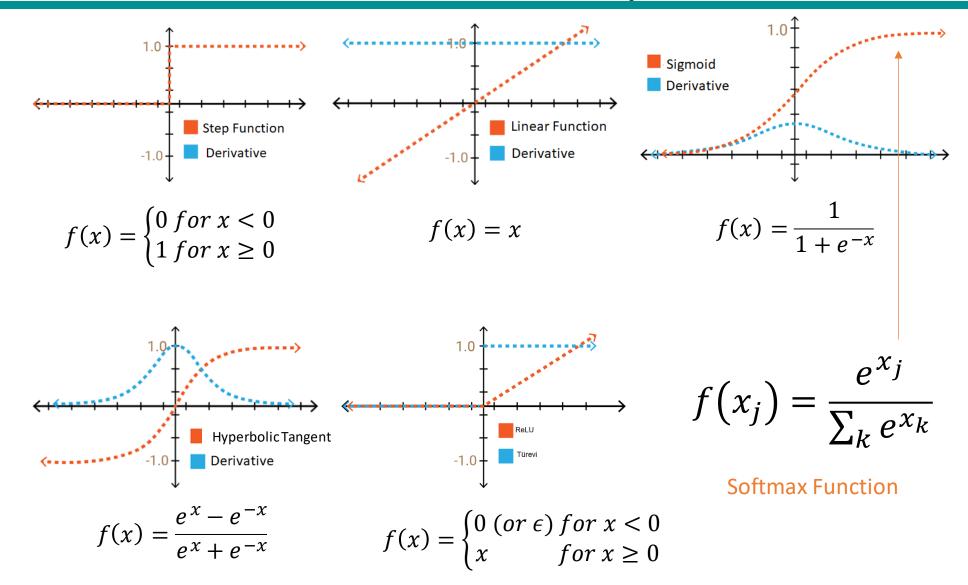


#### Alternative 3: soft exponential linear unit

Soft version: log(exp(x)+1)

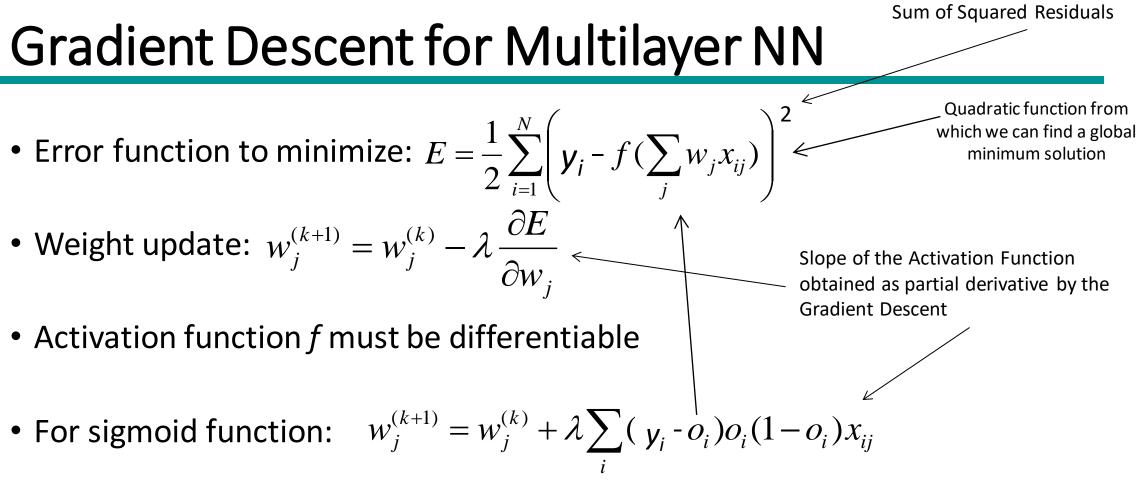
Doesn't saturate (at one end) Sparsifies outputs Helps with vanishing gradient

### **Activation Functions Summary**



# Learning Multi-layer Neural Network

- Can we apply perceptron learning to each node, including hidden nodes?
- Perceptron computes error e = y f(w, x) and updates weights accordingly
- Problem: how to determine the true value of y for hidden nodes?
- Approximate error in hidden nodes by error in the output nodes
- Problems:
  - Not clear how adjustment in the hidden nodes affect overall error
  - No guarantee of convergence to optimal solution

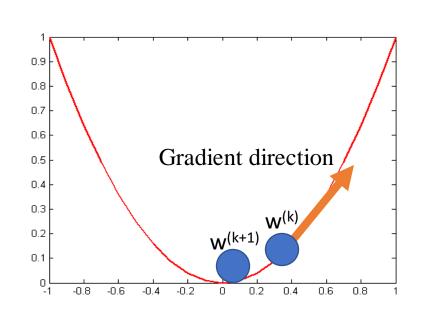


Step Size

• Stochastic Gradient Descent (update the weight immediately)

# **Gradient Descent for Multilayer NN**

- Weights are updated in the opposite direction of the gradient of the loss function.
- Gradient direction is the direction of uphill of the error function.
- By taking the negative we are going downhill.
- Hopefully to a minimum of the error.

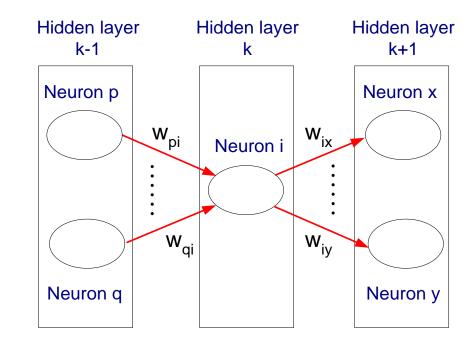


 $w_{j}^{(k+1)} = w_{j}^{(k)} - \lambda \frac{\partial E}{\partial w_{j}}$ 

# Gradient Descent for Multilayer NN

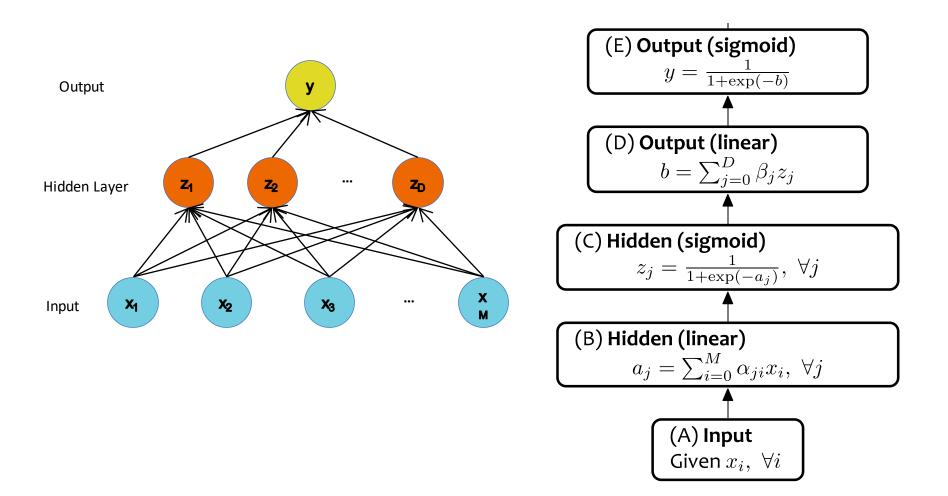
- For output neurons, weight update formula is the same as before (gradient descent for perceptron)
- For hidden neurons:

$$w_{pi}^{(k+1)} = w_{pi}^{(k)} + \lambda o_i (1 - o_i) \sum_{j \in \Phi_i} \delta_j w_{ij} x_{pi}$$
  
Output neurons  $: \delta_j = o_j (1 - o_j) (t_j - o_j)$   
Hidden neurons  $: \delta_j = o_j (1 - o_j) \sum_{k \in \Phi_j} \delta_k w_{jk}$ 

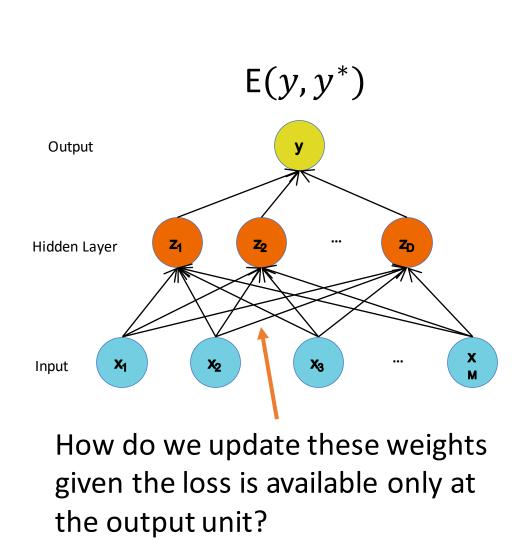


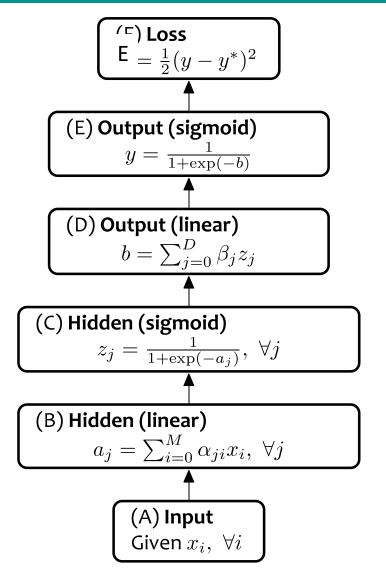
o: output of the networkt: target value (ground truth)

### **Training Multilayer NN**

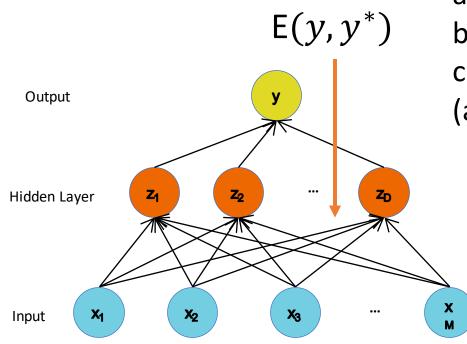


### **Training Multilayer NN**





### **Error Backpropagation**



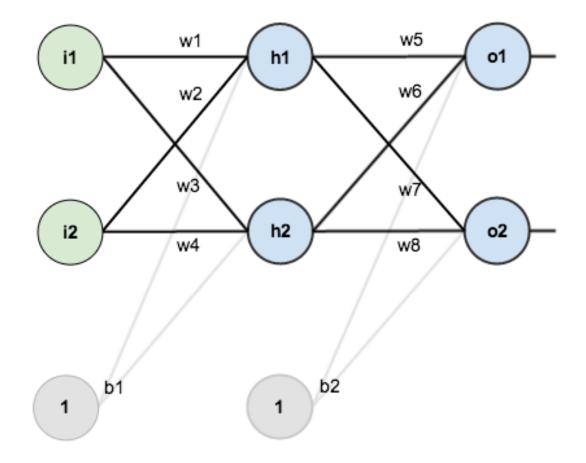
Error is computed at the output and propagated back to the input by chain rule to compute the contribution of each weight (a.k.a. derivative) to the loss

#### A 2-step process

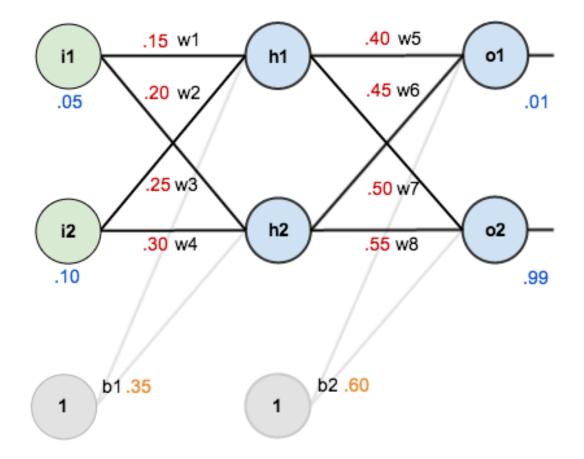
- 1. Forward pass Compute the network output
- 2. Backward pass Compute the loss function gradients and update

https://mattmazur.com/2015/03/17/a-step-by-step-backpropagation-example/

### Error Backpropagation - Example

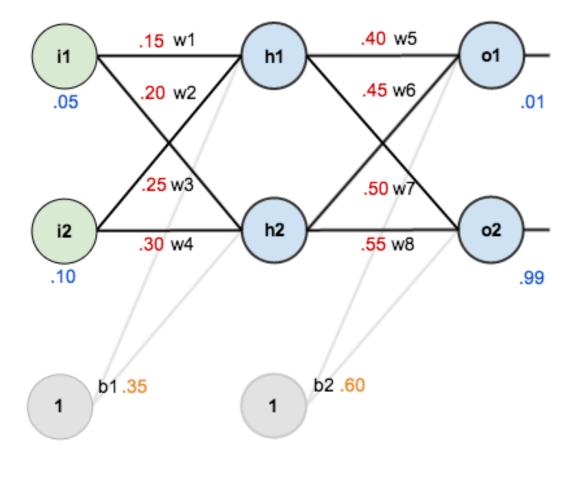


### **Error Backpropagation - Example**

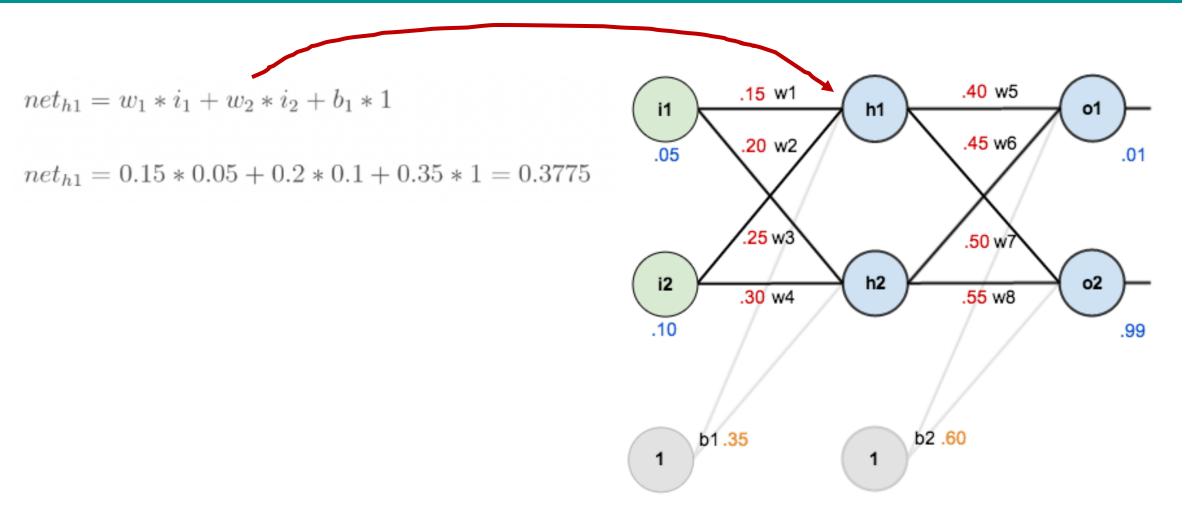


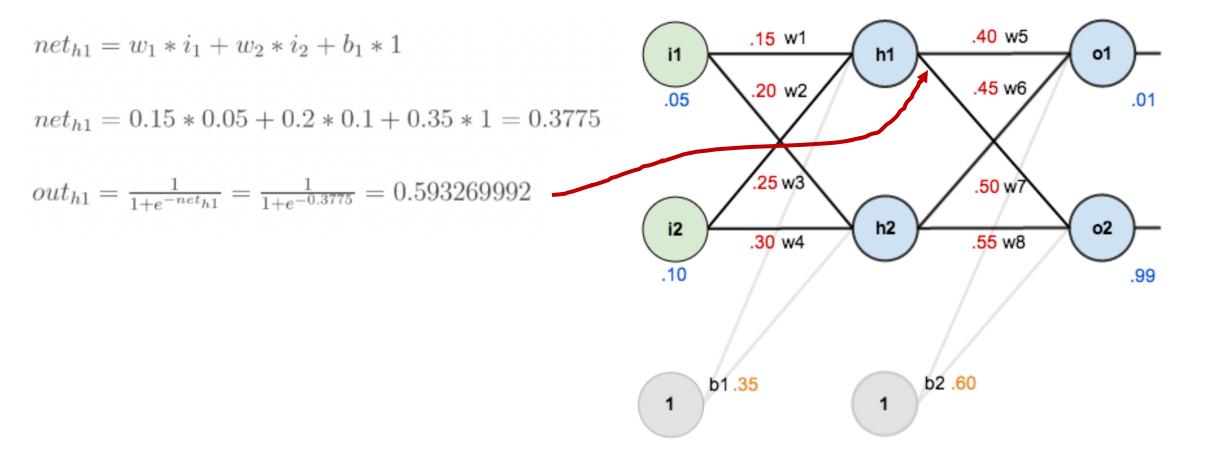
The goal of backpropagation is to optimize the weights so that the neural network can learn how to correctly map arbitrary inputs to outputs.

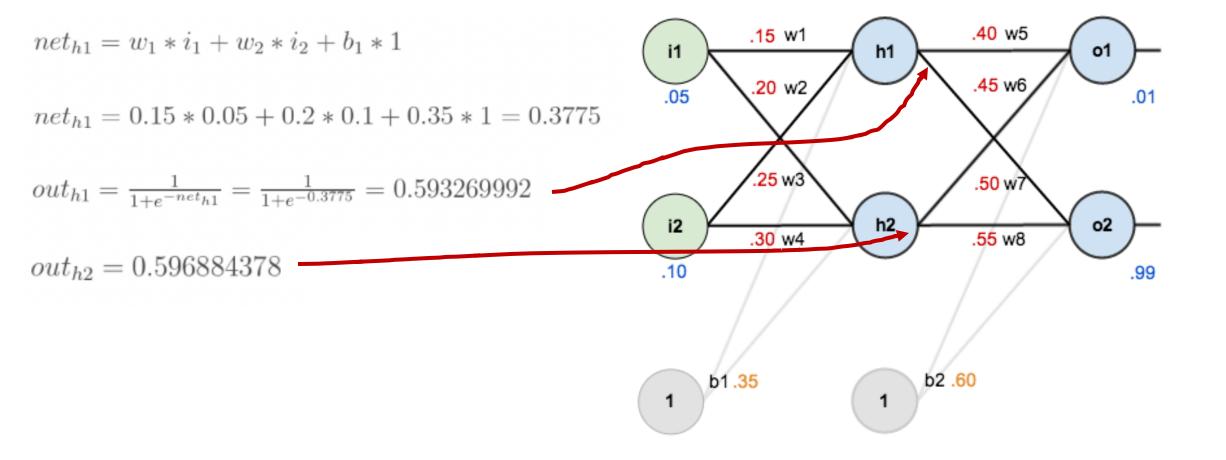
### **Error Backpropagation - Example**

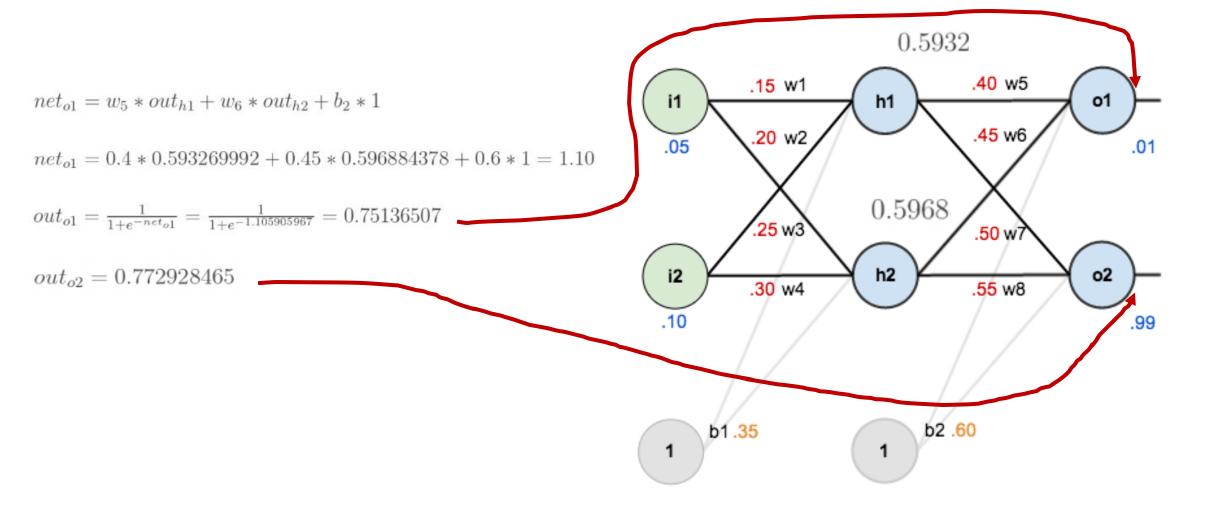


- initial weights
- biases
- training inputs/outputs
- activation:logistic

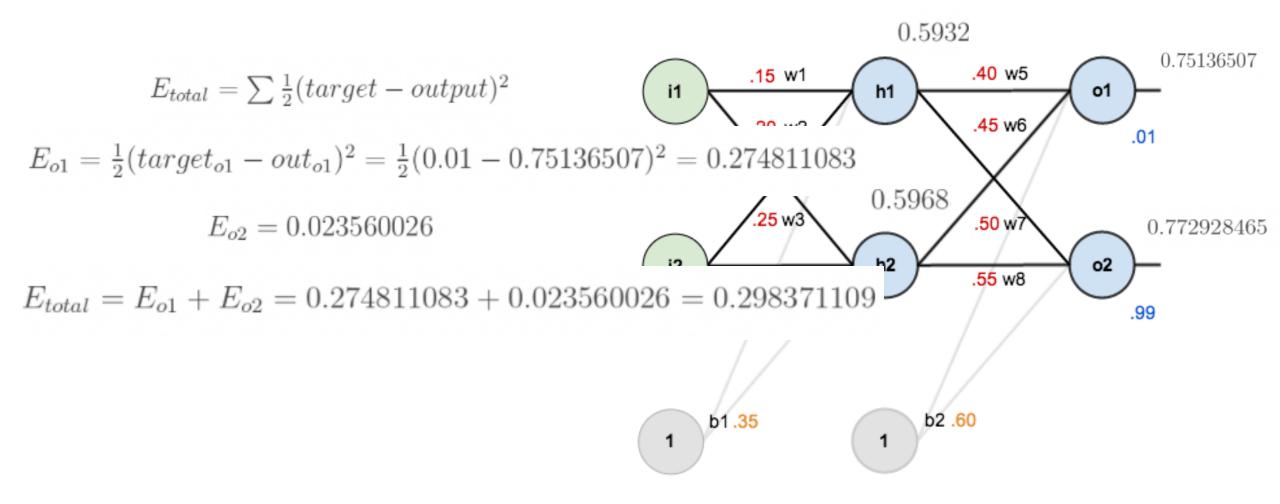






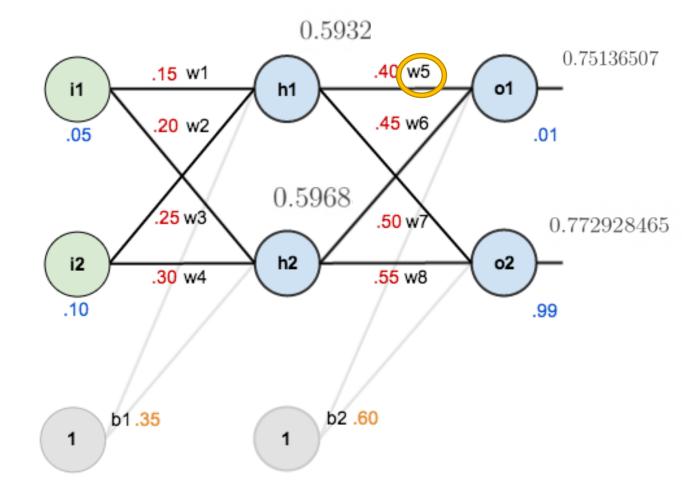


### Example – Calculating the Total Error

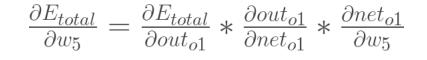


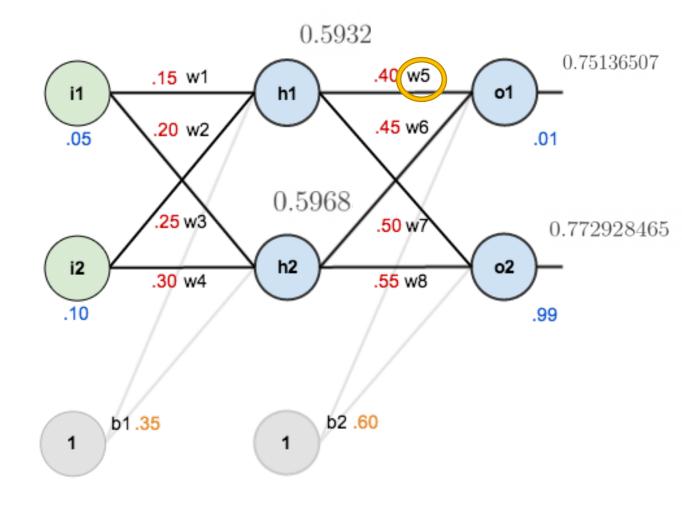
# Example - The Backward Pass -

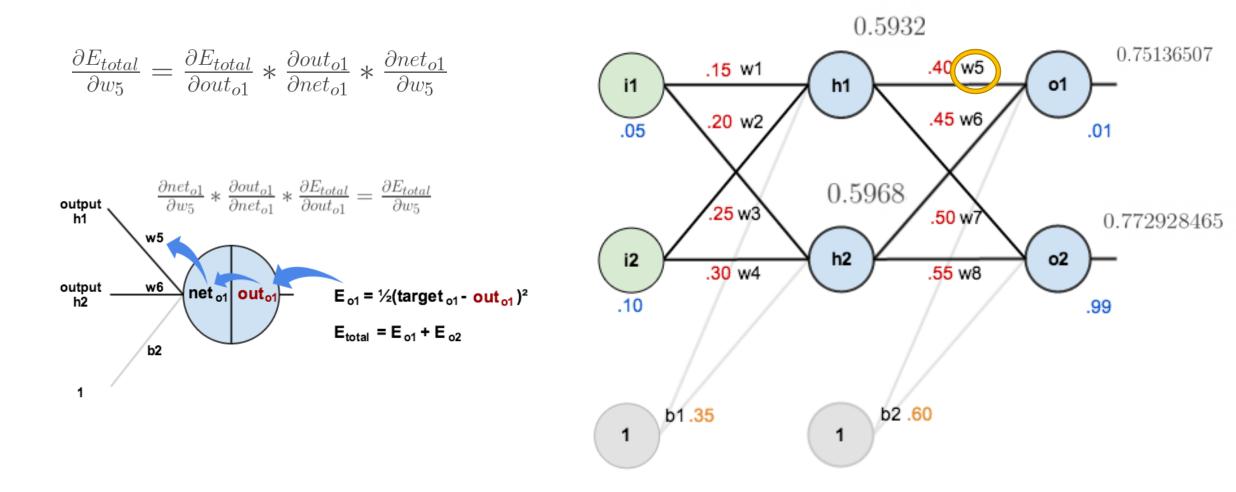
How much a change in w5 affects the total error?

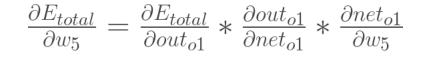


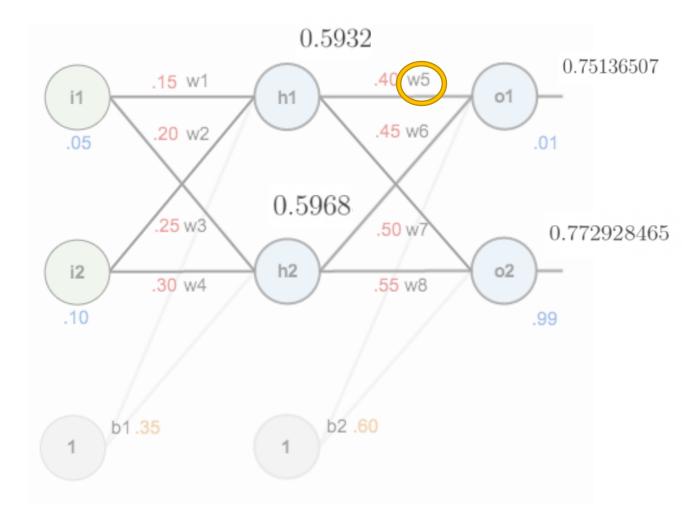
### Example - The Backward Pass ←

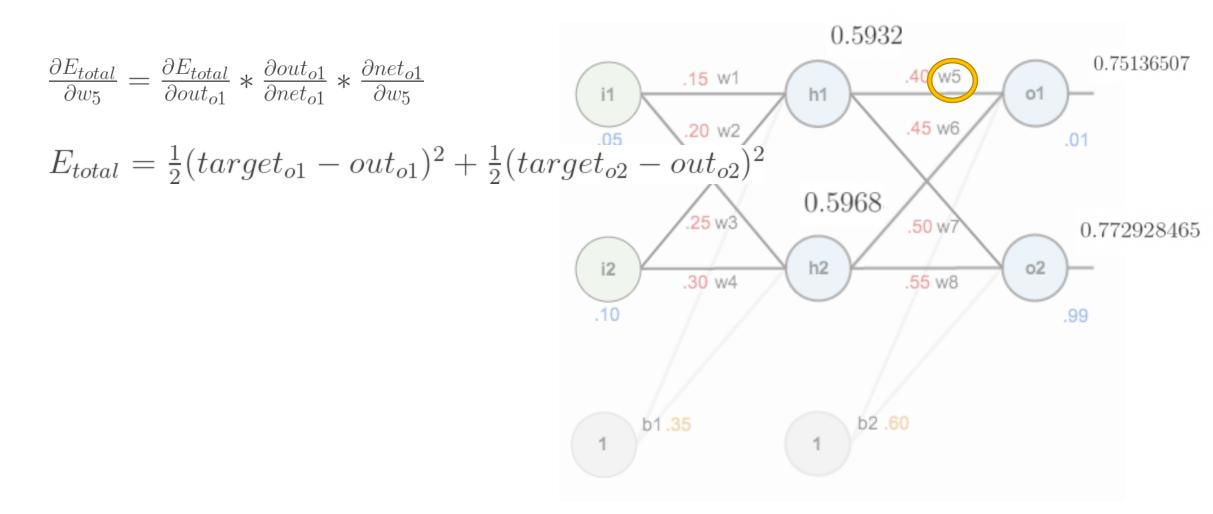


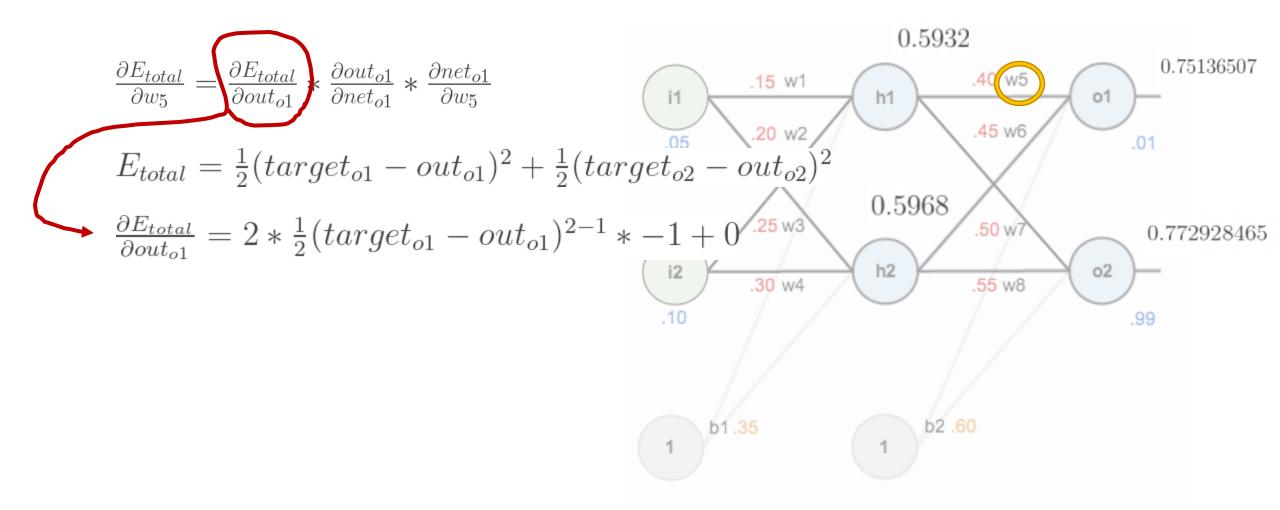


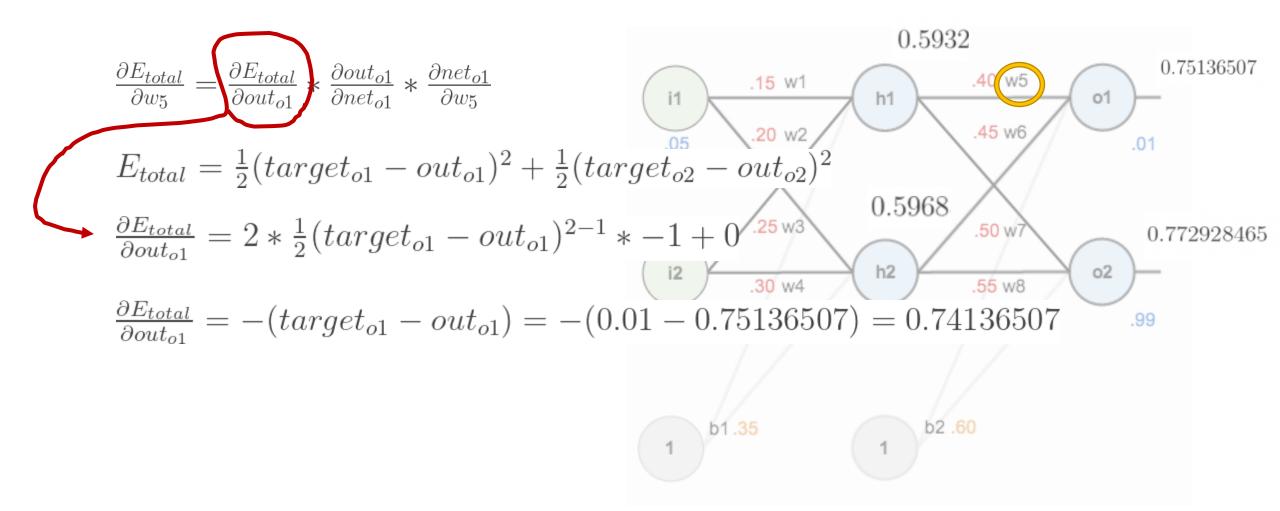


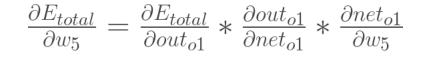


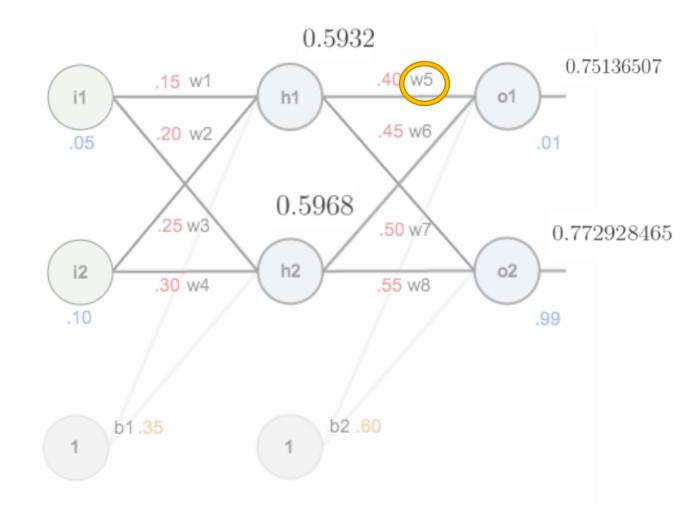






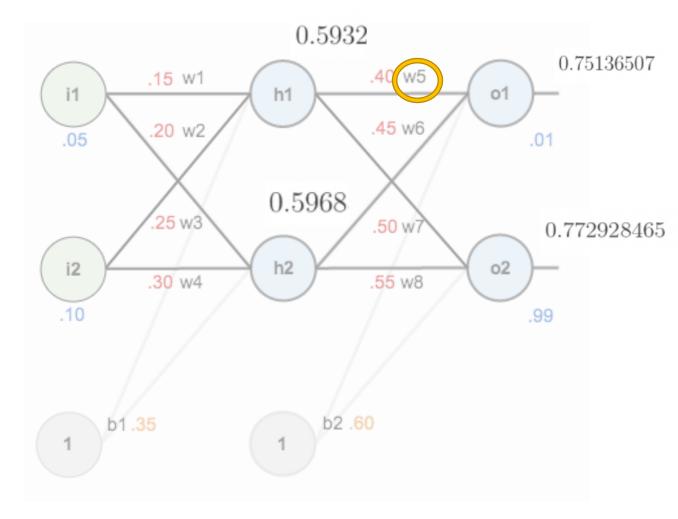




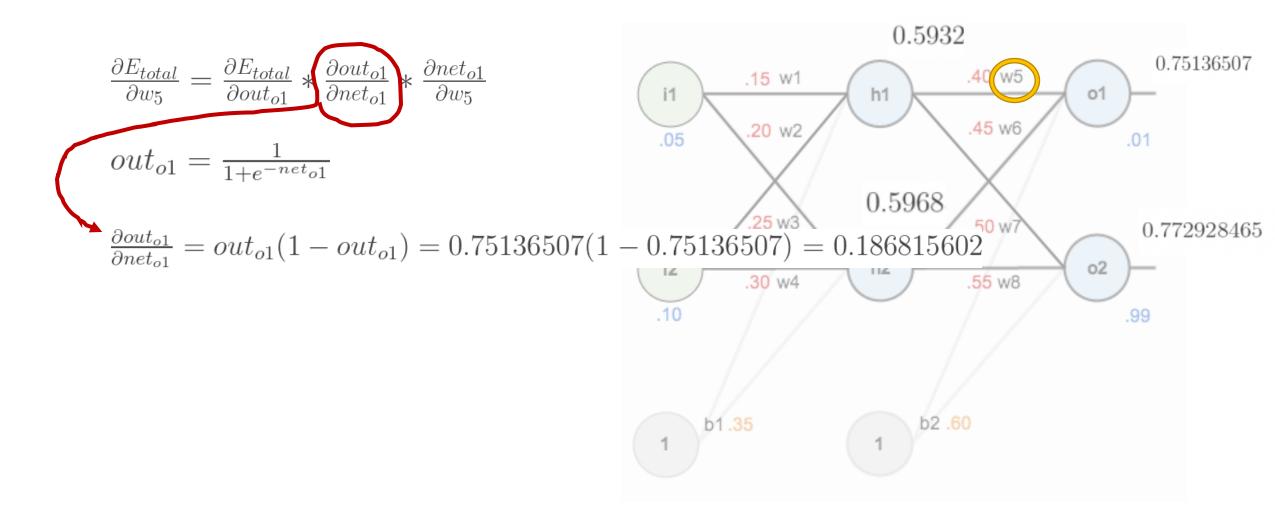


how much does the output o1 change with respect to its total net input?

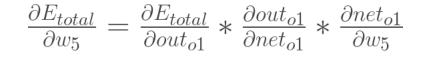
$$\frac{\partial E_{total}}{\partial w_5} = \frac{\partial E_{total}}{\partial out_{o1}} * \frac{\partial out_{o1}}{\partial net_{o1}} * \frac{\partial net_{o1}}{\partial w_5}$$
$$out_{o1} = \frac{1}{1 + e^{-net_{o1}}}$$

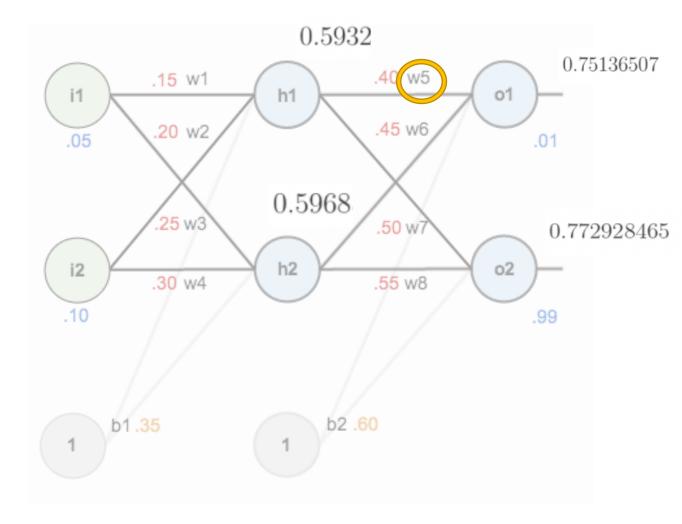


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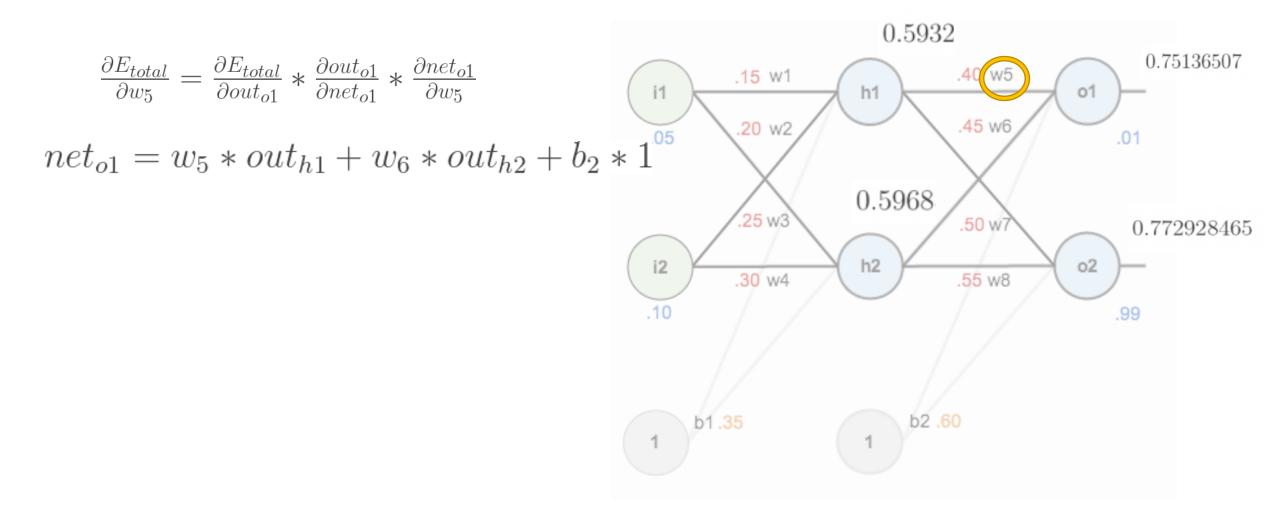


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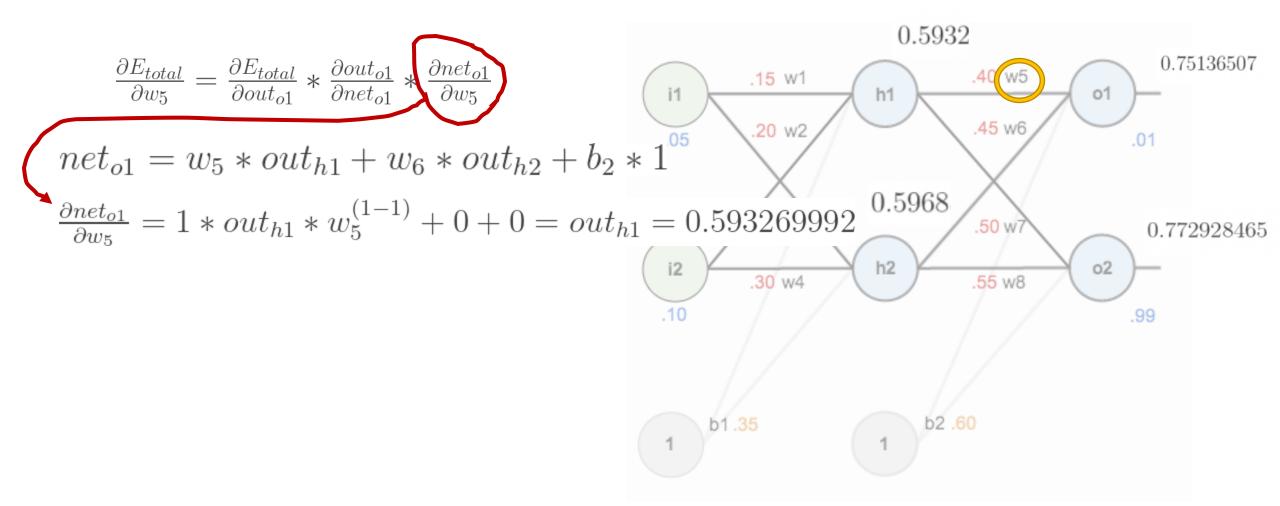




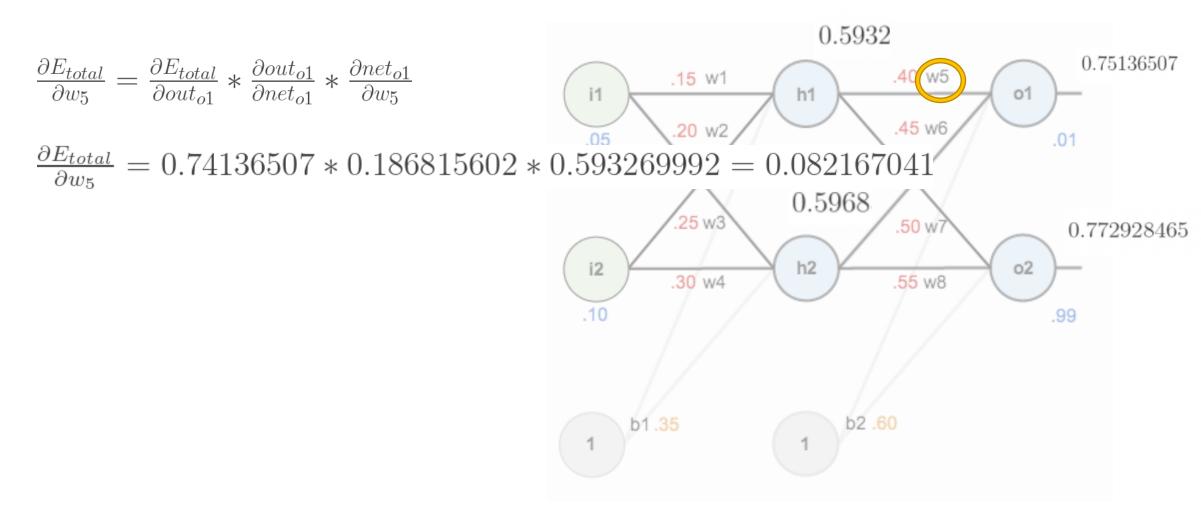
how much does the total net input of o1 change with respect to w5?



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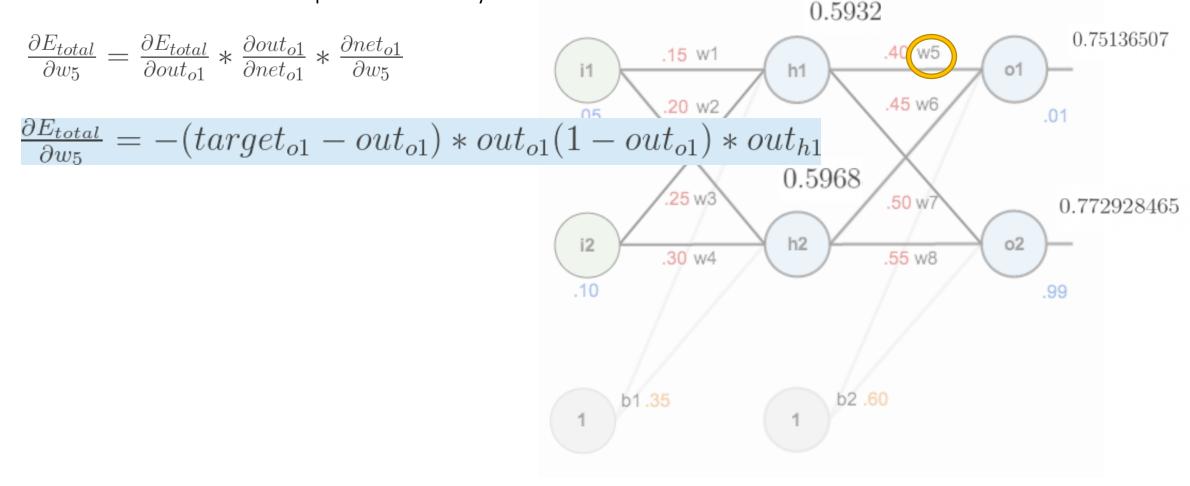


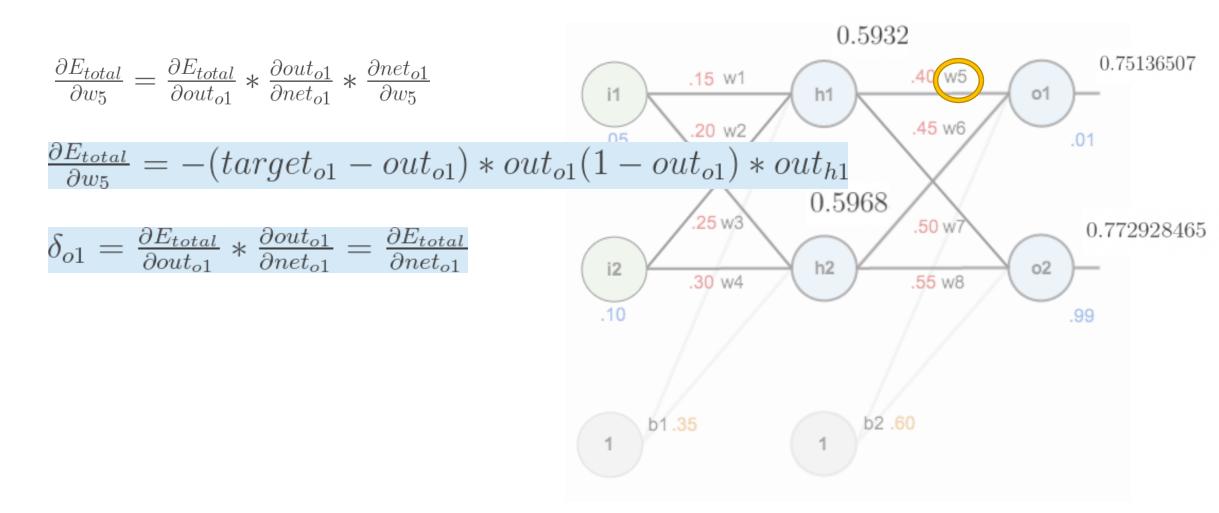
how much does the total net input of o1 change with respect to w5?



Put everything together

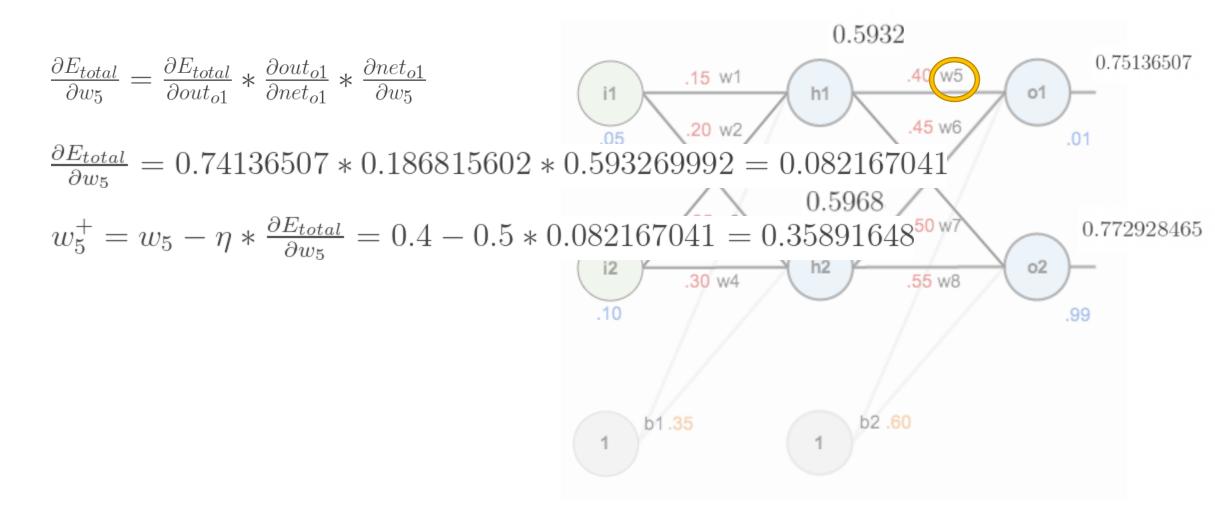
Slope of the Activation Function obtained as partial derivative by the Gradient Descent



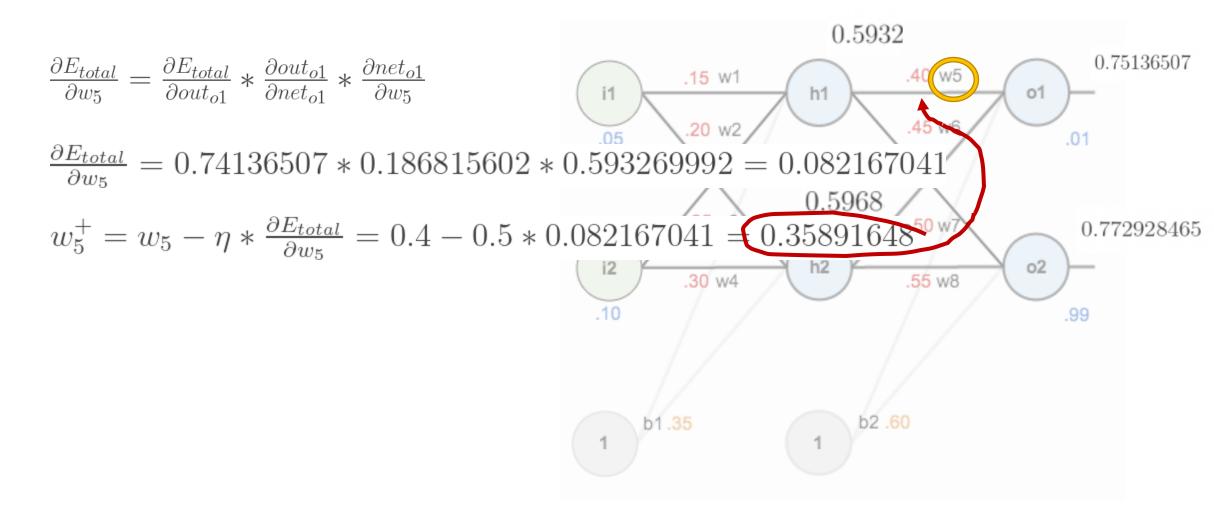


$$\frac{\partial E_{total}}{\partial w_{5}} = \frac{\partial E_{total}}{\partial out_{o1}} * \frac{\partial net_{o1}}{\partial met_{o1}} * \frac{\partial net_{o1}}{\partial w_{5}} \qquad (1 \\ 0.5932 \\ 0.5932 \\ 0.5932 \\ 0.75136507 \\ 0.752928465 \\ 0.75292845 \\ 0.75292845 \\ 0.75292845 \\ 0.75292845 \\$$

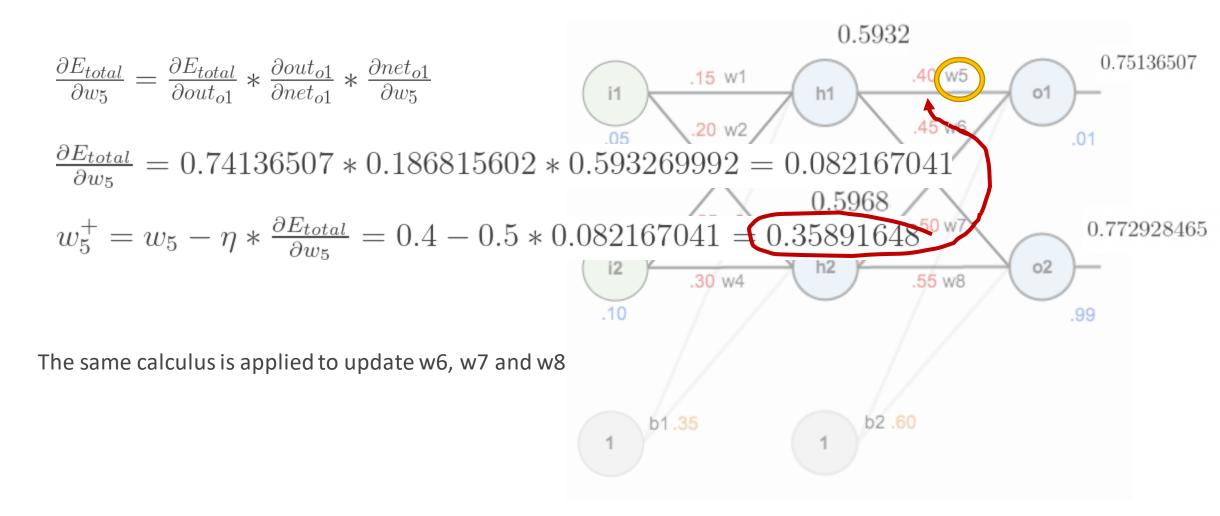
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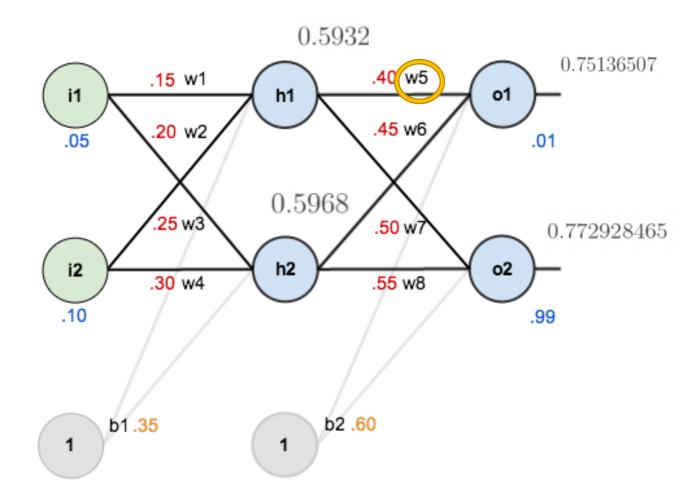


Apply the step size to update w5.

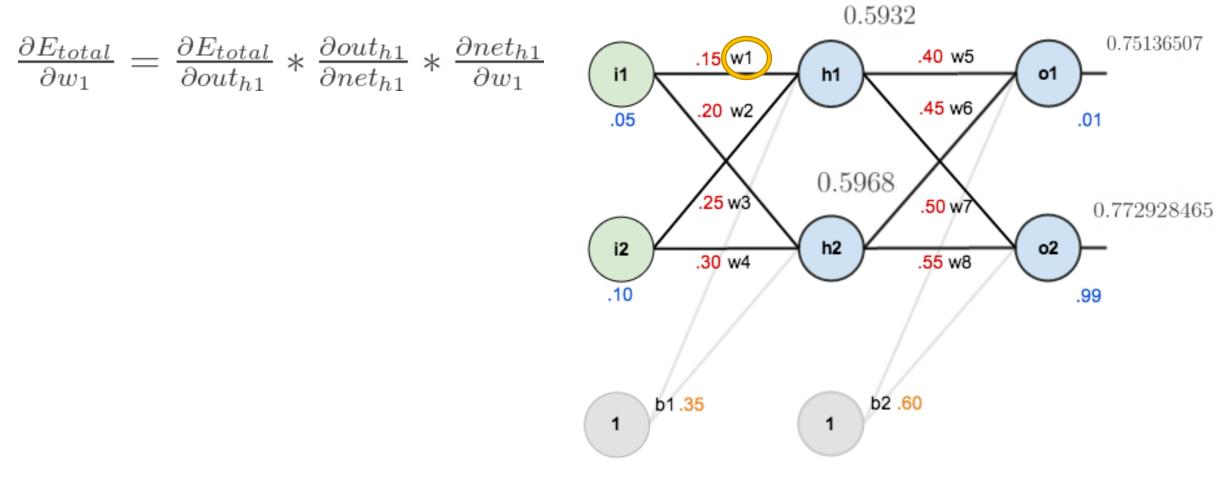


Apply the step size to update w5.

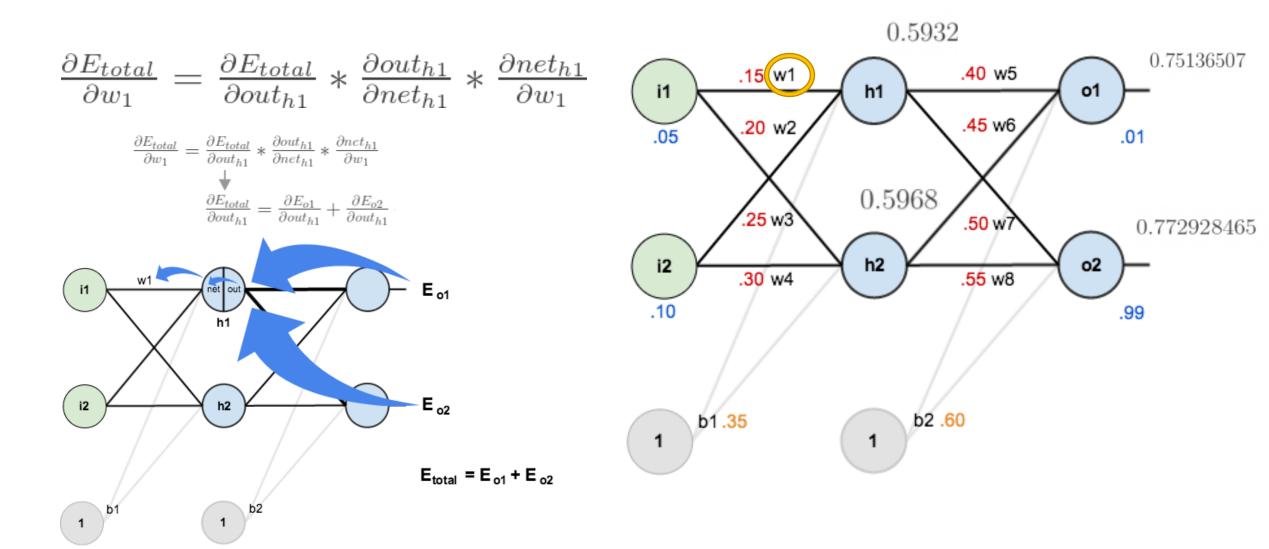


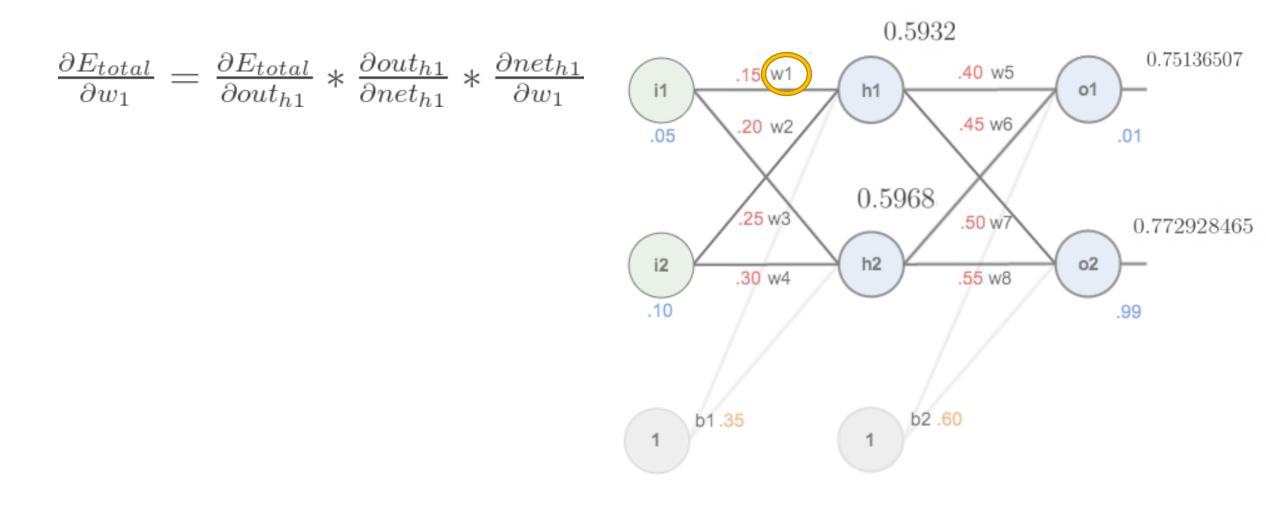


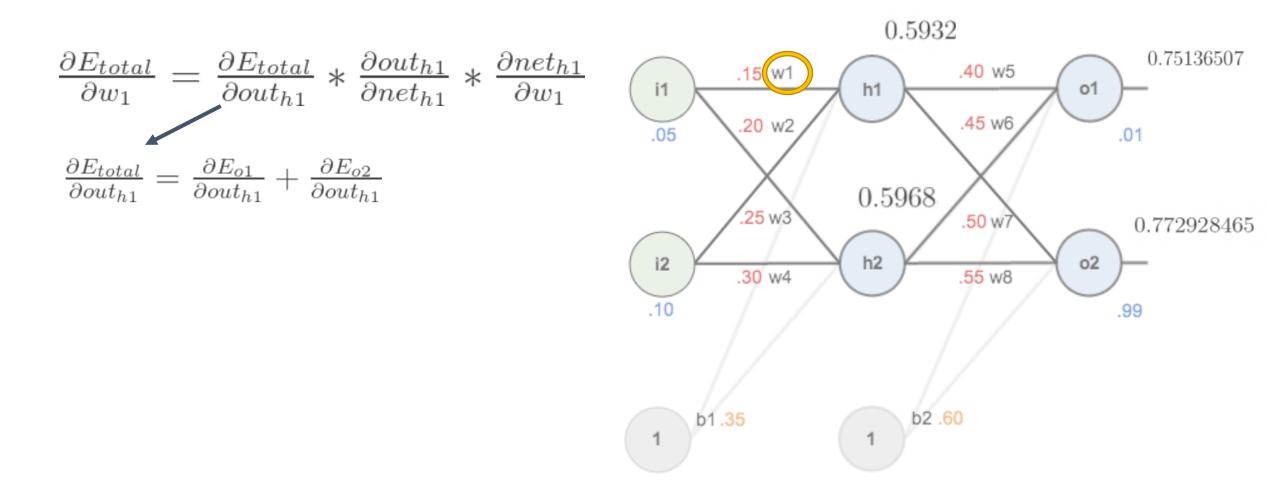
After that w5, w6, w7 and w8 have been updated we continue backwards to update w1, w2, w,3 and w4

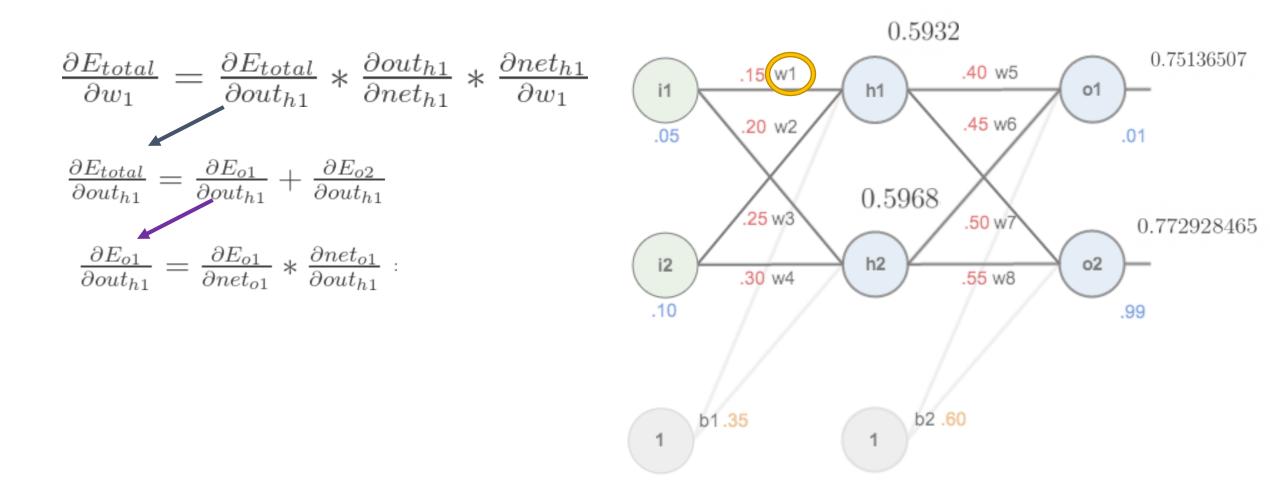


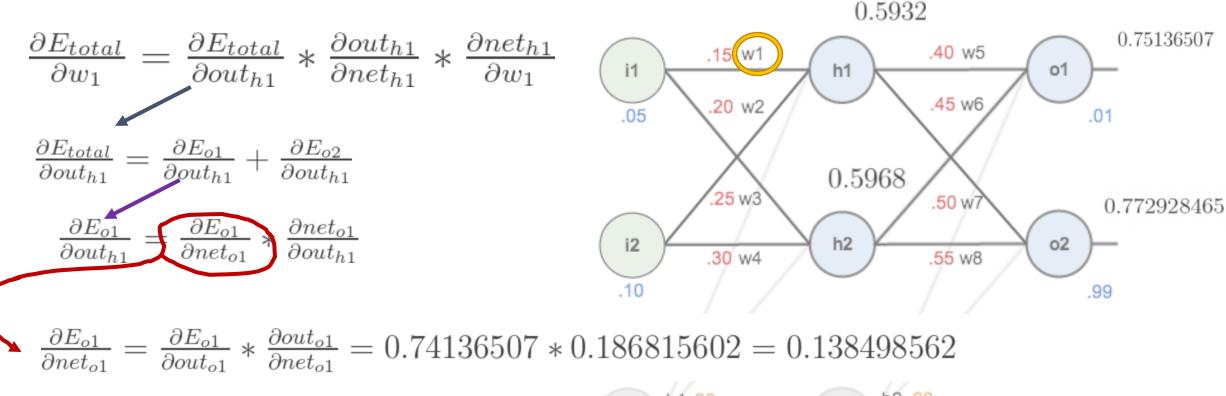
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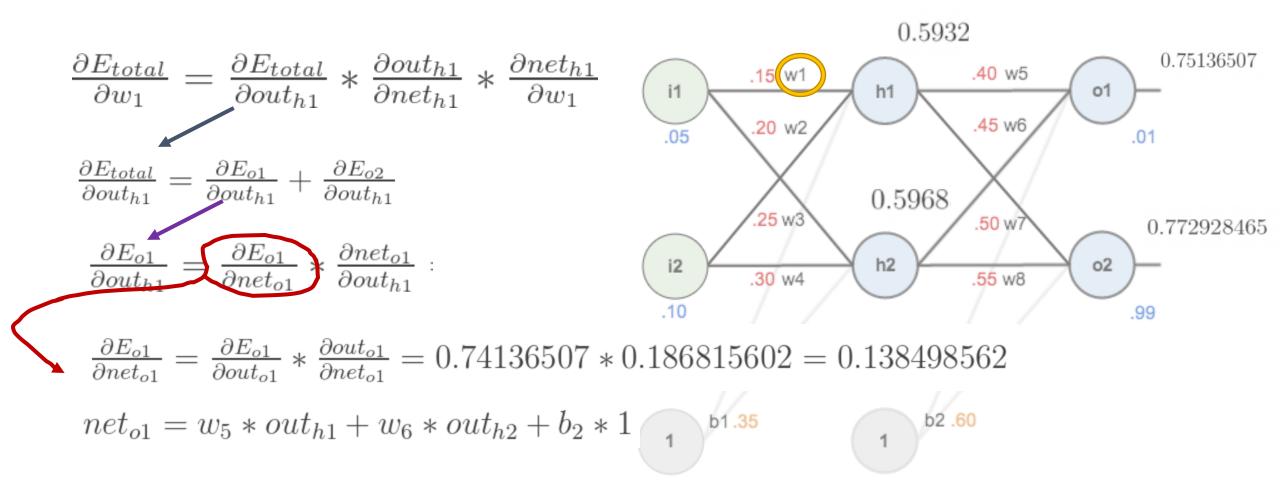


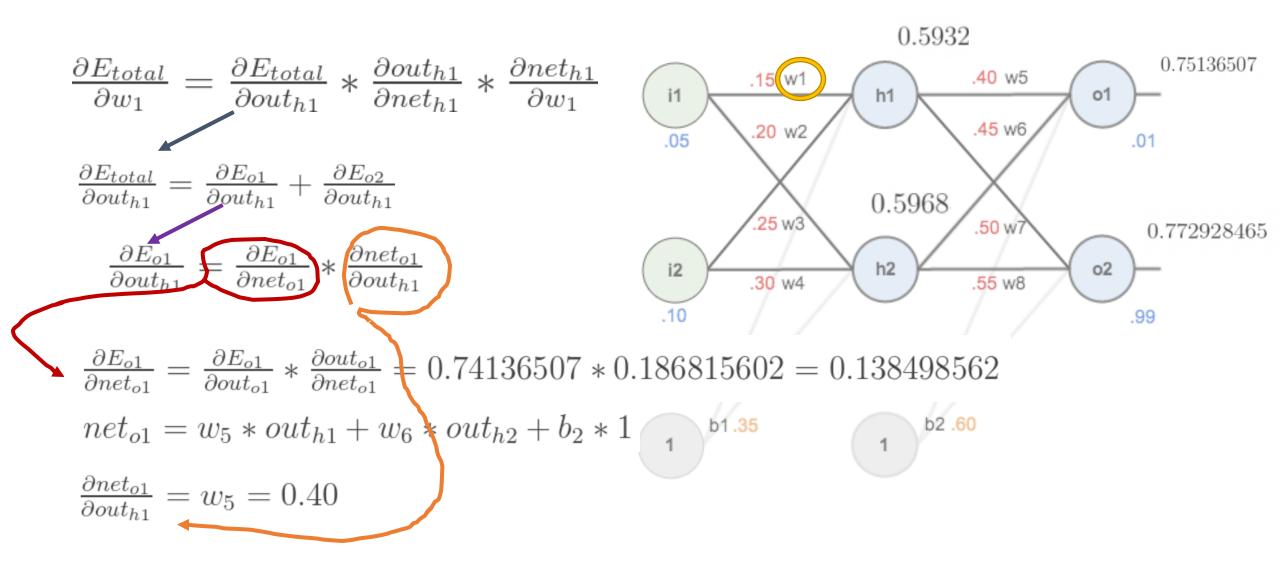


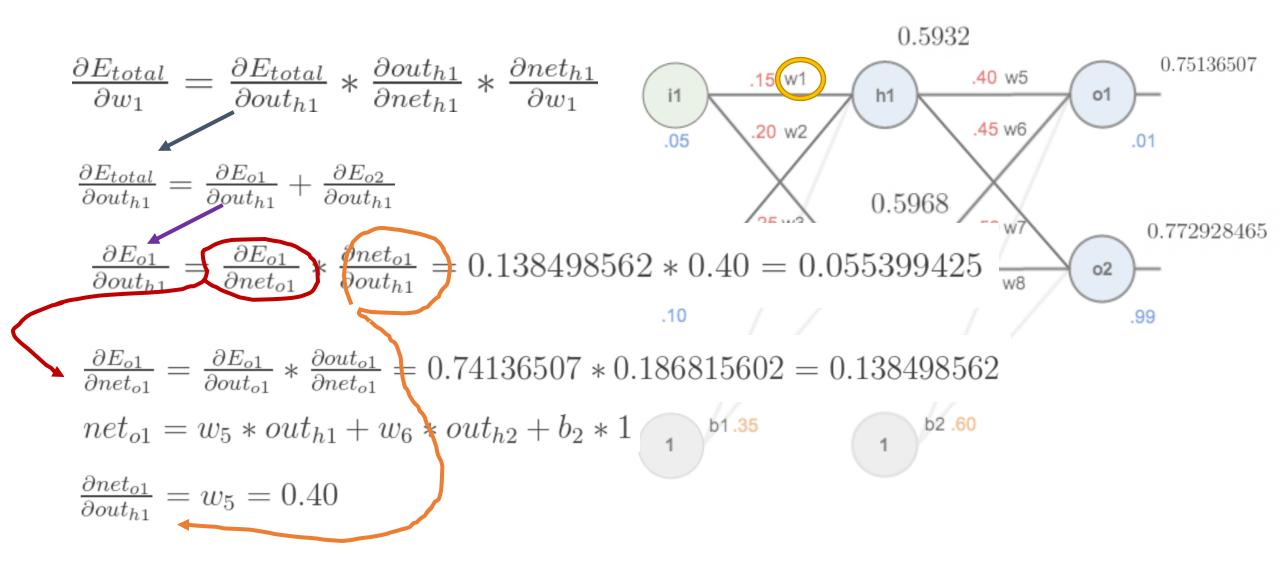


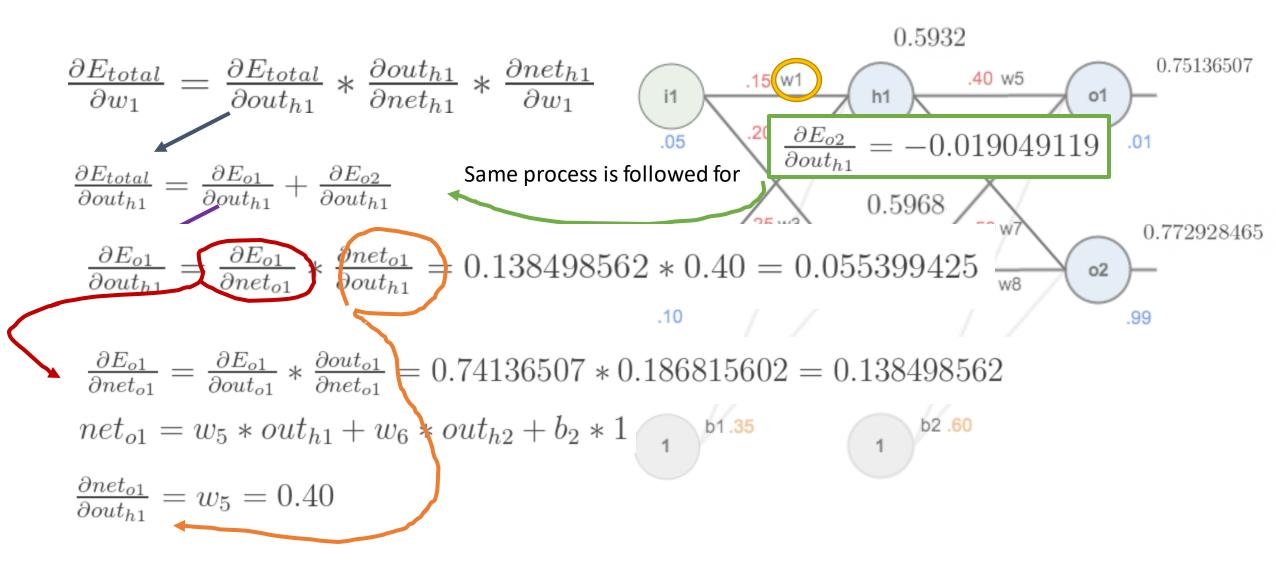


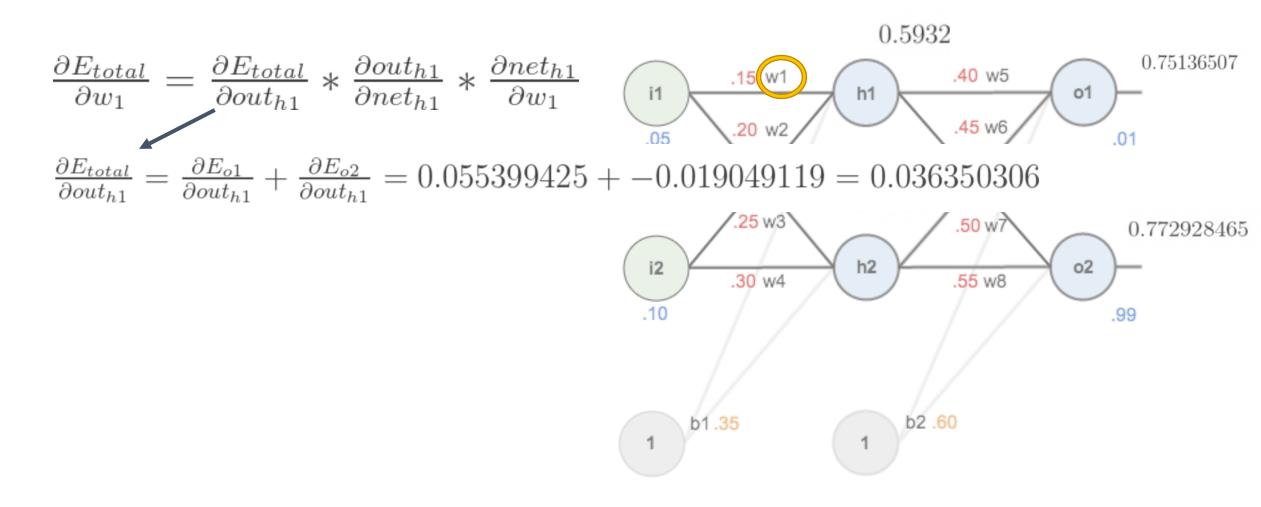


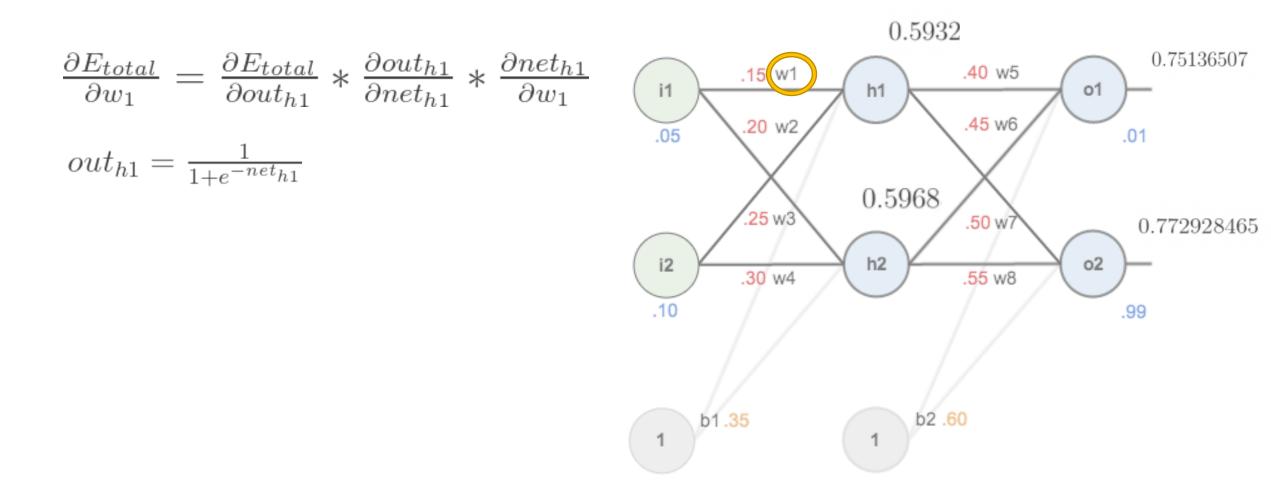


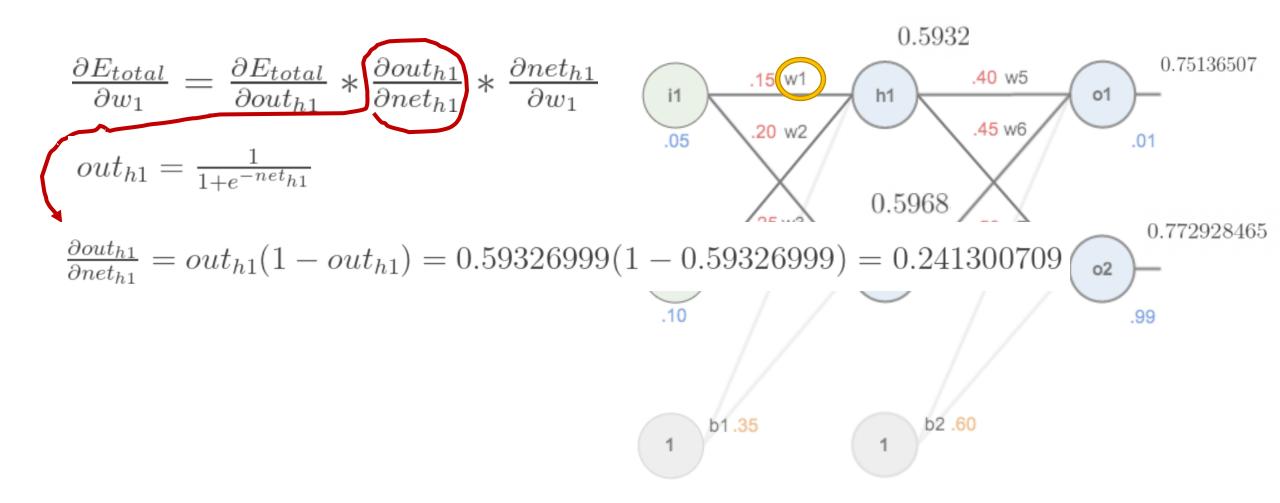












$$\frac{\partial E_{total}}{\partial w_1} = \frac{\partial E_{total}}{\partial out_{h1}} * \frac{\partial out_{h1}}{\partial net_{h1}} * \frac{\partial net_{h1}}{\partial w_1}$$

$$net_{h1} = w_1 * i_1 + w_3 * i_2 + b_1 * 1$$

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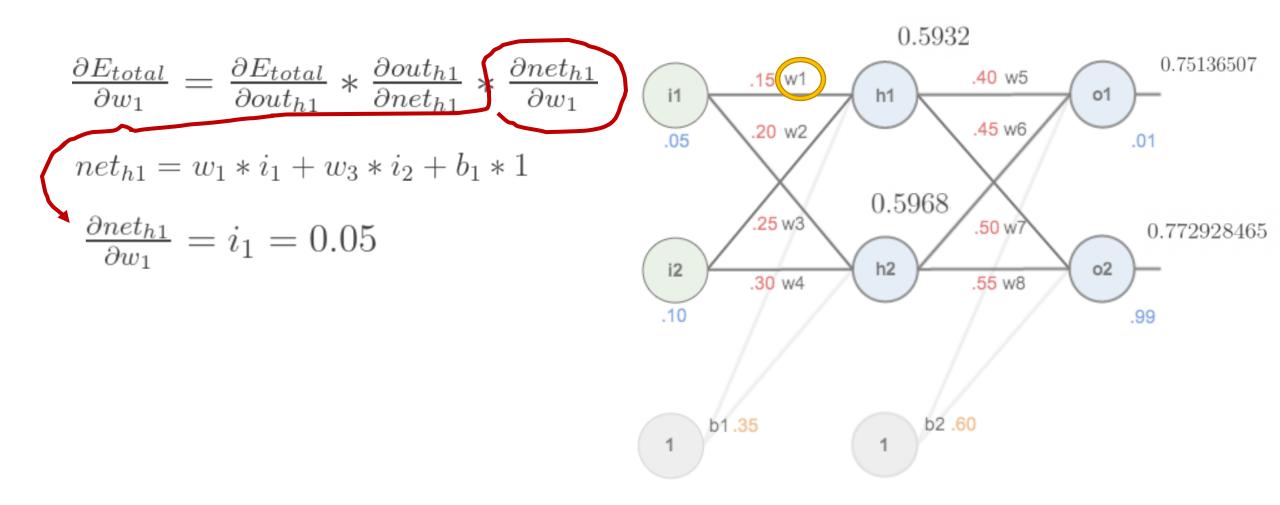
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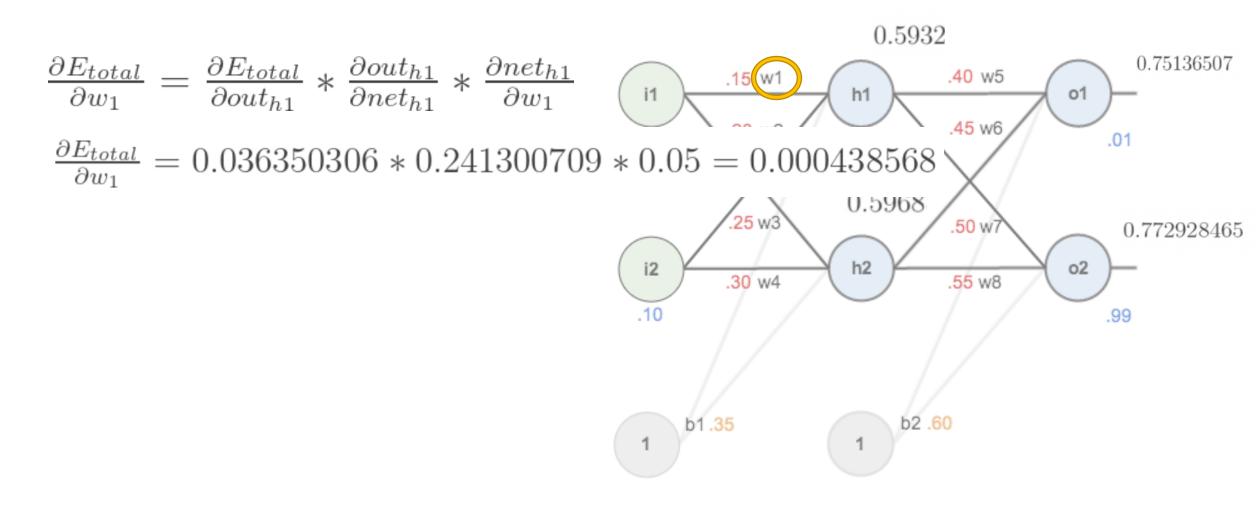
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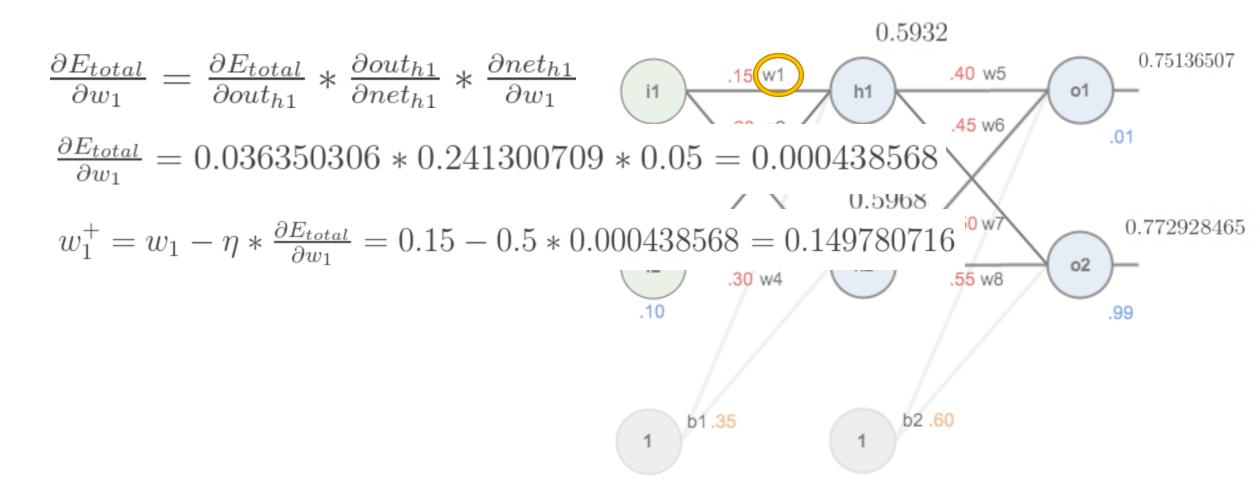
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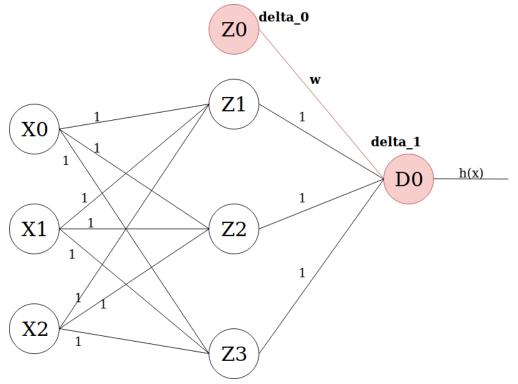


#### Example - The Backward Pass -



#### Backpropagation in other words

- In order to get the loss of a node (e.g. Z0), we multiply the value of its corresponding f'(z) by the loss of the node it is connected to in the next layer (delta\_1), by the weight of the link connecting both nodes.
- We do the delta calculation step at every unit, back-propagating the loss into the neural net, and finding out what loss every node/unit is responsible for.



https://towardsdatascience.com/how-does-back-propagation-in-artificial-neural-networks-work-c7cad873ea7

#### On the Key Importance of Error Functions

- The error/loss/cost function reduces all the various good and bad aspects of a possibly complex system down to a single number, a scalar value, which allows candidate solutions to be compared.
- It is important, therefore, that **the function faithfully represent our design goals**.
- If we choose a poor error function and obtain unsatisfactory results, the fault is ours for badly specifying the goal of the search.

#### **Objective Functions for NN**

- Regression: A problem where you predict a real-value quantity.
  - Output Layer: One node with a linear activation unit.
  - Loss Function: Quadratic Loss (Mean Squared Error (MSE))
- Classification: Classify an example as belonging to one of K classes
  - Output Layer:
    - One node with a sigmoid activation unit (K=2, binary cross-entropy)
    - K output nodes in a softmax layer (K>2, categorical cross-entropy)\*
  - Loss function: Cross-entropy (i.e. negative log likelihood)

J = EForwardBackwardQuadratic $J = \frac{1}{2}(y - y^*)^2$  $\frac{dJ}{dy} = y - y^*$ Cross Entropy<br/>(binary) $J = y^* \log(y) + (1 - y^*) \log(1 - y)$  $\frac{dJ}{dy} = y^* \frac{1}{y} + (1 - y^*) \frac{1}{y - 1}$ 

\*When K > 2 the target variable needs to be one-hot encoded

```
J = \sum y^* \log(y)
```

Cross Entropy (categorical)

#### **Design Issues in ANN**

- Number of nodes in input layer
  - One input node per binary/continuous attribute
  - *k* or *log*<sub>2</sub>*k* nodes for each categorical attribute with k values
- Number of nodes in output layer
  - One output for binary class problem
  - *k* or *log*<sub>2</sub>*k* nodes for k-class problem
- Number of nodes in hidden layer
- Initial weights and biases

#### **Characteristics of ANN**

- Multilayer ANN are universal approximators but could suffer from *overfitting* if the network is too large.
- Gradient descent may converge to *local minimum*.
- Model building can be very time consuming, but testing can be very fast.
- Can handle redundant attributes because weights are automatically learnt.
- Sensitive to noise in training data.
- Difficult to handle missing attributes.

## **Tips and Tricks of NN Training**

#### Dataset Should Normally be Split Into

- **Training set:** use to update the weights. Records in this set are repeatedly in random order. The weight update equation are applied after a certain number of records.
- Validation set: use to decide when to stop training only by monitoring the error and to select the best model configuration
- **Test set:** use to test the performance of the neural network. It should not be used as part of the neural network development and model selection cycle

- Choice of *initial weight values is important as this decides starting position in weight space.* That is, how far away from global minimum
  - Aim is to select weight values which produce midrange function signals
  - Select weight values randomly from uniform probability distribution
  - Normalize weight values so number of weighted connections per unit produces midrange function signal
- Try different random initialization to
  - Assess robustness
  - Have more opportunities to find optimal results

### Two learning fashion (plus one)

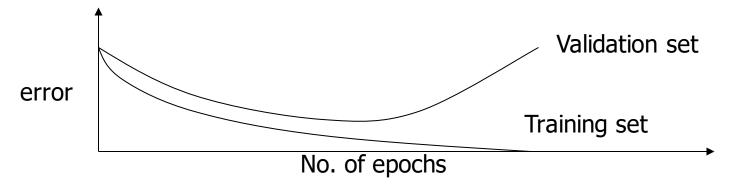
- **Sequential mode** (on-line, stochastic, or per-pattern)
  - Weights updated after each records is presented
  - Many weight updates, can quicker convergence but also make learning less stable
- Batch mode (off-line or per-epoch)
  - Weights updated after all records are presented
  - Can be very slow and lead to trapping in early local minima
- Minibatch mode (a blend of the two above)
  - Weights updated after a few records (from tens to thousands) are presented
  - Best of both (and good for GPU)

#### **Convergence** Criteria

- Learning is obtained by repeatedly supplying training data and adjusting by backpropagation
  - Typically 1 training set presentation = **1 epoch**
- We need a stopping criteria to define convergence
  - Euclidean norm of the gradient vector reaches a sufficiently small value
  - Absolute rate of change in the average squared error per epoch is sufficiently small
  - Validation for generalization performance: stop when generalization performance reaches a peak

## **Early Stopping**

- Running too many epochs may overtrain the network and result in overfitting and perform poorly in generalization
- Keep a hold-out validation set and test accuracy after every epoch. Maintain weights for best performing network on the validation set and stop training when error increases beyond this
- Always let the network run for some epochs before deciding to stop (patience parameter), then backtrack to best result



#### **Model Selection**

- **Too few hidden units** prevent the network from learning adequately fitting the data and learning the concept.
- Too many hidden units leads to overfitting, unless you regularize heavily (e.g. dropout, weight decay, weight penalties)
- Cross validation should be used to determine an appropriate number of hidden units by using the optimal validation error to select the model with optimal number of hidden layers and nodes.

#### Regularization

- Constrain the learning model to avoid overfitting and help improving generalization.
- Add **penalization terms** to the loss function that *punish* the model for excessive use of resources
  - Limit the **amount of weights** that is used to learn a task
  - Limit the **total activation of neurons** in the network

$$E' = E(y, y^*) + \lambda R(\cdot)$$

Hyperparameter to be chosen in model selection

 $R(W_{ heta})$  Penalty on parameters

R(Z)

Penalty on activations

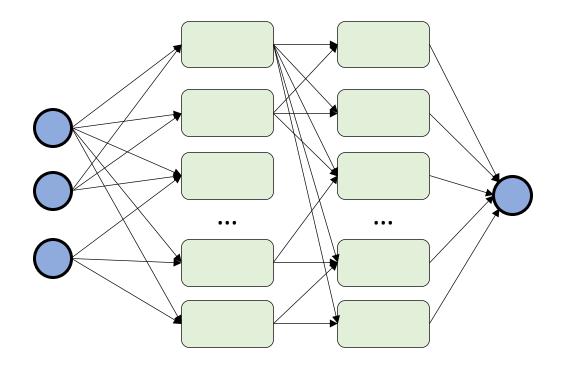
#### Common penalty terms (norms)

- 1-norm  $||A||_1 = \sum_{ij} |a_{ij}|$ 
  - Parameters:  $R(W_{\theta}) = ||W_{\theta}||_{1}^{2}$
  - Activations:  $R(Z(X)) = ||Z(X)||_1^2$  (Z hidden unit activation)

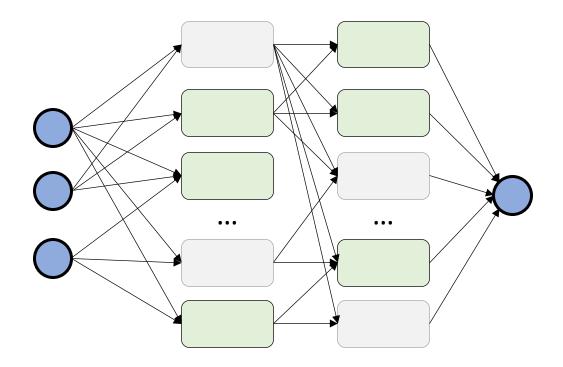
• 2-norm 
$$||A||_2 = \sqrt{\sum_{ij} a_{ij}^2}$$

- Parameters:  $R(W_{\theta}) = ||W_{\theta}||_2^2$
- Activations:  $R(Z(X)) = ||Z(X)||_2^2$  (Z hidden unit activation)
- Any p-norm and more...

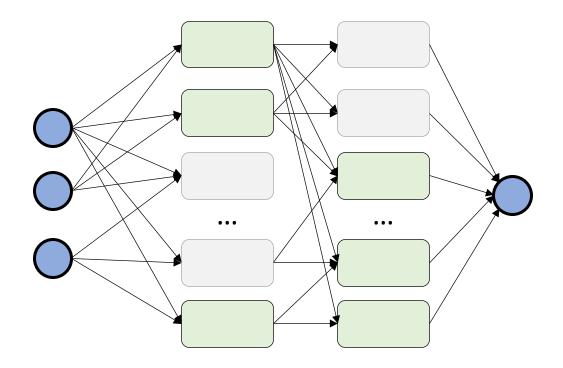
Randomly disconnect units from the network during training



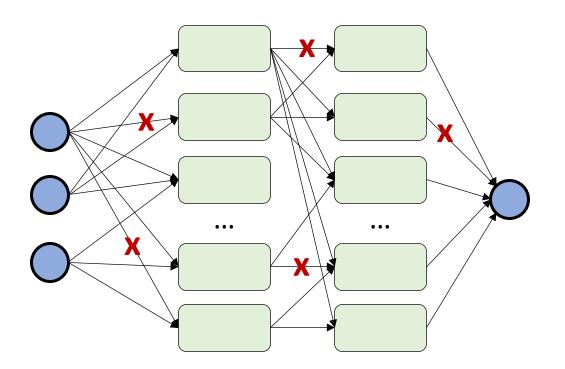
Randomly disconnect units from the network during training



Randomly disconnect units from the network during training



Randomly disconnect units from the network during training



You can also **drop single connections** (dropconnect)

- Regulated by unit dropping hyperparameter
- Prevents unit coadaptation
- Committee machine effect
- Need to adapt **prediction phase**
- Used at prediction time gives predictions with confidence intervals

#### Momentum

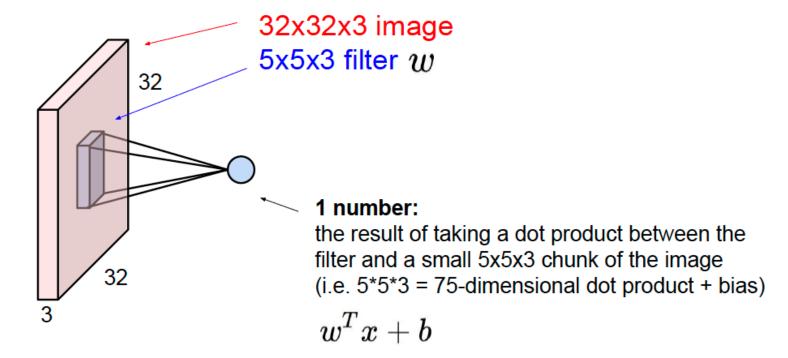
- Adding a term to weight update equation to store an exponentially weight history of previous weights changes
- Reducing problems of instability while increasing the rate of convergence
  - If weight changes tend to have same signs, the momentum term increases and gradient decrease speed up convergence on shallow gradient
  - If weight changes tend have opposing signs, the momentum term decreases and gradient descent slows to reduce oscillations (stabilizes)
  - Can help escape being trapped in local minima

### **Choosing the Optimization Algorithm**

- Standard Stochastic Gradient Descent (SGD)
  - Easy and efficient
  - Difficult to pick up the best learning rate
  - Unstable convergence
  - Often used with momentum (exponentially weighted history of previous weights changes)
- RMSprop
  - Adaptive learning rate method (reduces it using a moving average of the squared gradient)
  - Fastens convergence by having quicker gradients when necessary
- Adagrad
  - Like RMSprop with element-wise scaling of the gradient
- ADAM
  - Like Adagrad but adds an exponentially decaying average of past gradients like momentum

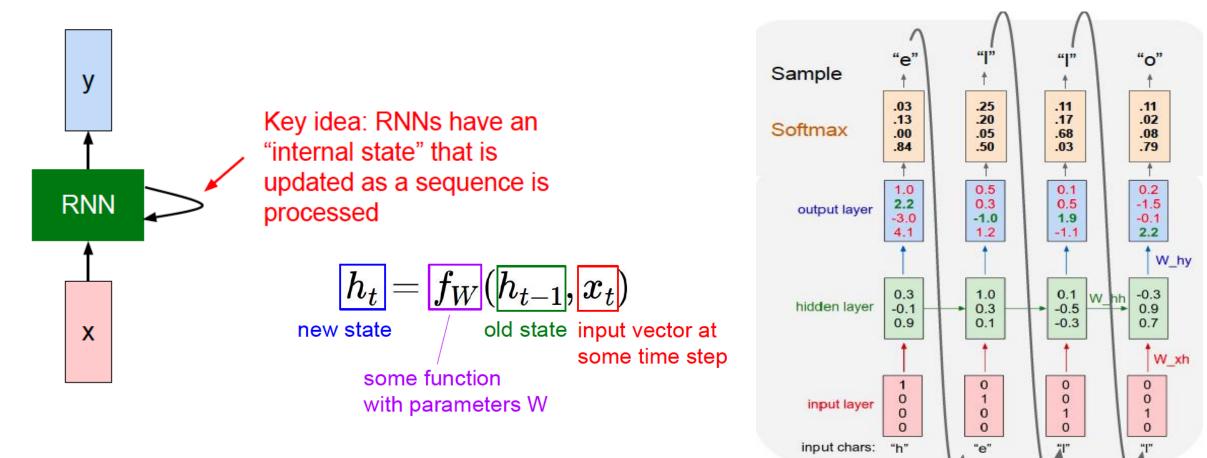
#### **Convolutional Neural Networks**

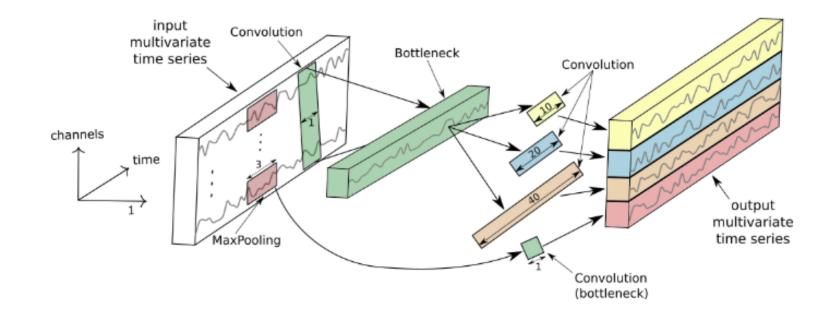
- Are typically applied for the classification of images and time series
- Instead of having only "fully connected" layers adopt "convolutional layers"



#### **Recurrent Neural Network**

• Are typically applied in natural language processing (NLP).





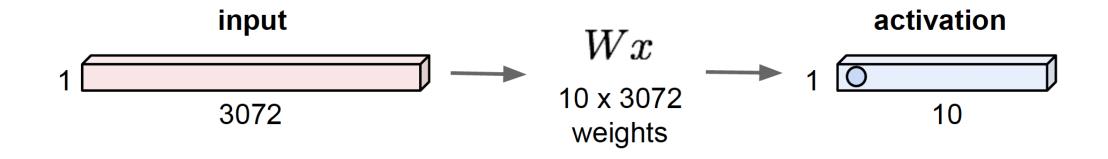
# **Convolutional Neural Network**

Slides edited from Stanford

http://cs231n.stanford.edu/slides/2019/cs231n\_2019\_lecture09.pdf

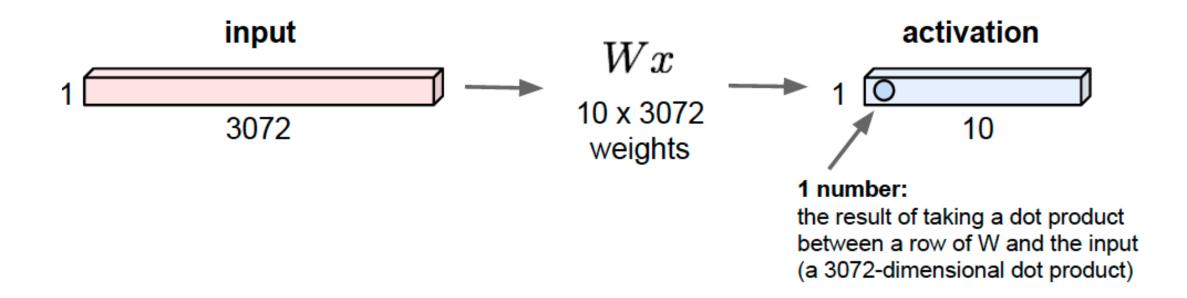
#### **Fully Connected Layer**

#### 32x32x3 image -> stretch to 3072 x 1

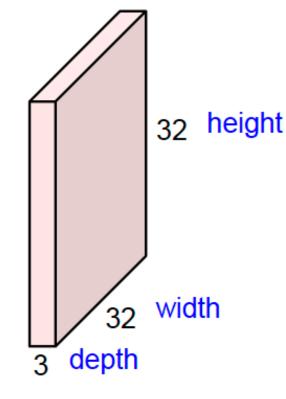


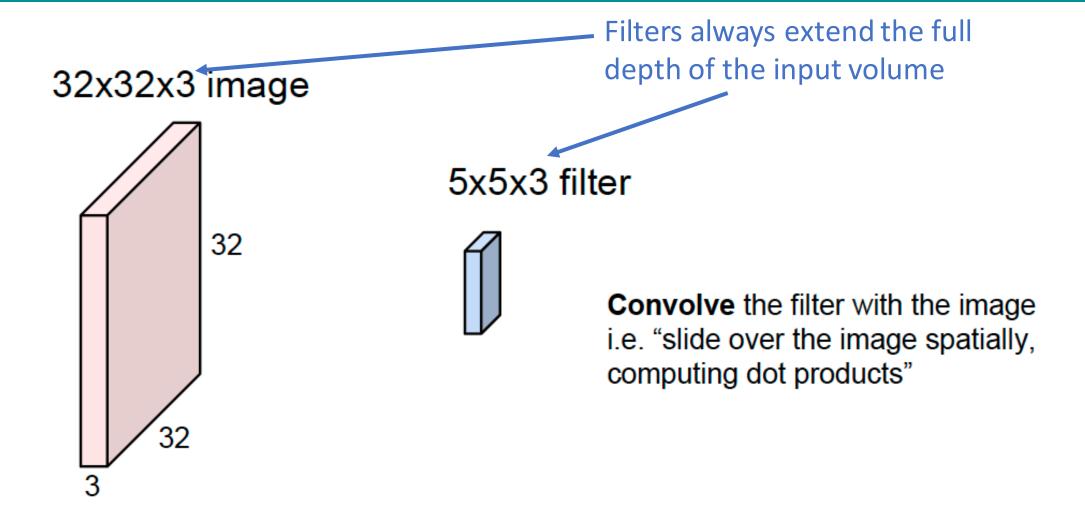
#### **Fully Connected Layer**

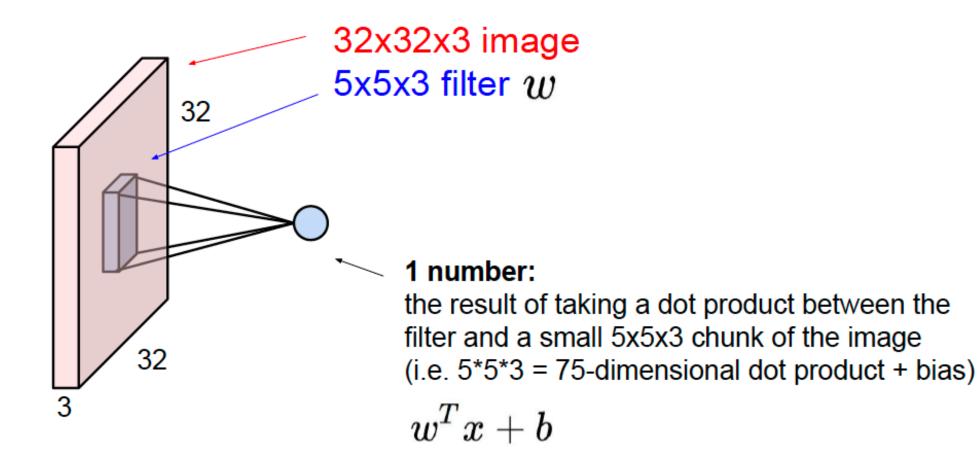
#### 32x32x3 image -> stretch to 3072 x 1

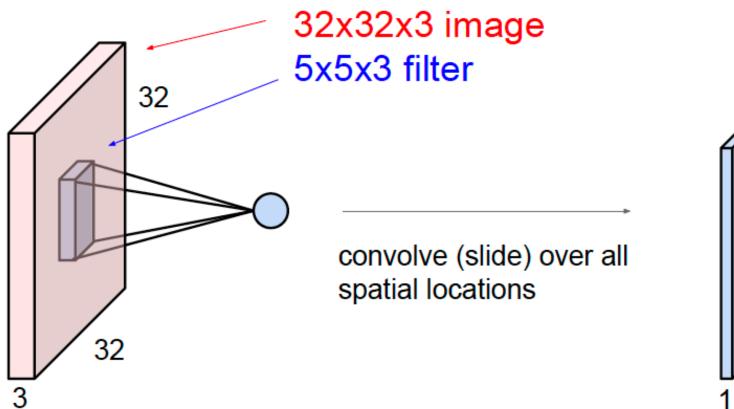


32x32x3 image -> preserve spatial structure

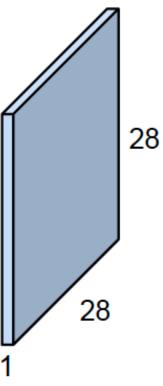


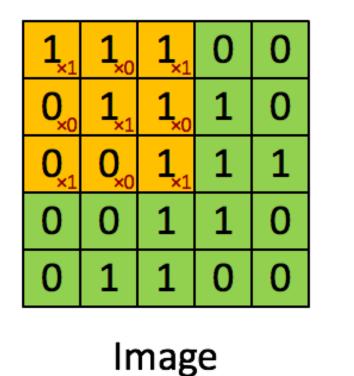


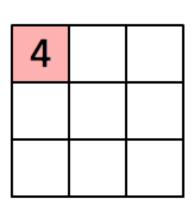


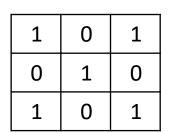


#### activation map









Convolution Kernel

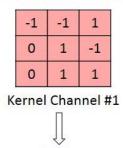
Convolved Feature

0	0	0	0	0	0	
0	156	155	156	158	158	
0	153	154	157	159	159	
0	149	151	155	158	159	( <b></b>
0	146	146	149	153	158	
0	145	143	143	148	158	·

0	0	0	0	0	0	
0	167	166	167	169	169	
0	164	165	168	170	170	
0	160	162	166	169	170	
0	156	156	159	163	168	
0	155	153	153	158	168	

0	0	0	0	0	0	
0	163	162	163	165	165	
0	160	161	164	166	166	
0	156	158	162	165	166	
0	155	155	158	162	167	
0	154	152	152	157	167	

Input Channel #1 (Red)



308

+

1	0	0
1	-1	-1
1	0	-1

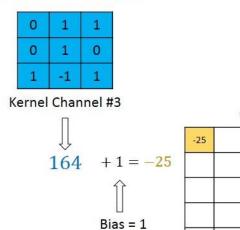
Input Channel #2 (Green)

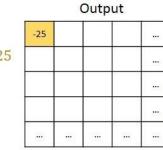
Kernel Channel #2

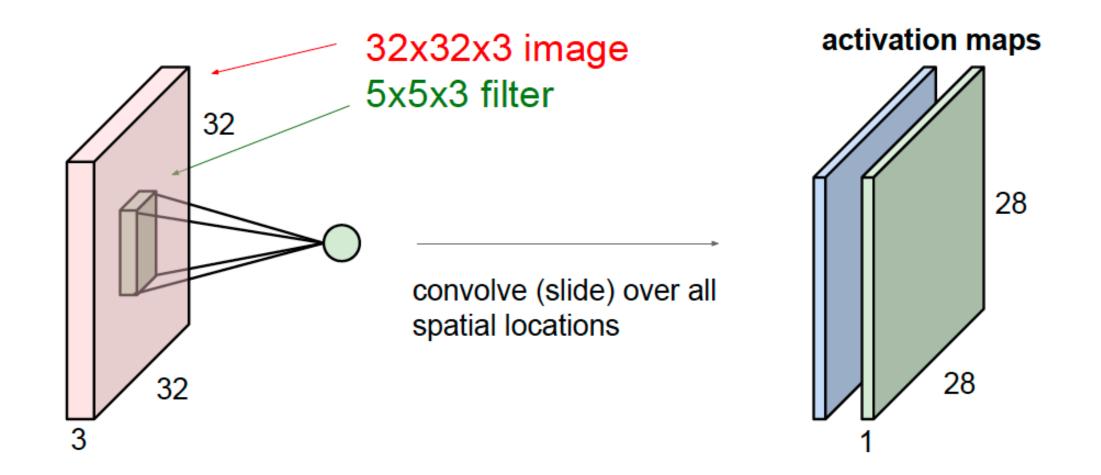
-498

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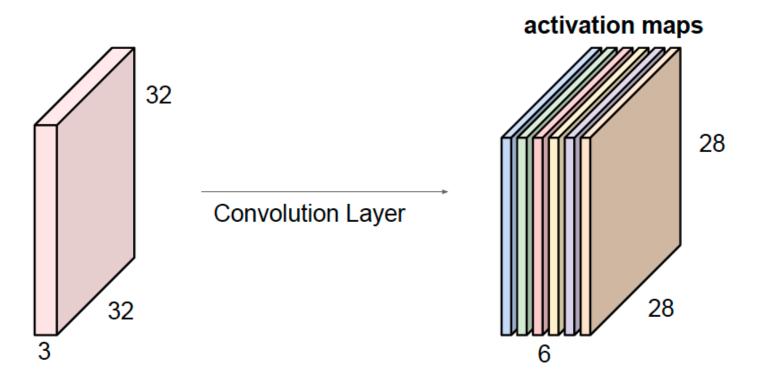
Input Channel #3 (Blue)





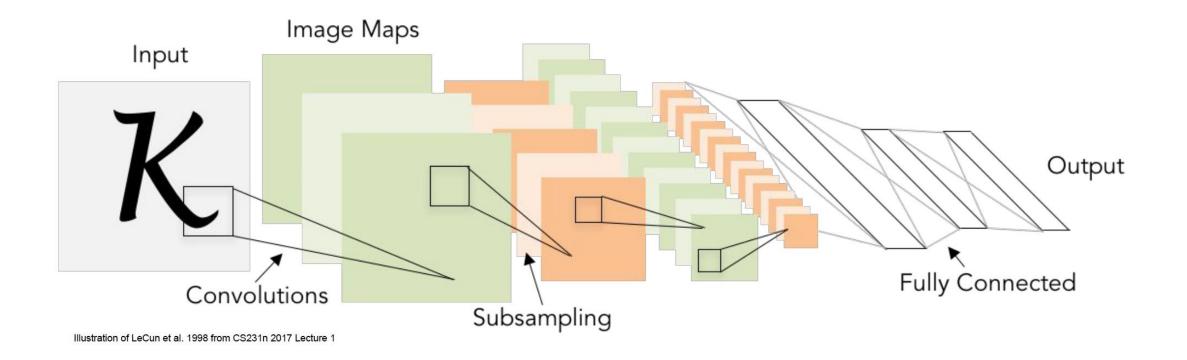


For example, if we had 6 5x5 filters, we'll get 6 separate activation maps:



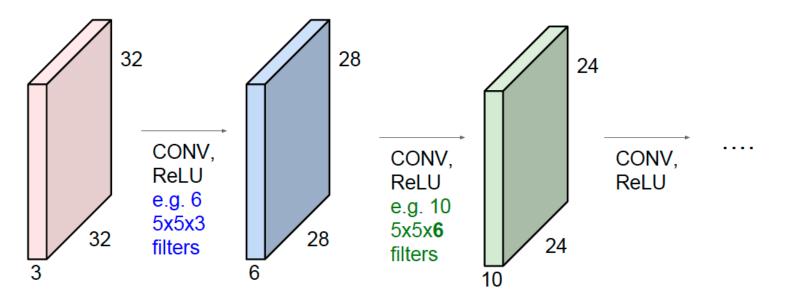
We stack these up to get a "new image" of size 28x28x6!

#### **Convolutional Neural Network**

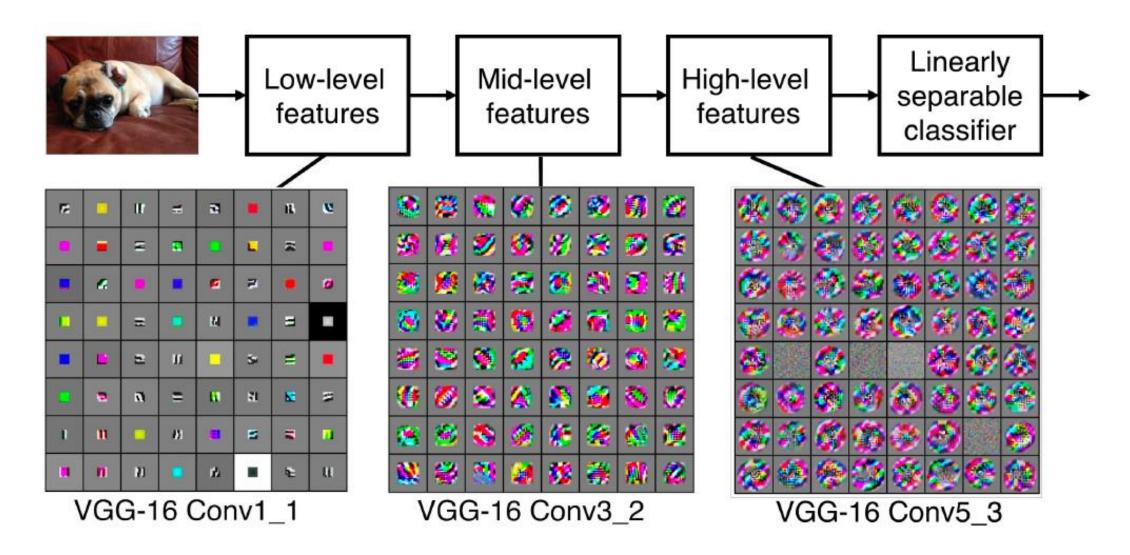


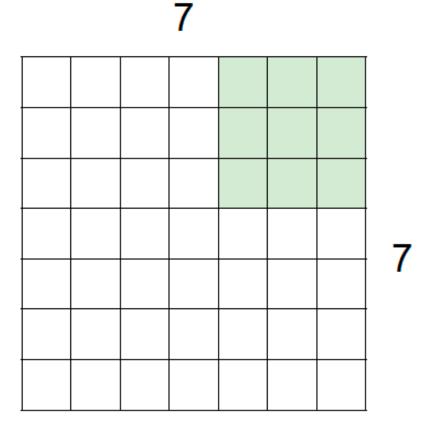
#### **Convolutional Neural Network**

- CNN is a sequence of Conv Layers, interspersed with activation functions.
- CNN shrinks volumes spatially.
- E.g. 32x32 input convolved repeatedly with 5x5 filters! (32 -> 28 -> 24 ...).
- Shrinking too fast is not good, doesn't work well.



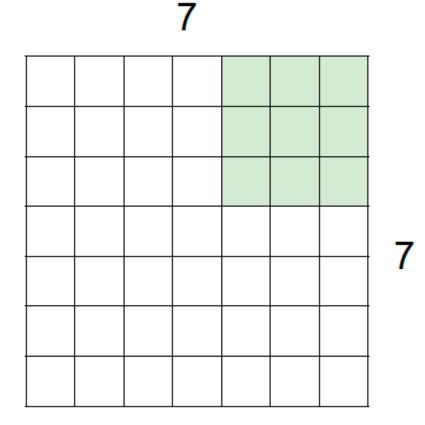
### **CNN for Image Classification**



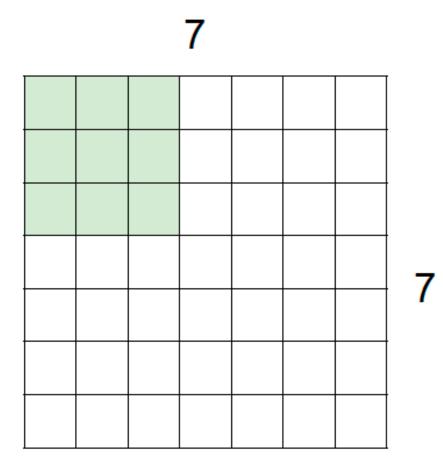


7x7 input (spatially) assume 3x3 filter

=> 5x5 output



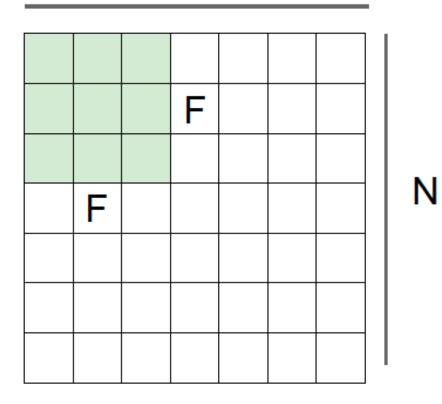
7x7 input (spatially) assume 3x3 filter applied with stride 2 => 3x3 output!



7x7 input (spatially) assume 3x3 filter applied **with stride 3?** 

doesn't fit! cannot apply 3x3 filter on 7x7 input with stride 3.

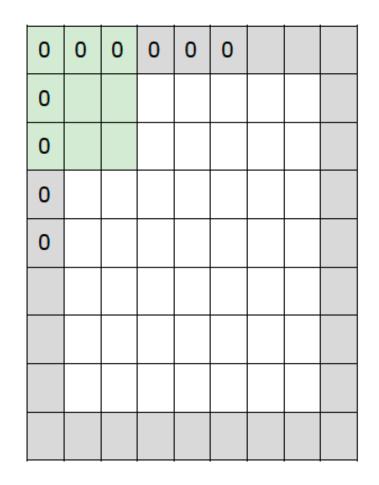
Ν



Output size: (N - F) / stride + 1

e.g. N = 7, F = 3: stride 1 => (7 - 3)/1 + 1 = 5 stride 2 => (7 - 3)/2 + 1 = 3 stride 3 => (7 - 3)/3 + 1 = 2.33 :\

## Padding



e.g. input 7x7
3x3 filter, applied with stride 1
pad with 1 pixel border => what is the output?

#### 7x7 output!

In general, common to see CONV layers with stride 1, filters of size FxF, and zero-padding with (F-1)/2. (will preserve size spatially)

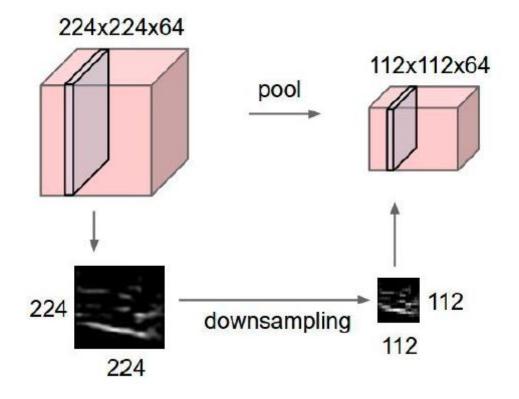
- F = 3 => zero pad with 1 pixel
- F = 5 => zero pad with 2 pixel
- F = 7 => zero pad with 3 pixel

## **Convolution Summary**

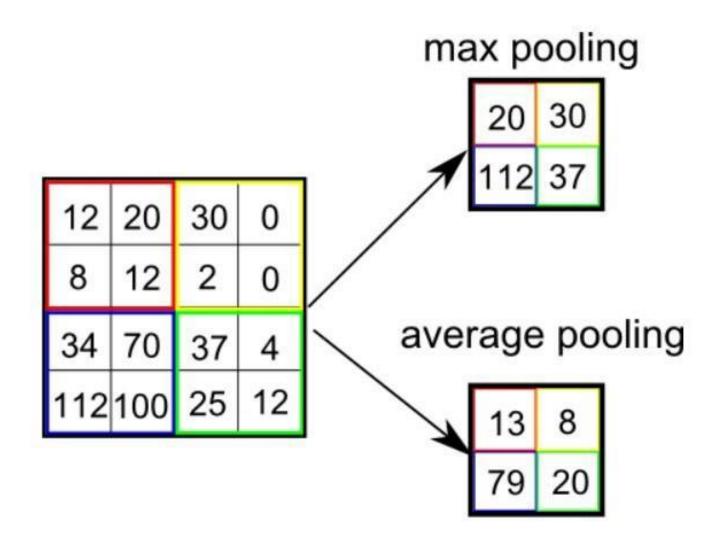
- Accepts a volume of size  $W_1 imes H_1 imes D_1$
- Requires four hyperparameters:
  - Number of filters K,
  - $\circ$  their spatial extent F,
  - the stride S,
  - the amount of zero padding P.
- Produces a volume of size  $W_2 imes H_2 imes D_2$  where:
  - $\circ W_2 = (W_1 F + 2P)/S + 1$
  - $\circ~H_2=(H_1-F+2P)/S+1$  (i.e. width and height are computed equally by symmetry)
  - $\circ D_2 = K$
- With parameter sharing, it introduces F · F · D<sub>1</sub> weights per filter, for a total of (F · F · D<sub>1</sub>) · K weights and K biases.
- In the output volume, the d-th depth slice (of size  $W_2 \times H_2$ ) is the result of performing a valid convolution of the d-th filter over the input volume with a stride of S, and then offset by d-th bias.

## **Pooling Layer**

- Makes the representations smaller and more manageable
- Operates over each activation map independently



## MaxPooling and AvgPoling



## **Pooling Summary**

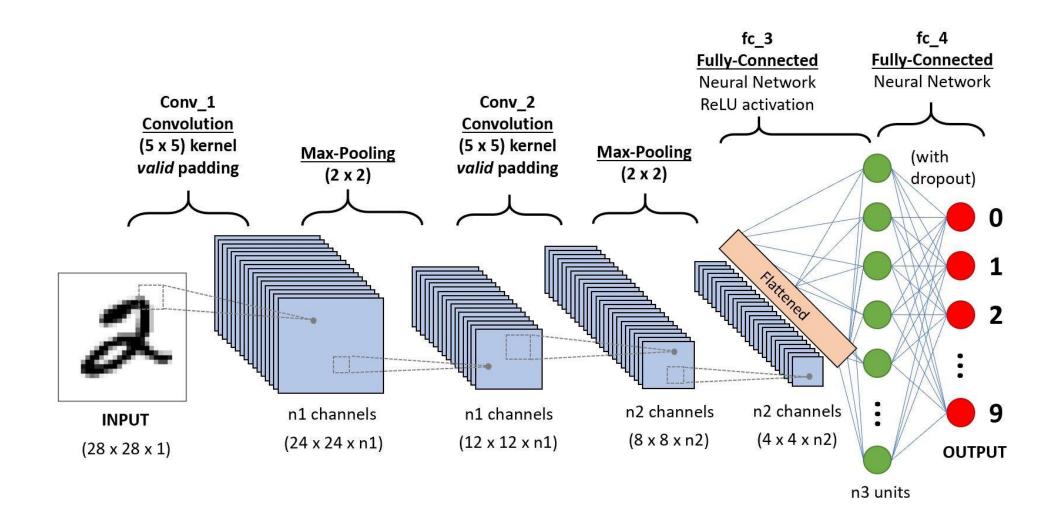
- Accepts a volume of size  $W_1 imes H_1 imes D_1$
- Requires three hyperparameters:
  - their spatial extent F,
  - $\circ\;$  the stride S ,
- Produces a volume of size  $W_2 imes H_2 imes D_2$  where:

$$\circ W_2 = (W_1 - F)/S + 1$$

$$H_2 = (H_1 - F)/S + 1$$

- $\circ D_2 = D_1$
- Introduces zero parameters since it computes a fixed function of the input
- Note that it is not common to use zero-padding for Pooling layers

### Example of CNN

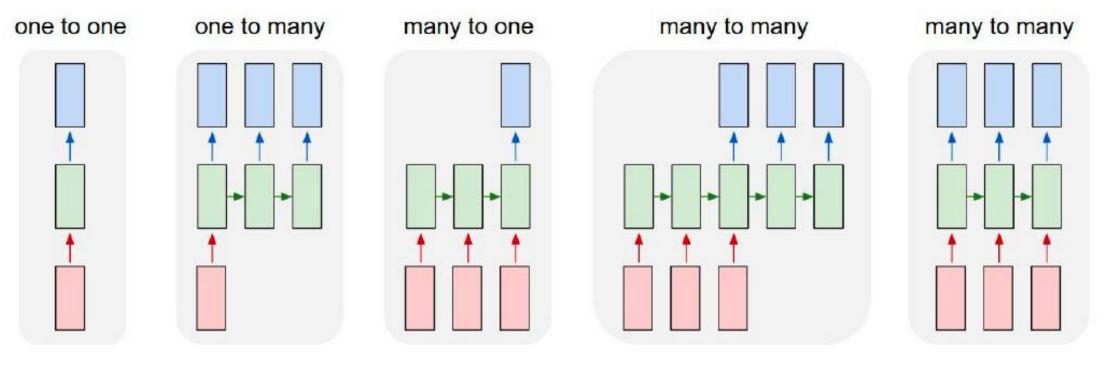


# **Recurrent Neural Network**

Slides edited from Stanford

http://cs231n.stanford.edu/slides/2019/cs231n\_2019\_lecture10.pdf

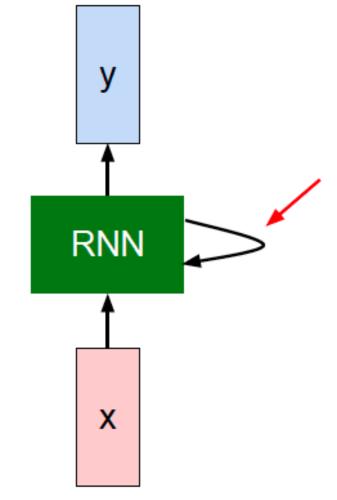
## **Types of Recurrent Neural Networks**



Vanilla NN

Image --> Sequence of Words --> Sequence of Words Sentiment Image Captioning Sentiment Classification TS Classification Sequence of Words --> Sequence of Words Machine Translation Video Classification

#### **Recurrent Neural Network - RNN**



Key idea: RNNs have an "internal state" that is updated as a sequence is processed

#### **Recurrent Neural Network - RNN**

 We can process a sequence of vectors *x* by applying a *recurrence formula* at every time step:

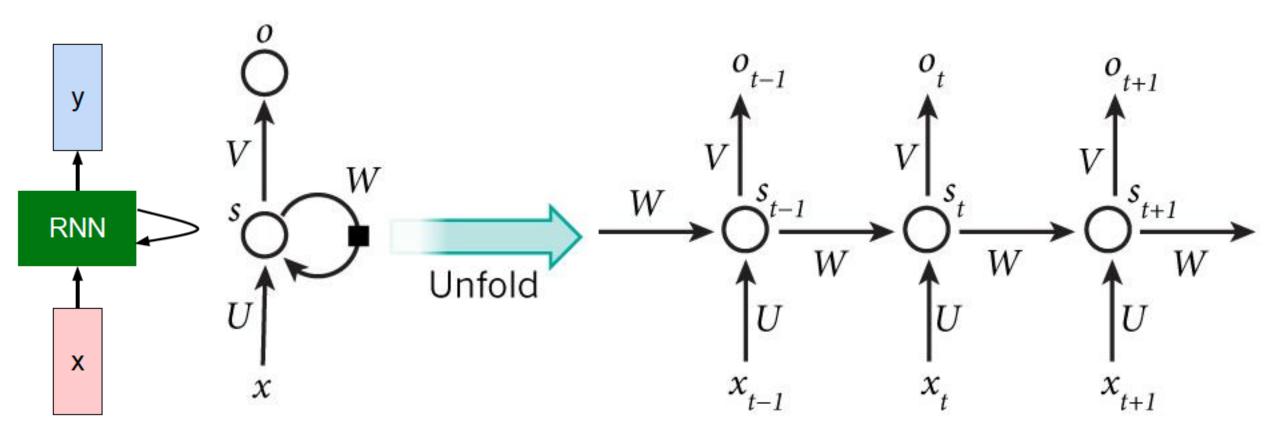
y

RNN

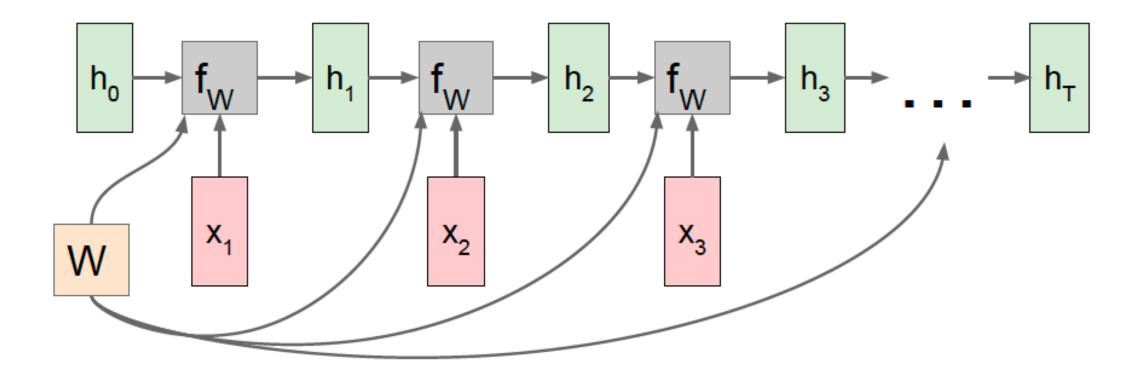
Х

$$egin{aligned} h_t = f_W(h_{t-1}, x_t) \ ext{new state} & ext{old state input vector at some time step} \ ext{some function} \ ext{with parameters W} \end{aligned}$$

#### **Unfolded RNN**

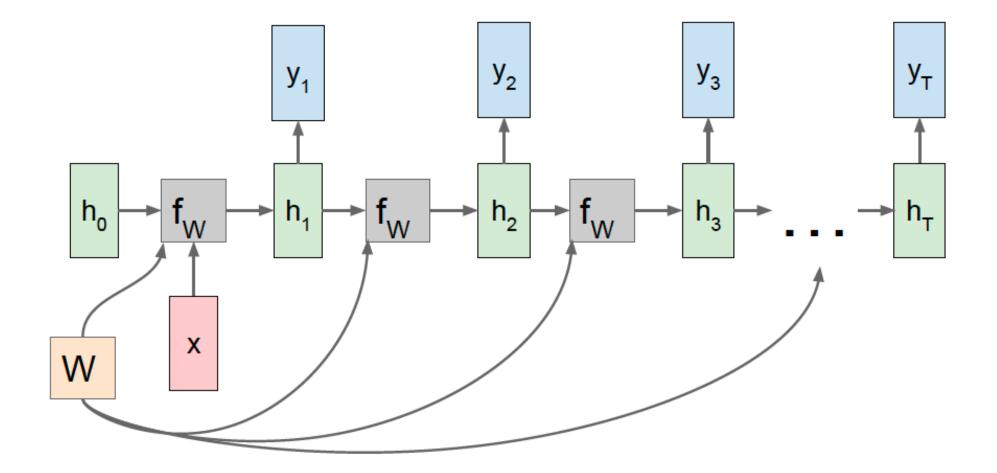


#### RNN: Computational Graph

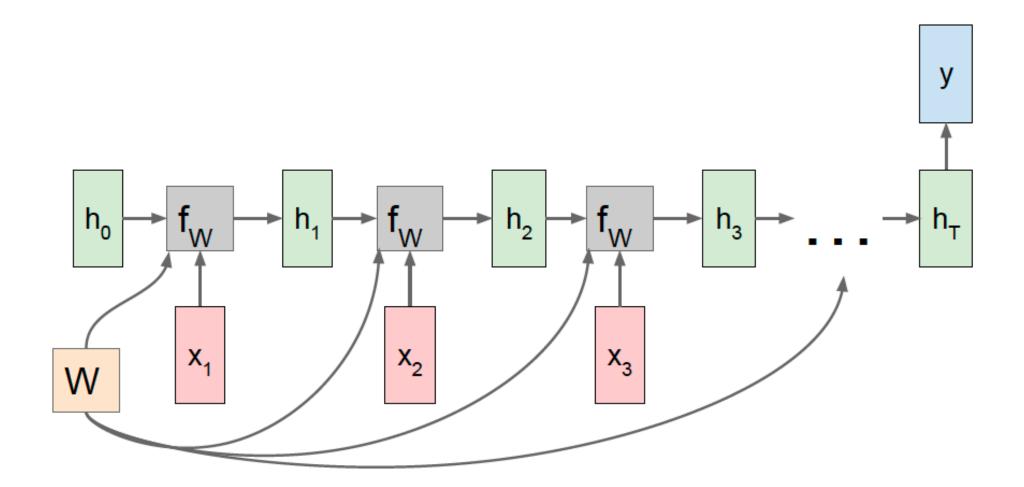


Reminder: Re-use the same weight matrix at every time-step

#### RNN: Computational Graph: Many to Many



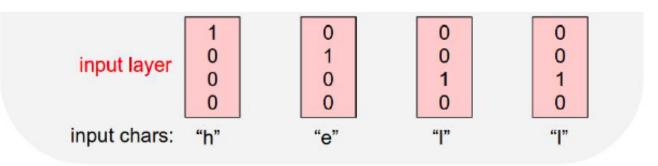
#### RNN: Computational Graph: Many to One



### **RNN: Example Training**

Vocabulary: [h,e,l,o]

Example training sequence: **"hello"** 

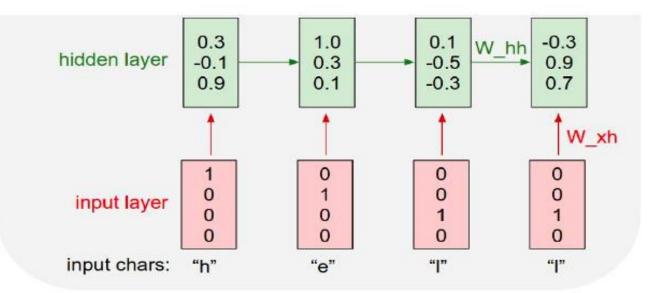


### **RNN: Example Training**

Example: Character-level Language Model

Example training sequence: "hello"

$$h_t = anh(W_{hh}h_{t-1} + W_{xh}x_t)$$

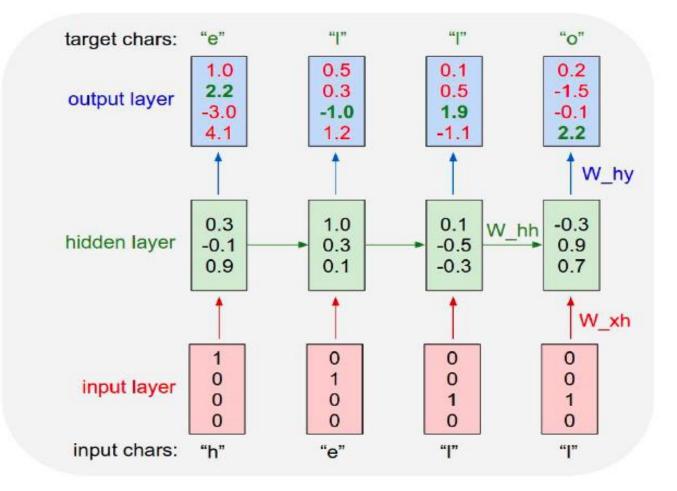


## **RNN: Example Training**

Example: Character-level Language Model

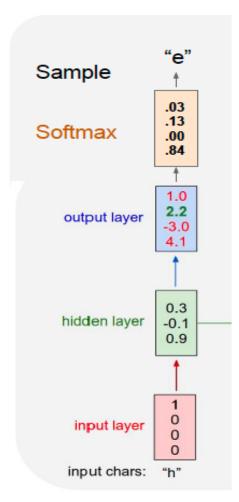
Vocabulary: [h,e,l,o]

Example training sequence: "hello"



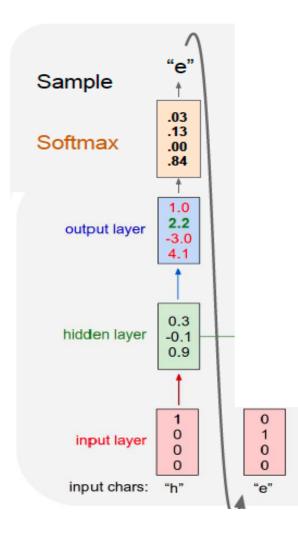
Example: Character-level Language Model Sampling

Vocabulary: [h,e,l,o]



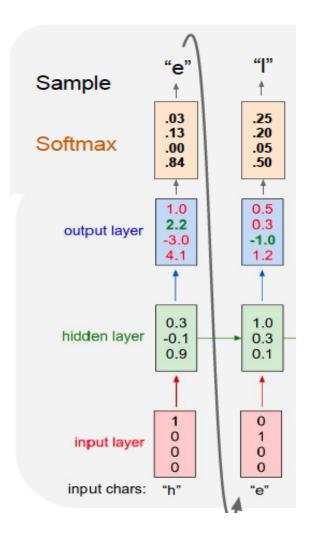
Example: Character-level Language Model Sampling

Vocabulary: [h,e,l,o]



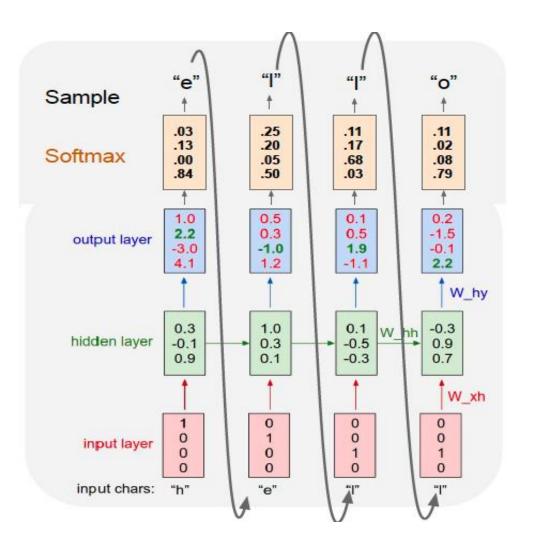
Example: Character-level Language Model Sampling

Vocabulary: [h,e,l,o]



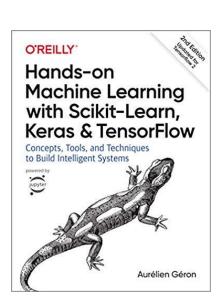
Example: Character-level Language Model Sampling

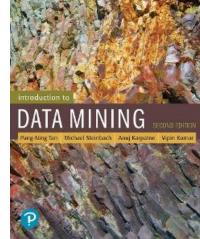
Vocabulary: [h,e,l,o]

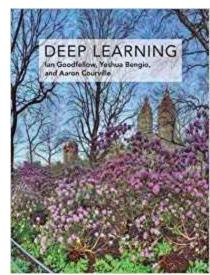


## References

- Artificial Neural Network. Chapter 5.4 and 5.5. Introduction to Data Mining.
- Hands-on Machine Learning with Scikit-Learn, Keras & Tensorflow. A practical handbook to start wrestling with Machine Learning models (2nd ed).
- Deep Learning. Ian Goodfellow, Yoshua Bengio, and Aaron Courville. The reference book for deep learning models.



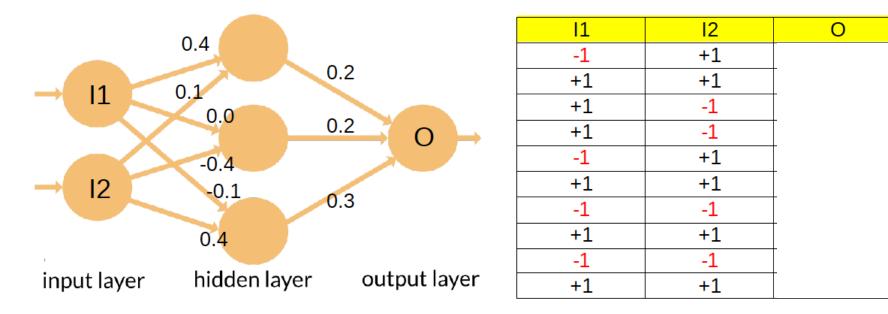




## **Exercises - Neural Network**

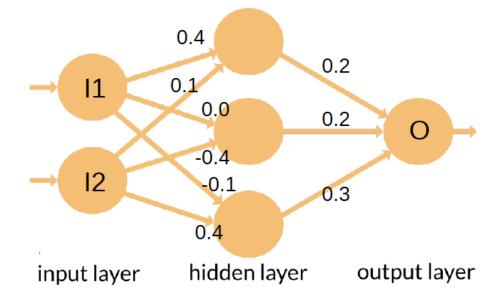
#### Predict with a Neural Network

- Given the following NN with
  - assigned weights (see figure)
  - activation function f(S) = sign(S-0.2) for all nodes
- Label the test set on the right, then compute accuracy, and precision & recall for both classes



## Predict with a Neural Network - Solution

- Given the following NN with
  - assigned weights (see figure)
  - activation function f(S) = sign(S-0.2) for all nodes
- Label the test set on the right, then compute accuracy and precision & recall for both classes



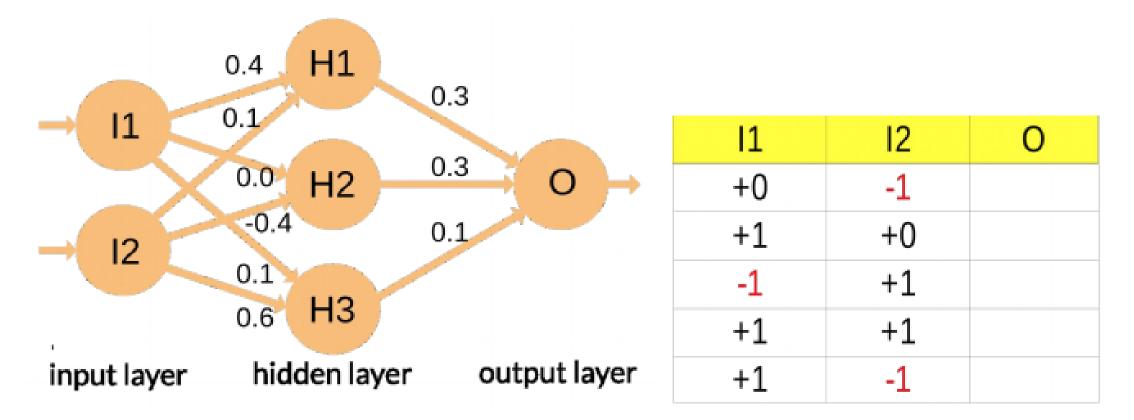
	——————————————————————————————————————
12	c = si
+1	-1
+1	+1
-1	-1
-1	+1
+1	+1
+1	+1
-1	-1
+1	-1
-1	-1
+1	+1
	+1 +1 -1 -1 +1 +1 -1 +1 -1 -1

 $H_{1} = sign(0.4 * -1 + 0.1 * 1 - 0.2) =$ = sign(-0.5) = -1  $H_{2} = sign(0.0 * -1 + -0.4 * 1 - 0.2) =$ = sign(-0.6) = -1  $H_{3} = sign(-0.1 * -1 + 0.4 * 1 - 0.2) =$ = sign(0.3) = 1

$$Y_1 = sign(0.2 * -1 + 0.2* -1 + 0.3 * 1 - 0.2) =$$

## Predict with a Neural Network

Given the neural network below (on the left), apply it to the test set provided (on the right). The weights are reported beside each connection, while the activation function is simply f(S) = sign(S), i.e. -1 for positive values, +1 for positive ones and 0 for S=0. For each case, show the output also of the nodes on the hidden layer.



### Predict with a Neural Network - Solution

